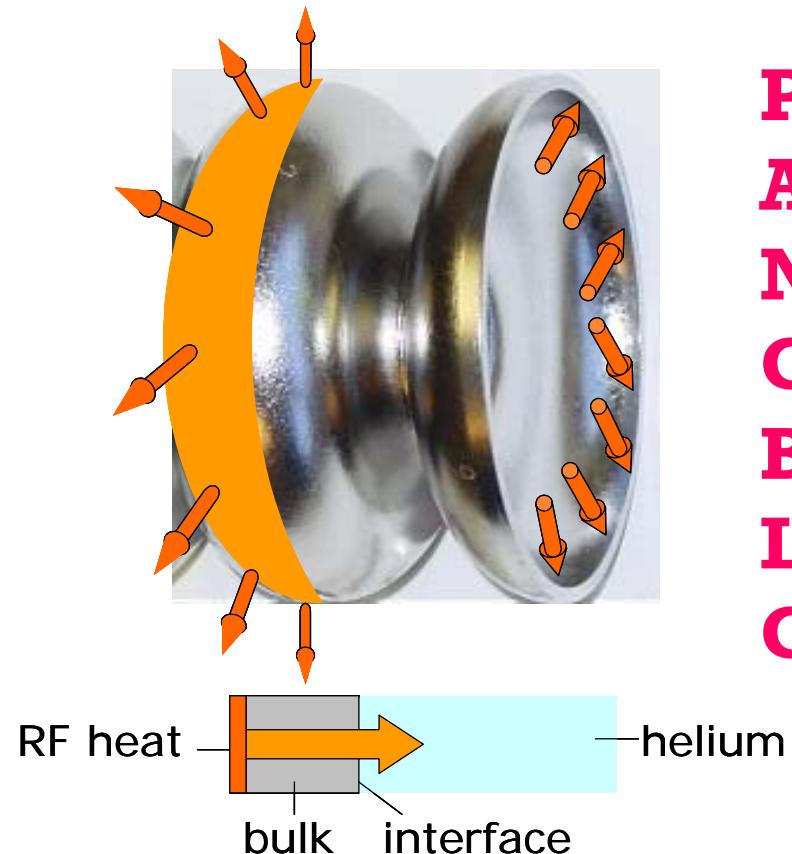


# **Evidence of Non-Linear BCS Resistance in Multi-Lab Cavity Data to Model Comparison**



**P. Bauer - FNAL,  
A. Gurevich – ASC-UW,  
N. Solyak - FNAL,  
G. Ciovati - JLab,  
B. Visentin - CEA,  
L. Lilje - DESY.  
G. Eremeev - Cornell**

# Thermal Feedback

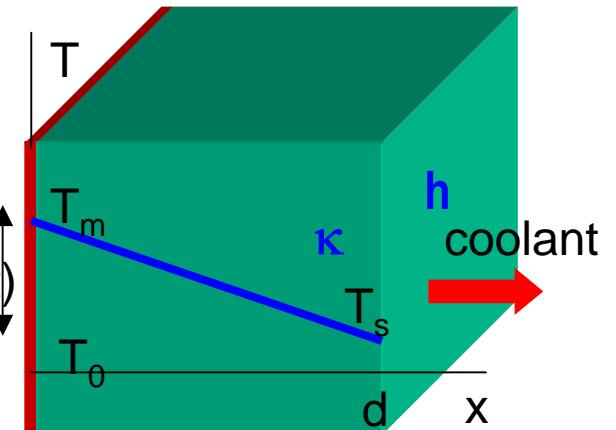
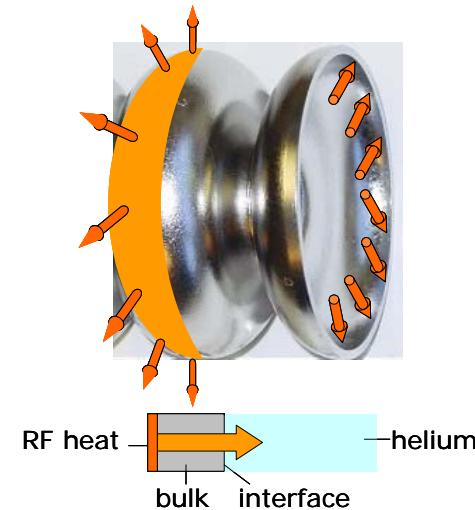
**Thermal feed-back: exponential T-dependence of BCS surface resistance:  $\rightarrow R_s \rightarrow P_{RF} \rightarrow \Delta T \rightarrow R_s \rightarrow \dots$**

$$P_{RF} = \frac{1}{2} R_s H_\omega^2$$

$$R_s = R_{s,res} + \frac{A(\omega)}{T} e^{-\frac{\Delta}{k_B T}} \left[ 1 + C \left( \frac{H_\omega}{H_c} \right)^2 \right] + \dots + \dots$$

$$h_{Kap}(T_s, T_0) d(T_s - T_0) = \int_{T_s}^{T_m} \kappa(T') dT' \quad \left( \frac{W}{m} \right)$$

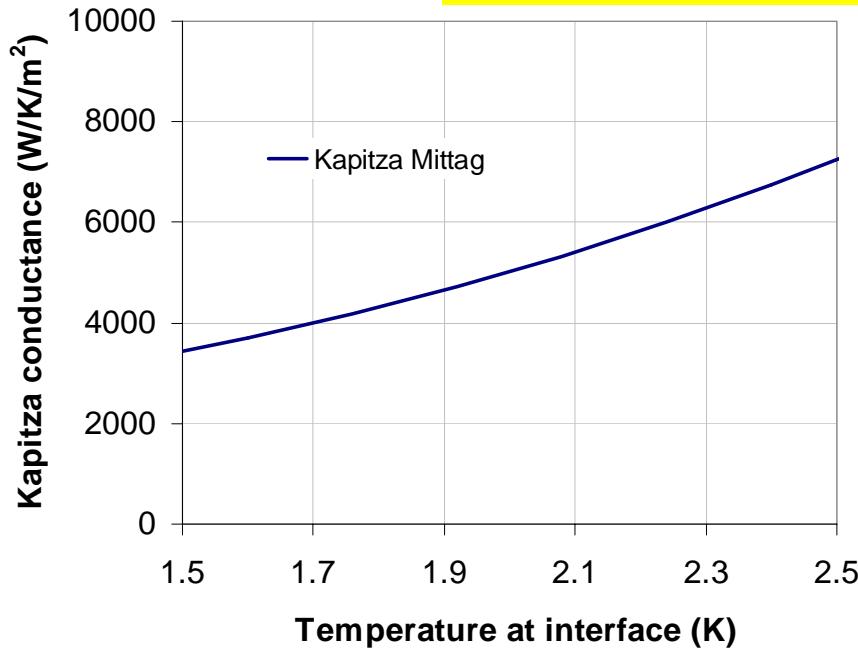
$$\frac{1}{2} R_s(T_m, H_c, \dots) H_{RF}^2 = h_{Kap}(T_s, T_0)(T_s - T_0) \quad \left( \frac{W}{m^2} \right) H(t)$$



# Material Properties

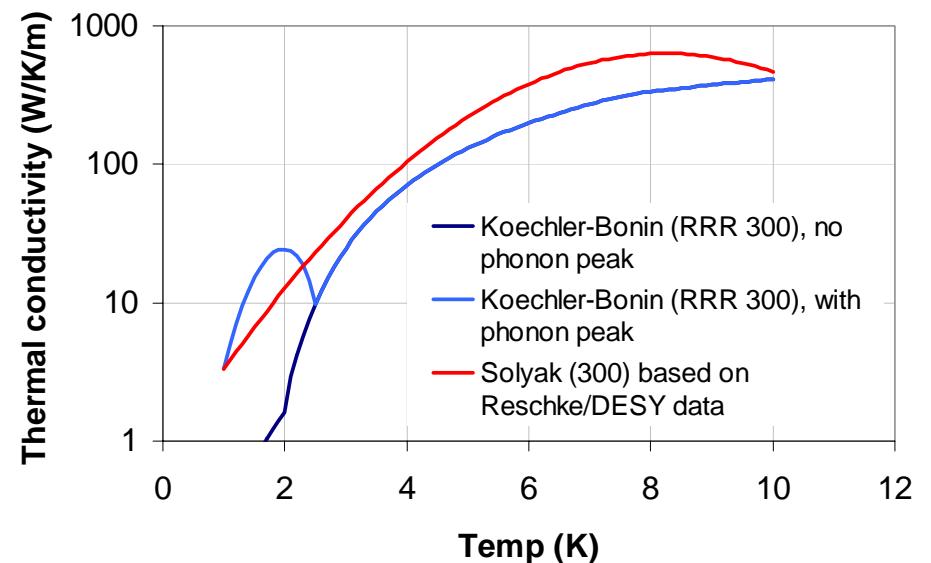
$$a_{Kap}(T) = 200 \cdot (T_0^{4.65}) \left[ 1 + 1.5 \left( \frac{T - T_0}{T_0} \right) + \left( \frac{T - T_0}{T_0} \right)^2 + 0.25 \left( \frac{T - T_0}{T_0} \right)^3 \right] \left( \frac{W}{Km^2} \right)$$

$$\kappa(T) = 0.7 e^{(1.65T - 0.1T^2)} \quad \left( \frac{W}{K \cdot m} \right)$$



Mittag

7/10/2005



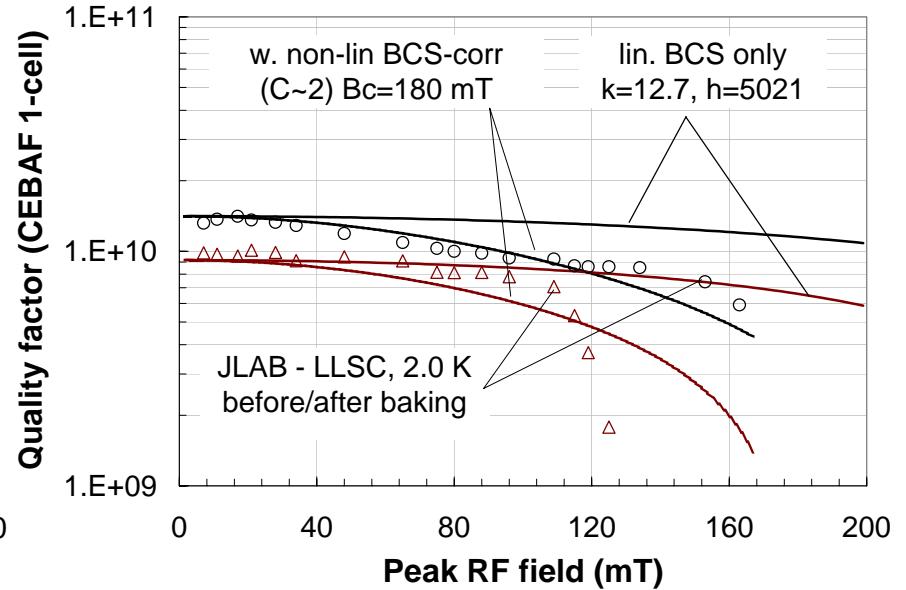
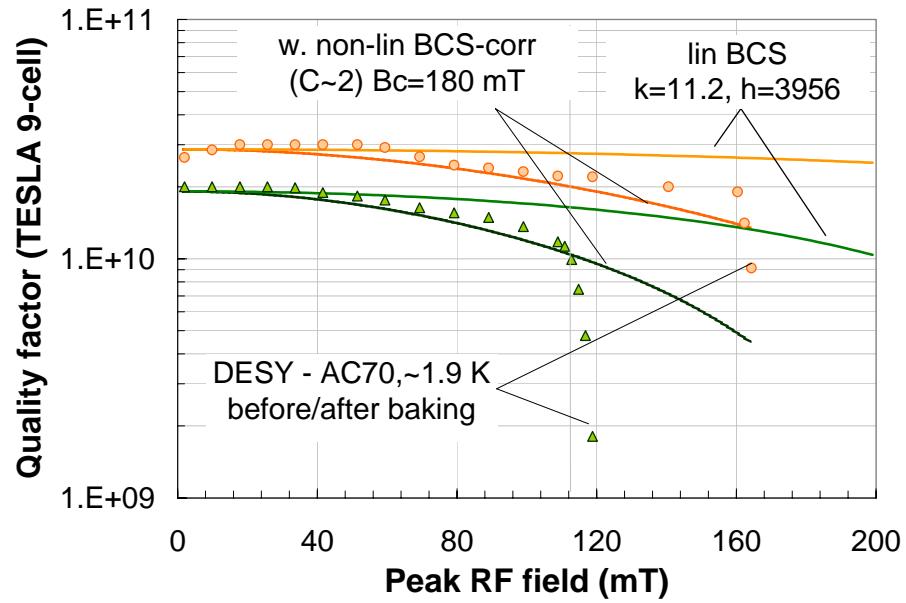
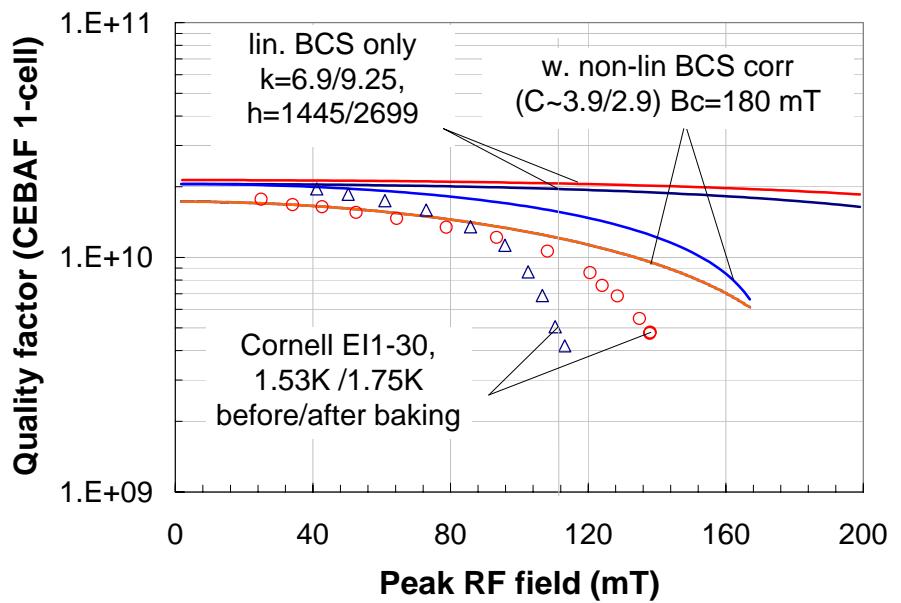
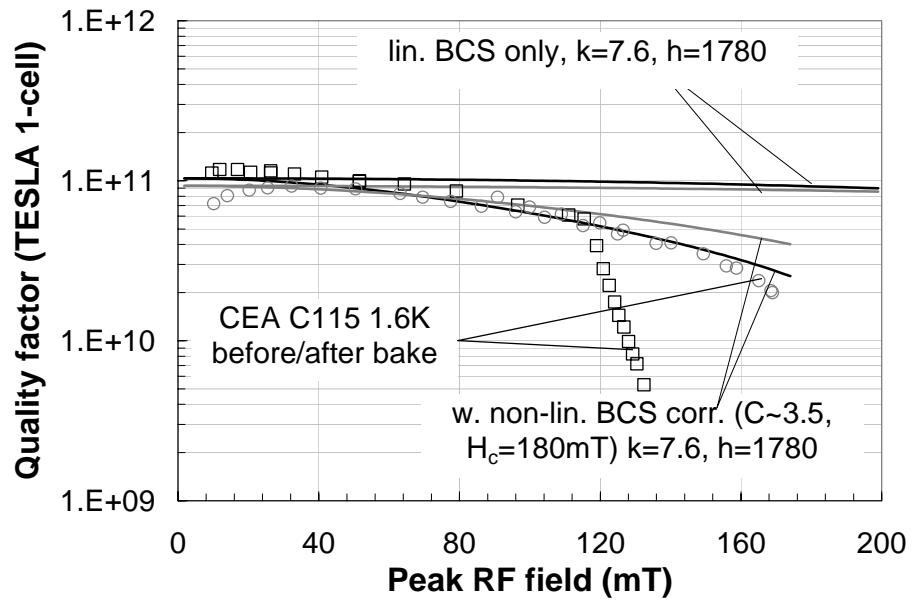
Koechler - Bonin

Pbauer – SRF05 – Q-Slope Session

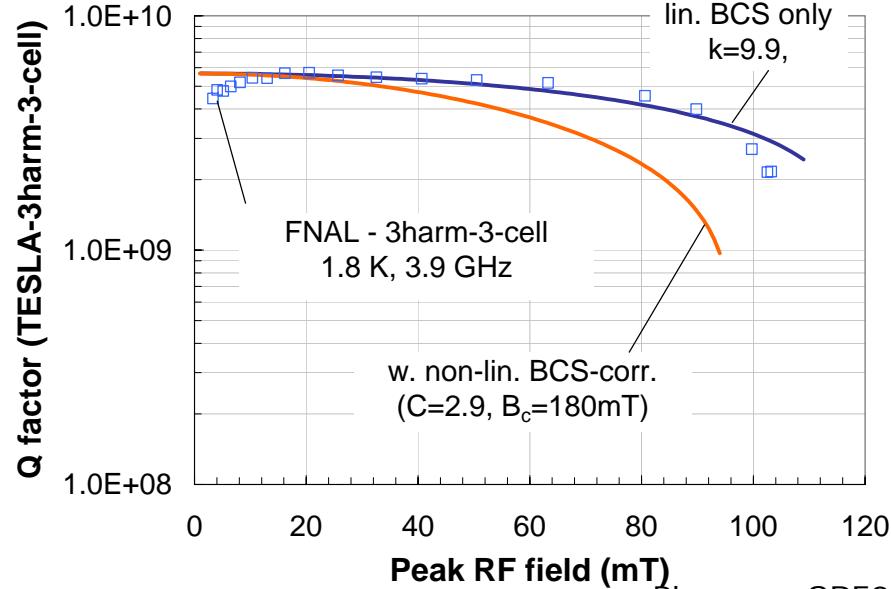
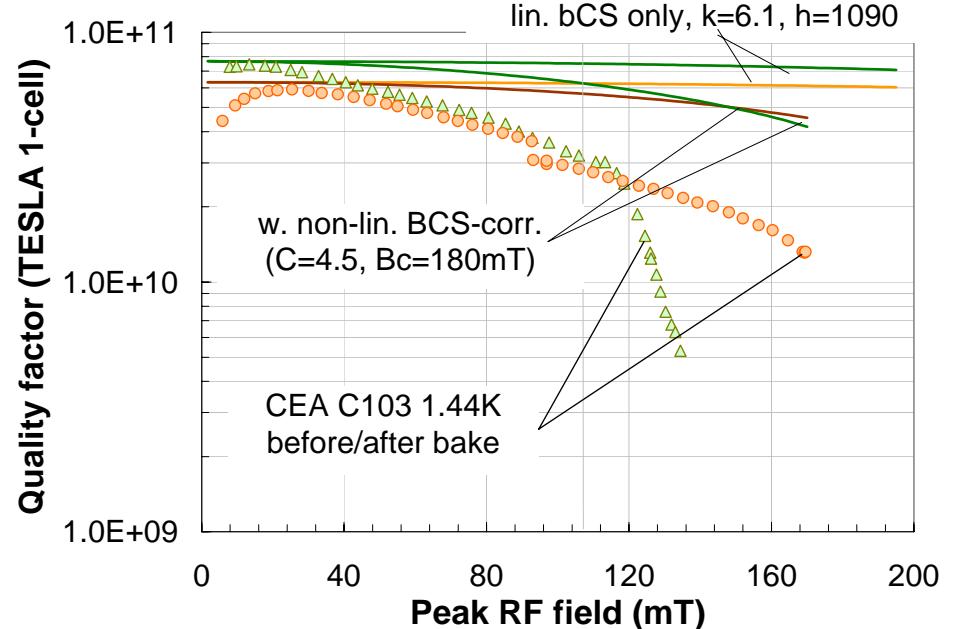
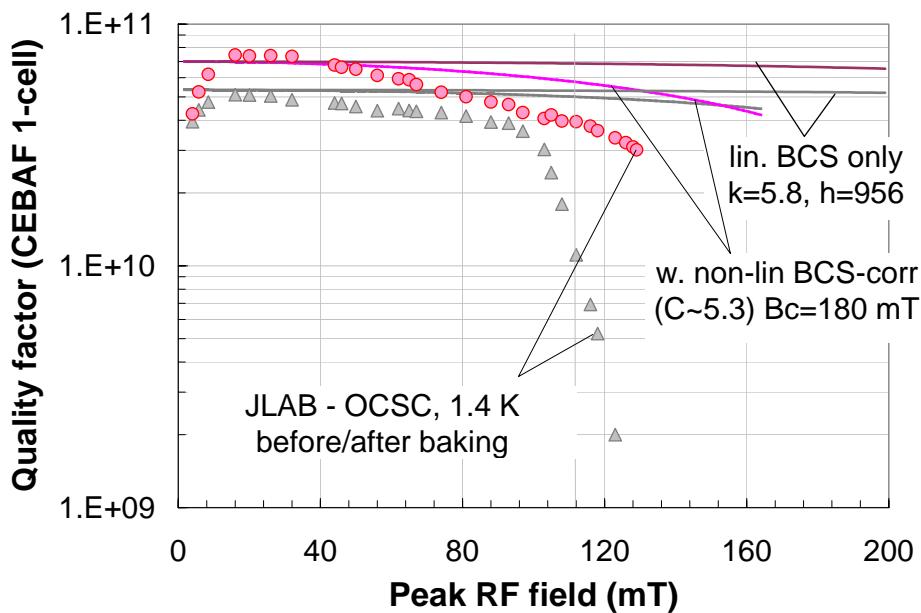
# SUMMARY - TABLE

	C-103 CEA	C-115 CEA	D-AC70 DESY	F-3C-1 FNAL	J-LLSC JLAB	J-OCSC JLAB	CU-EI1-30 CORNELL
T <sub>0</sub> (K)	1.44	1.6	2 (1.9)	1.8	2.0	1.4	1.53 (1.75)
G ( $\Omega$ )	283	283	270	291	282	273	255
d (mm)	2.6	2.6	2.6	2.6	2.6	2.6	2.75
$\kappa(T_0)$ (W/K/m)	6.1	7.6	11.22	9.9	12.7	5.8	6.9 (9.3)
$h_{\text{Kap}}(T_0)$ (W/K/m <sup>2</sup> )	1090	1780	3956	3080	5021	956	1445 (2699)
R <sub>res</sub> (n $\Omega$ )	3.2 (4.2)	1 (2)	-10 (5.2)	10	17 (9.4)	3.6 (5)	11 (11)
R <sub>bcs,lin</sub> (T <sub>0</sub> ) (n $\Omega$ )	0.5 (0.3)	1.7 (1.05)	24 (4.3)	40	31 (20)	3.9 (5.1)	5.6 (1)
$\Delta/k_B T_c$	2 (2.05)	1.97 (1.93)	1.53 (1.94)	1.92	2.1 (1.94)	2.09 (2.15)	1.99 (1.99)
A( $\omega$ ) (10 <sup>-5</sup> $\Omega$ )	2.76(2.13)	2.5 (1.2)	0.597(1.058)	14.8	4.4 (1.7)	4.46 (2.38)	3.7 (2.5)
T <sub>c</sub> (K) *	9.2	9.2	9.2	9.2	9.2	9.2	9.2
$\omega/2\pi$ (GHz)	1.3	1.3	1.3	3.9	1.5	1.5	1.5
C (T <sub>0</sub> , $\omega$ )	4.5 (4.5)	3.6 (3.4)	1.5 (2.5)	2.9	2.6 (2.2)	5.2 (5.5)	3.9 (2.9)
$\mu_0 H_c$ (mT) *	180	180	180	180	180	180	180

# Comparison Model-Data: GRAPHS I



## Comparison Model-Data: GRAPHS II



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$$C(T, \omega) = \frac{\pi^2}{384} \left[ 1 + \frac{\ln(9)}{3 \ln \left( 4.1 \frac{k_B T \Delta}{(\hbar \omega)^2} \left( \frac{\xi}{\lambda} \right)^2 \right)} \right] \left( \frac{\Delta}{k_B T} \right)^2$$

**C increases with lower T and higher f!**

## SUMMARY

### Assuming

- A standardized set of thermal material parameters;
  - Measured low field residual and lin BCS surface resistance contribution;
  - TFBM in a homogeneous material;
- 
- Non-lin BCS surface resistance contribution as recently presented by A. Gurevich can explain medium field Q-Slope;
  - C is not large enough at lower temps (1.4 K) and too large at higher frequency ( $f > 2$  GHz);
  - Non lin BCS also cannot explain ultimate field Q-drop;

# Surface Resistance Review

- **BCS surface resistance**
  - Basic BCS
  - Corrections to BCS due to  $H_{\text{crit}}$
  - Interface tunnel exchange
- **Residual resistance**
  - Dielectric loss in oxide layer
  - Trapped flux (AF)
  - Localized states
- **Grain-boundary contribution**
  - Field-enhancement at the grain edges
  - Hysteresis loss due to JF in GBs
- ??????????????????
- ???

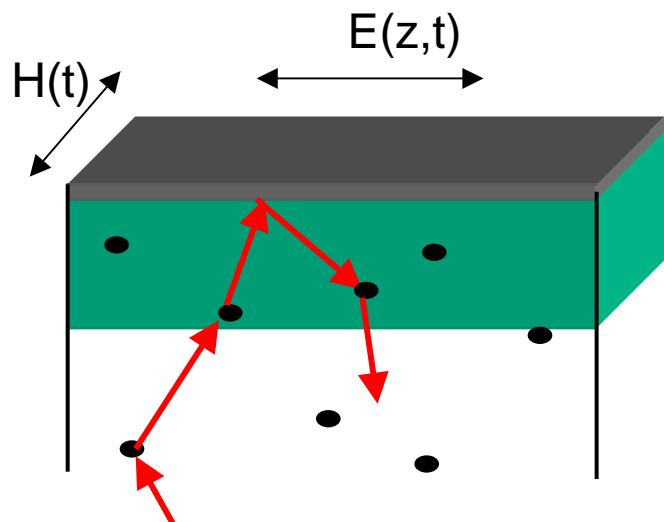
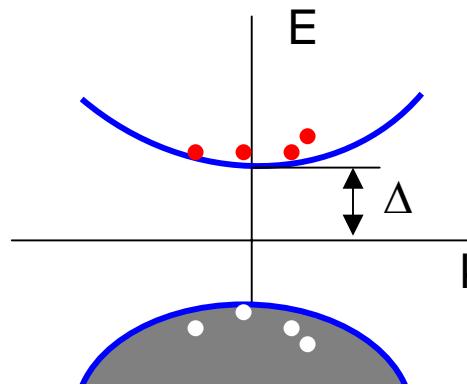
$$R_s \approx \frac{1}{2} \omega^2 \mu_0^2 \lambda_L^2 \sigma_n$$

# Surface Resistance

$$R_{s,RF} = R_{s,BCS}(T_m, H_{DC}, H_{RF}) + R_{res}(\omega, T, \dots) + R_{s,FE}(H_{RF}, \beta) + R_{s,Btrap}(H_0) + \dots \quad (\Omega)$$

- **BCS surface resistance**
  - Basic BCS
  - Corrections to BCS due to  $H_{crit}$  ➤ !
  - Interface tunnel exchange
- **Residual resistance**
  - Dielectric loss in oxide layer
  - Trapped flux (AF)
  - Localized states
- **Grain-boundary contribution**
  - Field-enhancement at the grain edges
  - Hysteresis loss due to JF in GBs

# BCS Surface Resistance



A. Gurevich

- Thermal activation of normal electrons

$$n_a = n_0 (\pi k_B T / 2\Delta)^{1/2} \exp(-\Delta/k_B T)$$

- Accelerating electric field

$$E(z,t) = \mu_0 \omega \lambda H_\omega e^{-\lambda|z|} \sin \omega t$$

- Scattering mechanisms and normal state conductivity:  $\sigma_n = e^2 n_0 \ell / p_F$ ,  $p_F = \hbar (3\pi^2 n_0)^{1/3}$

- Normal skin effect ( $\ell \ll \lambda$ ): multiple impurity scattering in the  $\lambda$ -belt:

$$R_s \sim (\mu_0^2 \omega^2 \lambda^3 \sigma_n \Delta / (k_B T)) \exp(-\Delta/k_B T)$$

- Anomalous skin effect ( $\ell \gg \lambda$ ): scattering by the gradient of the ac field  $E(z)$ :

$$\text{Effective } \sigma_{\text{eff}} \sim e^2 n_0 \lambda / p_F; \quad \ell \rightarrow \lambda$$

# Linear BCS Surface Resistance for $H_\omega \ll H_c$

- Solution of the kinetic equation for type-II superconductor for the clean limit and diffusive surface scattering at  $\omega^2 \ll \Delta T$ :

$$R_s = \frac{3\mu_0^2 \lambda^3 \Delta}{2k_B T} \sigma_{eff} \omega^2 e^{-\Delta/(k_B T)} \left[ \ln \frac{1.2 k_B T \Delta \xi^2}{\hbar^2 \omega^2 \lambda^2} \right]$$

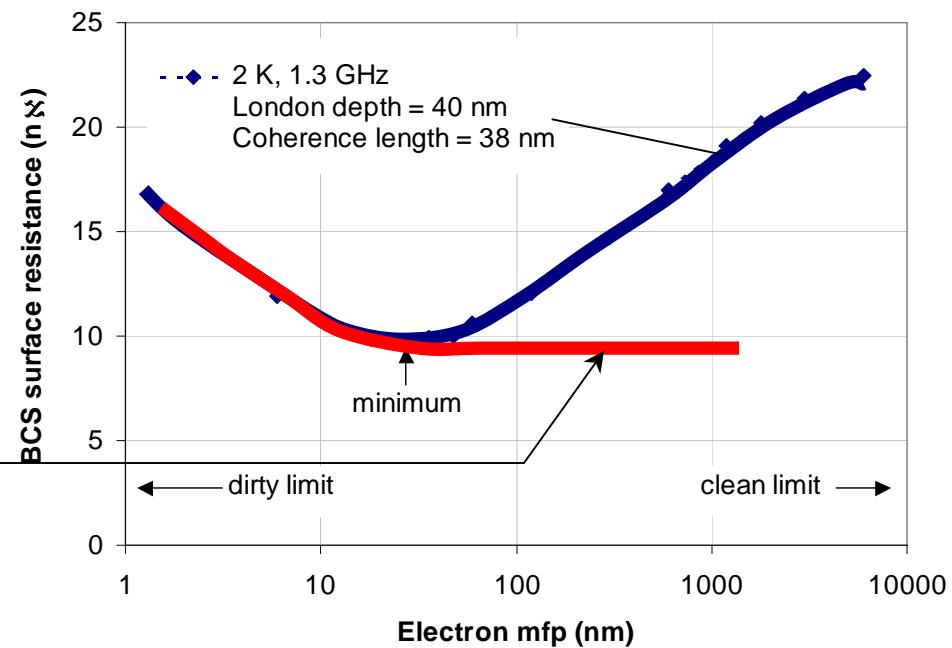
$$\Delta/(k_B T_c) \sim 2, T_c \sim 9.2 \text{ K}, \xi \sim \lambda \sim 40 \text{ nm}$$

$$n_0 \sim 6 \cdot 10^{28} \text{ m}^{-3}, v_F \sim 1.3 \cdot 10^6 \text{ m/s}$$

- Effective conductivity in the non-local clean limit:

$$\sigma_{eff} = \frac{n_0 e^2 \lambda}{p_F}$$

No dependence of  $R_s$  on the normal resistivity and impurity scattering



# Nonlinear BCS Surface Resistance

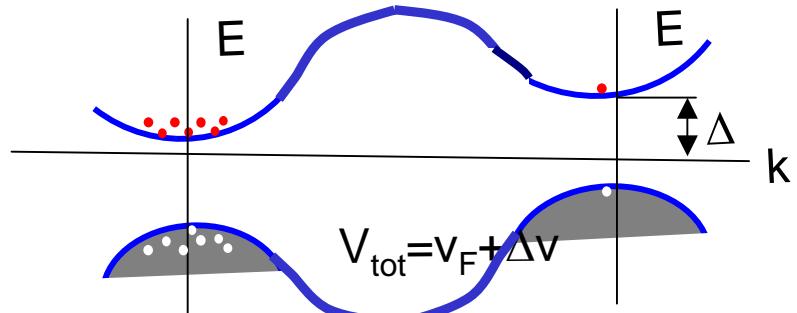
- RF dissipation was calculated for clean limit ( $\ell > \lambda$ ) from kinetic equations for a superconductor in a strong rf field superimposed on a dc field;

$$H(t) = H_\omega \cos\omega t + H_0$$

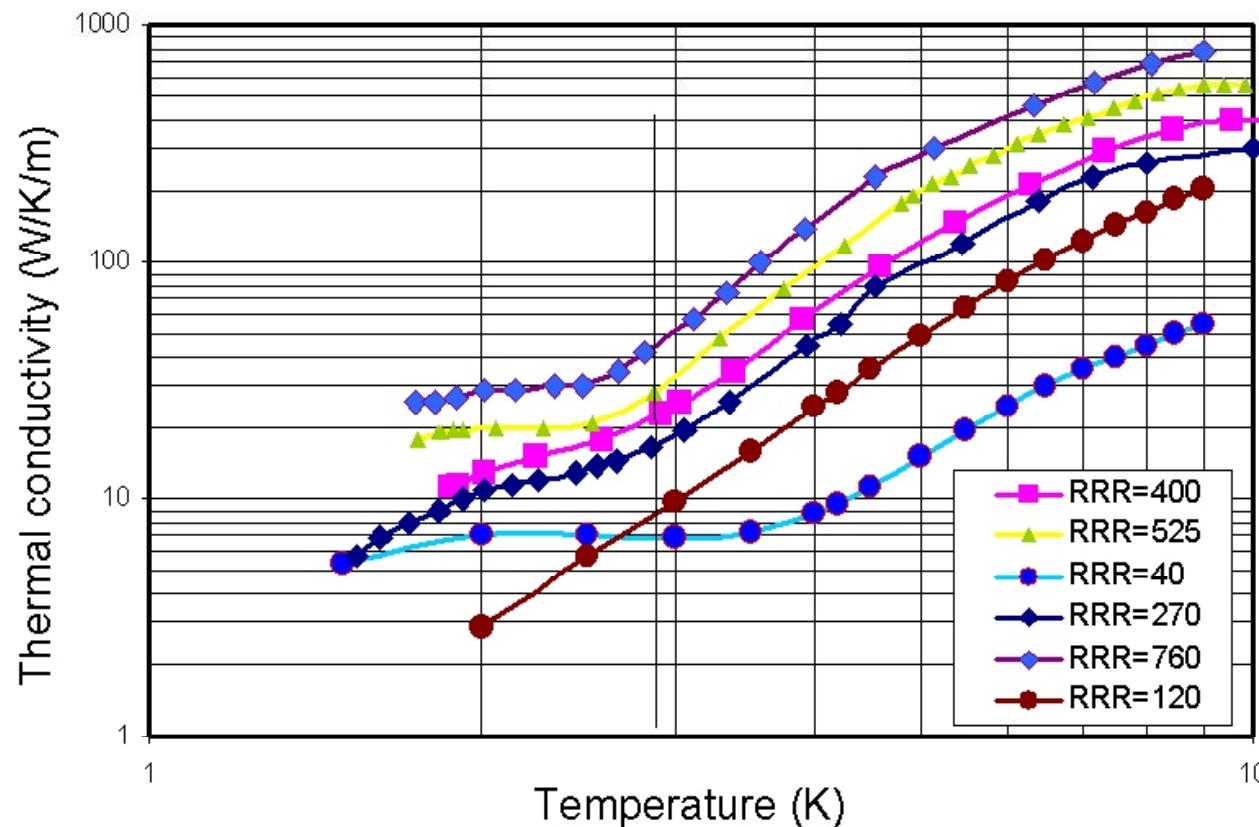
$$R_{s,BCS}(T, H_{RF}) = R_{s,BCS}(T, H_{RF} = 0) \left[ 1 + C(T, \omega) \left( \frac{H_{RF}}{H_c} \right)^2 + \dots \right]$$

$$C(T, \omega) = \frac{\pi^2}{384} \left[ 1 + \frac{\ln(9)}{3 \ln \left( 4.1 \frac{k_B T \Delta}{(\hbar \omega)^2} \left( \frac{\xi}{\lambda} \right)^2 \right)} \right] \left( \frac{\Delta}{k_B T} \right)^2$$

- Nonlinear correction due to rf pair-breaking increases as the temperature decreases, At low T, the non-linearity becomes important even for comparatively weak rf amplitudes
- RF power P depends quadratically on the RF magnetic field;
- Higher order terms  $\sim H_\omega^4$  also appear at  $H_\omega \sim H_c$ ;
- Contribution due to the DC magnetic field  $H_0$  is usually counted as “residual”;



# Material Properties



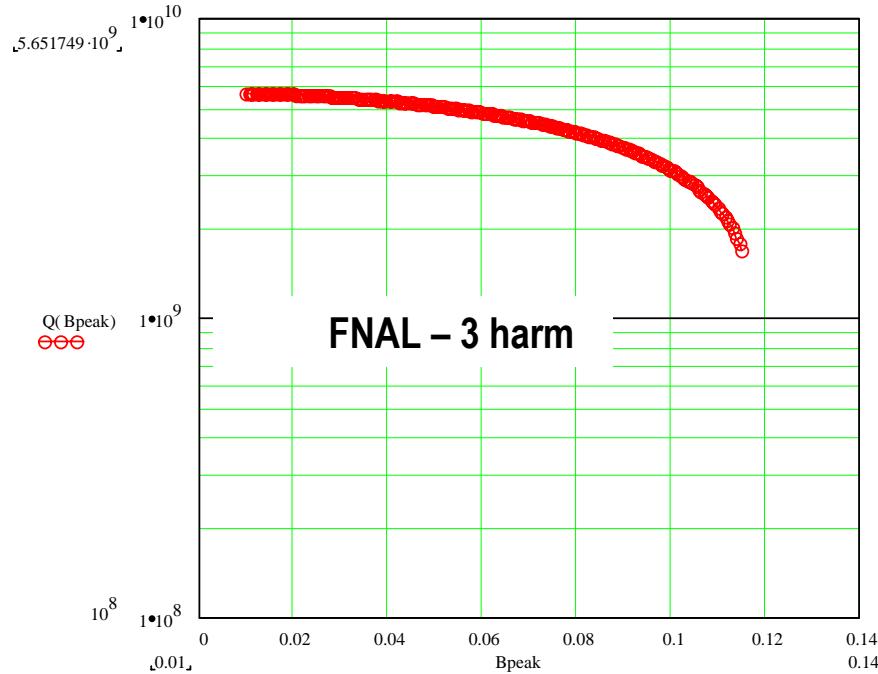
Courtesy of D. Retschke / DESY

# Breakdown RF Field – Linear BCS only

$$H_{RF}^2 = \frac{2(T_m - T_0)T_m}{A(\omega)T_c} e^{\frac{\alpha T_c}{T_m}} \left( \frac{\kappa h_{Kap}}{dh_{Kap} + \kappa} \right) \left( \frac{A^2}{m^2} \right)$$

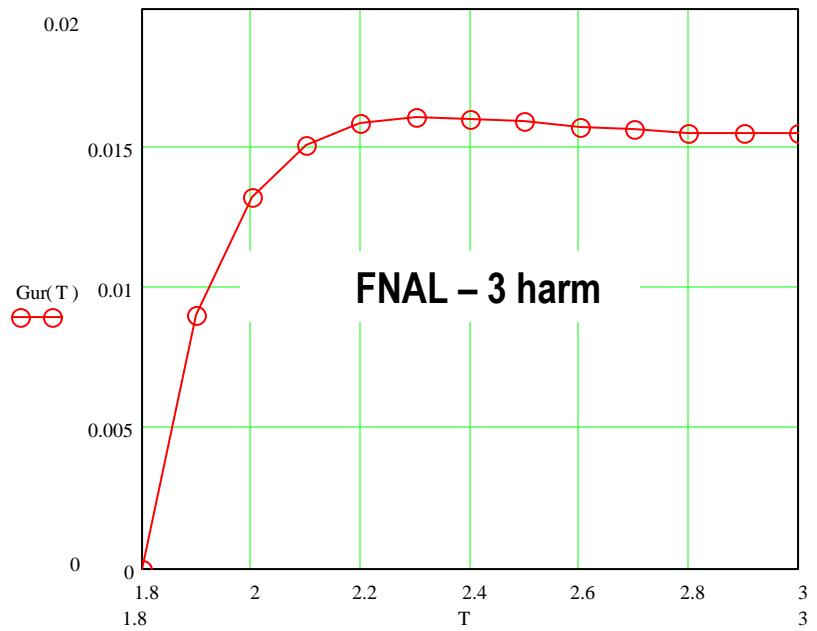
Thermal runaway occurs at a rather weak overheating. Thermal break-down field depends on  $T_0$  and  $\kappa, hd$ .

$$T_{max} \sim T_0 + T_0^2 / (\alpha T c)$$



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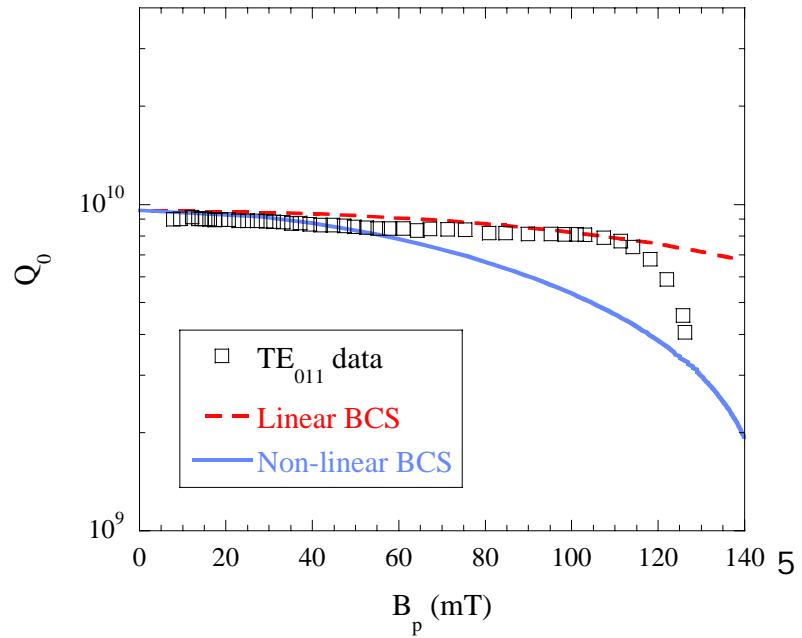
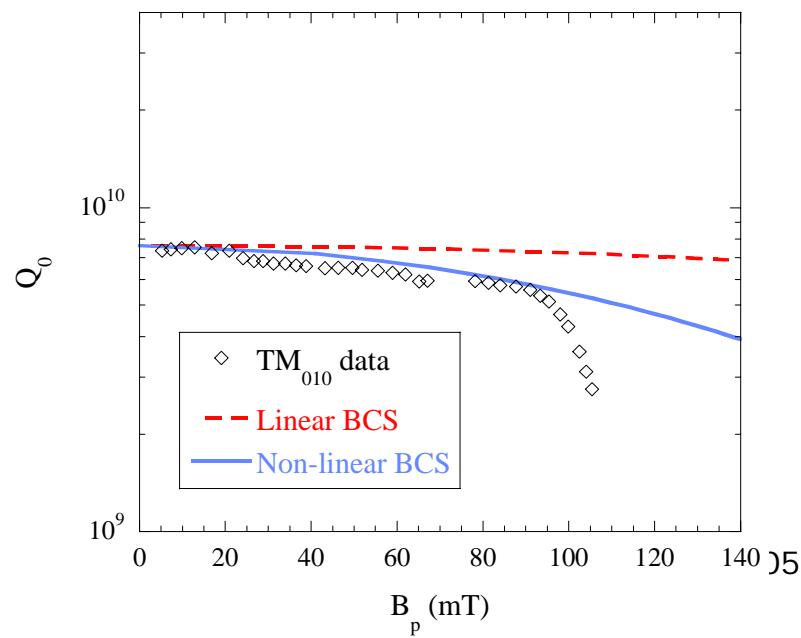
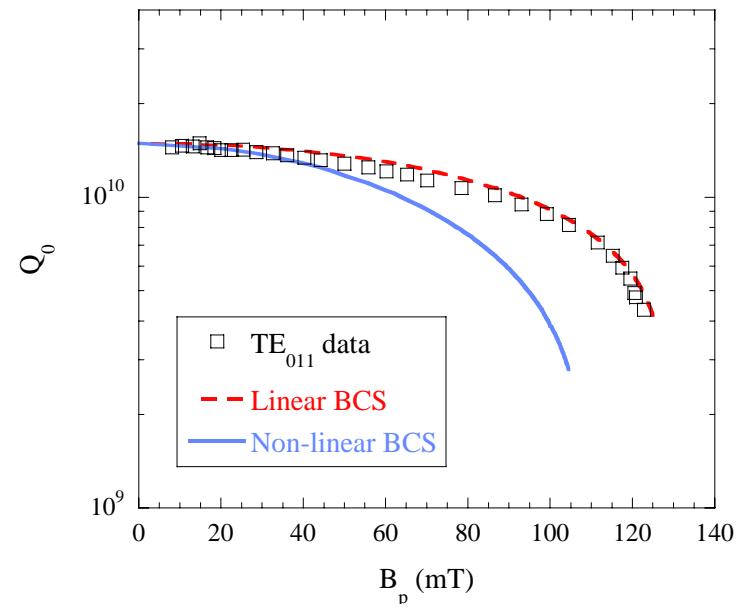
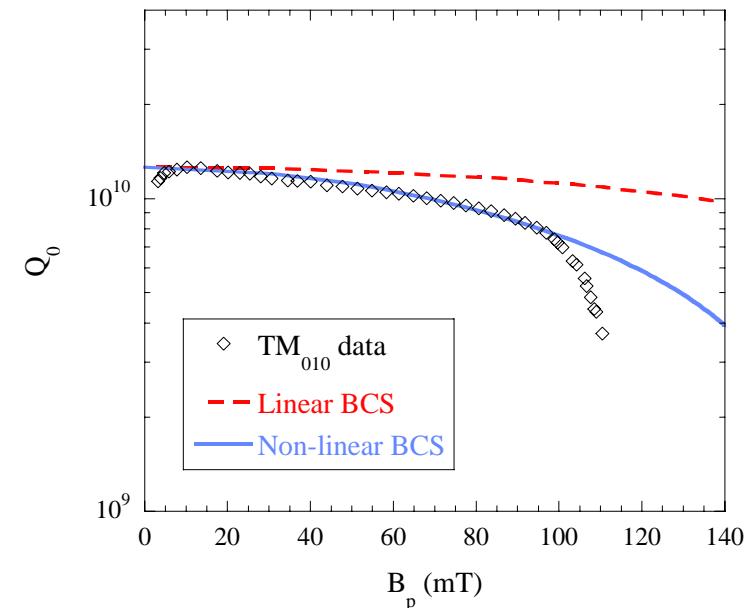


Inserting  $\Delta T \sim T_0^2 / \Delta$  gives an expression for the Q drop at the thermal quench:

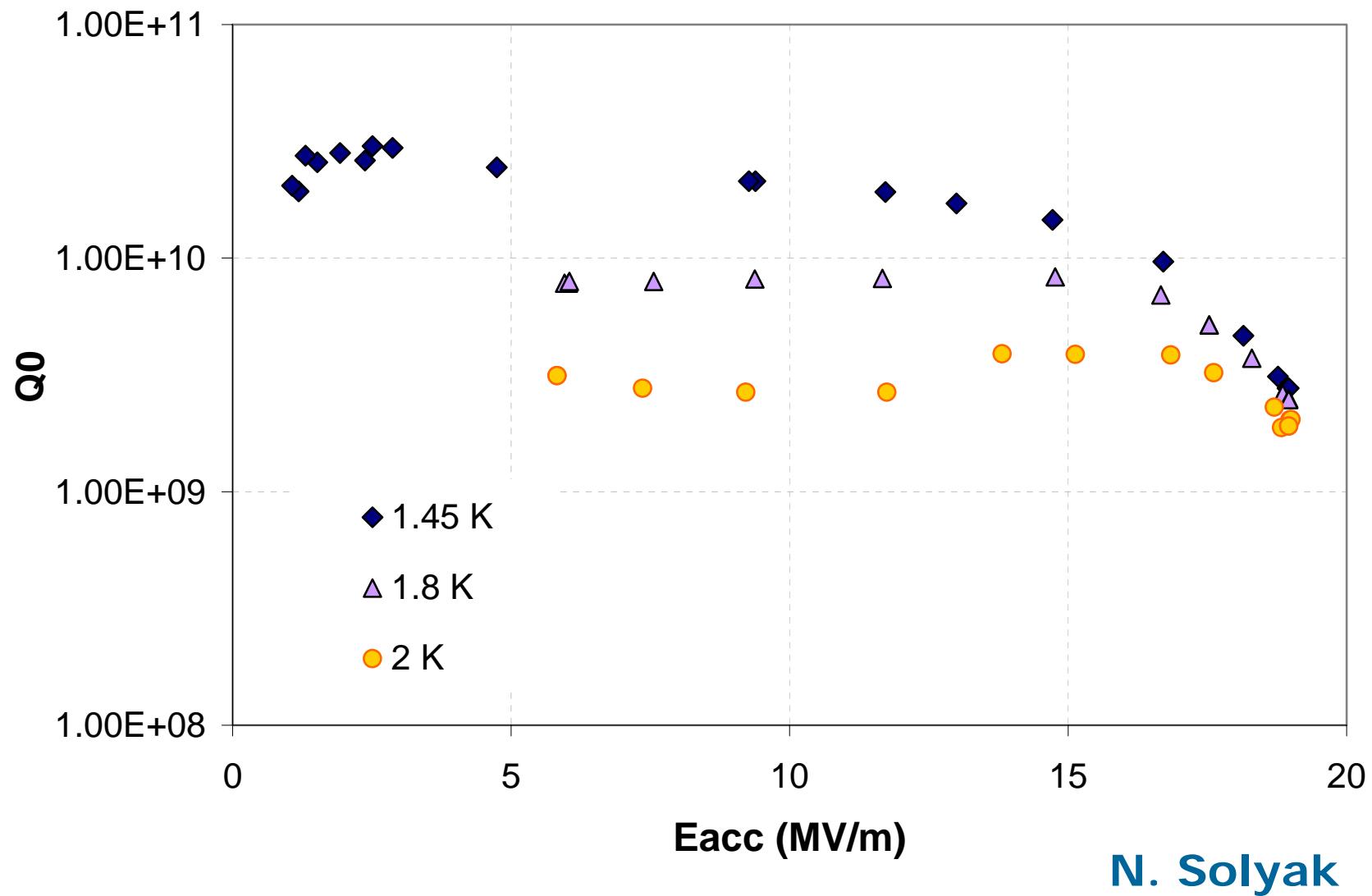
$$Q(H_b) \approx Q(0)/e$$

A. Gurevich

## G. Ciovati CEBAF 1cell in TM (1.47) and TE (2.82 GHz)



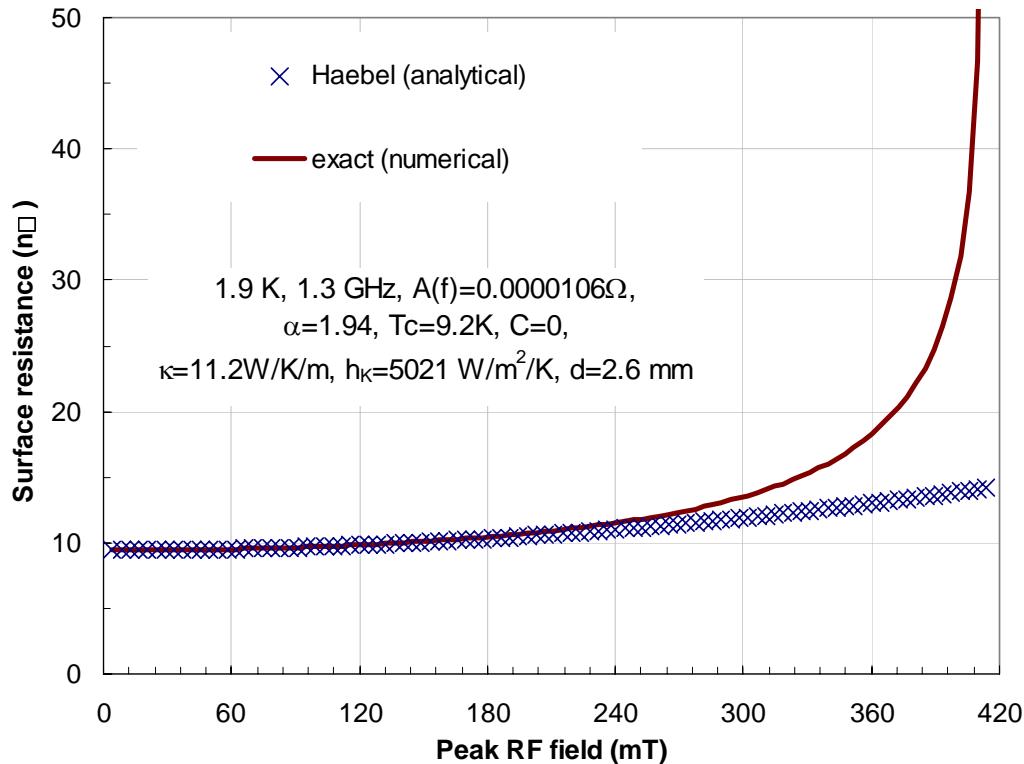
### 3rd harmonic 3-cell Fermilab March 2005



# Analytical “Haebel” Model

$$R_s(T) \approx R_s(T_0) + \frac{\partial R_s}{\partial T} \Big|_{T_0} \Delta T \quad (\Omega) \quad \frac{\partial \mathbf{R}_s}{\partial \mathbf{T}} \Big|_{T_0} = (\mathbf{R}_s(T_0) - \mathbf{R}_{s0}) \left( \frac{\alpha T_c}{T_0^2} - \frac{1}{T_0} \right)$$

$$\mathbf{R}_s(H_{RF}) \approx \mathbf{R}_s(T_0) \left[ 1 + \left( \frac{dh_{Kap}(T_0) + \kappa(T_0)}{2\kappa(T_0)h_{Kap}(T_0)} \right) \frac{\partial \mathbf{R}_s(\mathbf{T})}{\partial \mathbf{T}} \Big|_{T_0} H_{RF}^2 \right]$$



**First order Taylor expansion of  $R_s$  leads to analytical expression for  $R_s(H_{RF})$ ;**

**Not accurate close to quench!**