

# $\chi_{cJ}$ decays to light hadrons at CLEO

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CLEO Collaboration

and

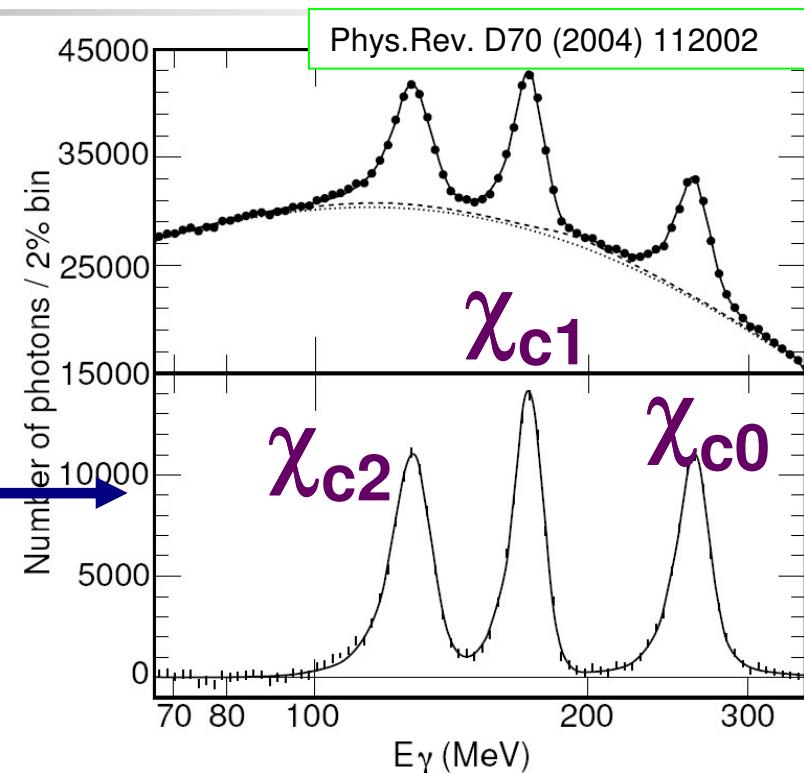
*Wayne State University*

June 28, 2006

Heavy Quarkonium 2006, BNL

# $\chi_{cJ}$ production at CLEO-c

- $e^+e^- \rightarrow \psi(2S)$ 
  - $5\text{pb}^{-1}$ , CLEO III & c, 3M  $\psi(2S)$
  - by the end of the year  $\times 10$
- $\psi(2S) \rightarrow \pi\pi J/\psi$ 
  - $\mathcal{B} \sim 50\%$
- $\psi(2S) \rightarrow \gamma \chi_{cJ}$ ,  $J=0,1,2$ 
  - $\mathcal{B}_J \sim 9\%$ , “ $\chi_{cJ}$  factory”
  - observed in inclusive analysis
  - $\mathcal{B}(\chi_{cJ} \rightarrow \text{hadrons})$  are not well known



- We find copious  $\chi_{cJ}$  hadronic decays in exclusive modes
  - $\chi_{cJ} \rightarrow 2\text{-body}$
  - $\chi_{cJ} \rightarrow 3\text{-body}$ , Dalitz analysis
  - $\chi_{cJ} \rightarrow 4$  and multi-body decays

# Outline

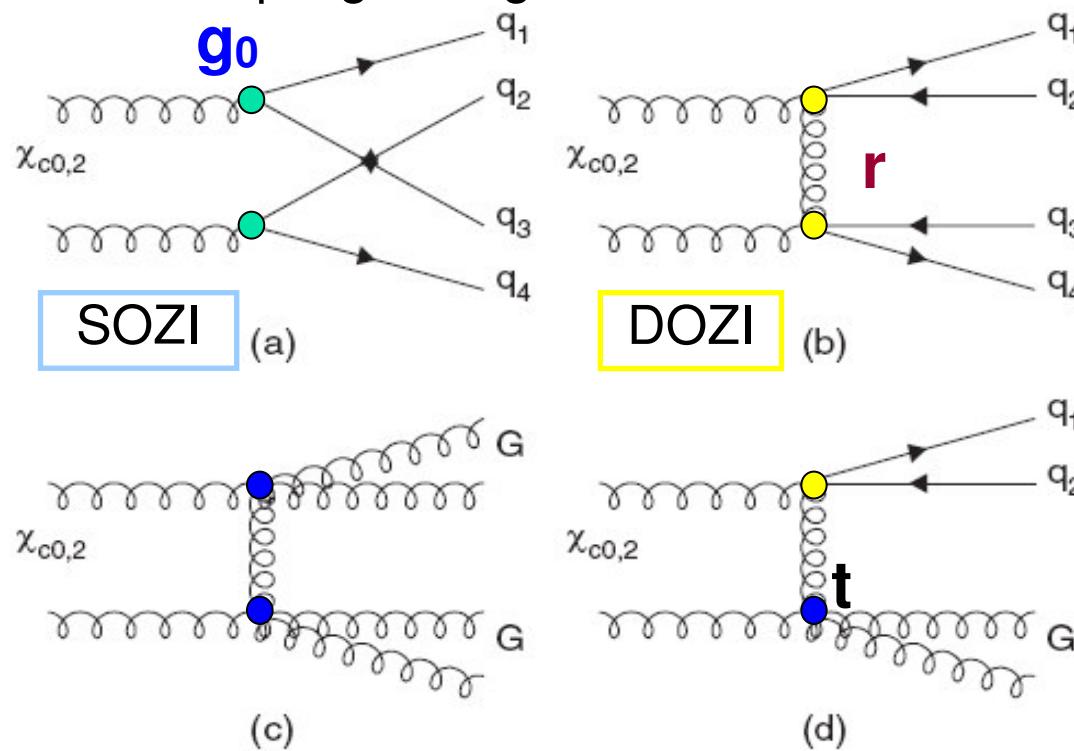
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- Selected analyses of  $\chi_{cJ}$  hadronic decays:
  - $\chi_{cJ} \rightarrow \eta^{(')}\eta^{(')}$
  - $\chi_{cJ} \rightarrow VV \quad (V = \varphi, \omega)$
  - $\chi_{cJ} \rightarrow h^+h^-h^0h^0 \quad (h = \pi, K, \eta, p)$
  - $\chi_{cJ} \rightarrow h^+h^-h^0$ , 3-body decays, Dalitz plot analysis

# Motivation $\chi_{c0,2} \rightarrow VV, PP, SS$

- Qiang Zhao, Phys. Rev., D72:074001, 2005:

- $g_0$ : basic  $gqq^*$  coupling
- $r$ : OZI-rule violation
- $R$ : SU(3) flavour breaking
- $t$ : glueball coupling strength



# Reconstruction of $\psi(2S) \rightarrow \gamma \chi_{cJ}$ , $\chi_{cJ} \rightarrow h^0 h^+ h^-$

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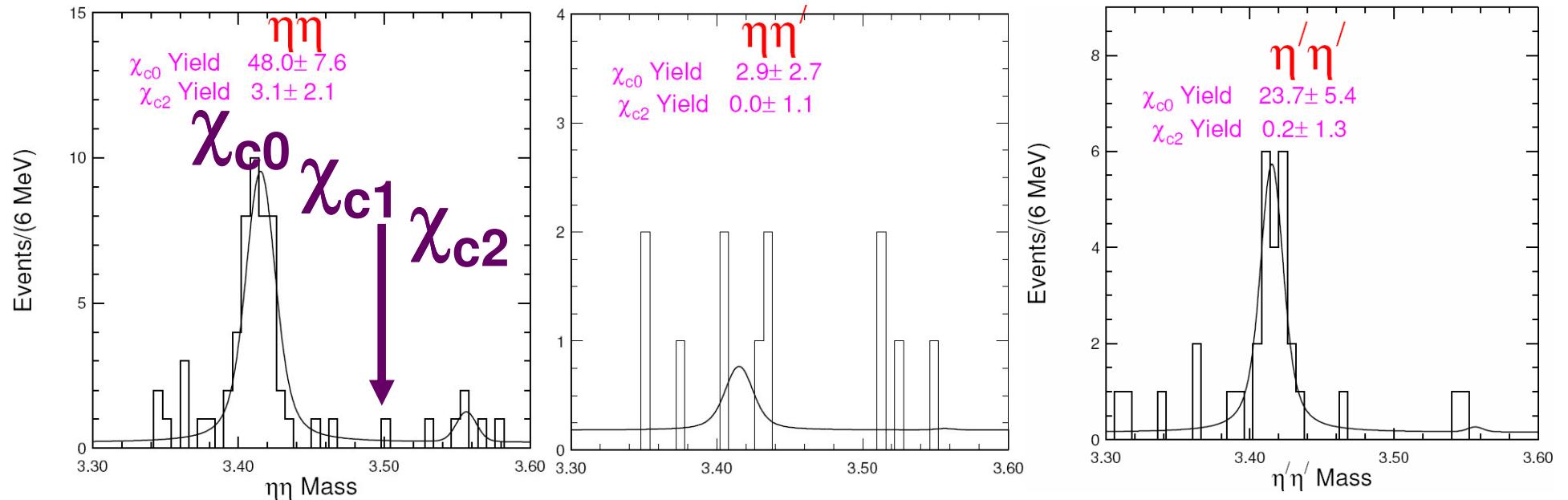
- Use particle ID ( $dE/dx$  & RICH) for  $\pi$ ,  $K$ ,  $p$
- $K_S^0 / \Lambda$ : flight path  $> 5 / 3$  mm,  $|\Delta m| < 10 / 5$  MeV/c $^2$
- $\gamma$ : 30 MeV in good barrel, 50 MeV elsewhere,  
no track match, good shower shape
- $\pi^0 \rightarrow \gamma\gamma$ , mass constrained fit  $\chi^2 < 10$
- $\eta \rightarrow \gamma\gamma$ ,  $\pi^+\pi^-\pi^0$ ,  $\pi^+\pi^-\gamma$ , meson mass constrained
- $\eta' \rightarrow \eta\pi^+\pi^-$ ,  $\gamma p$
- Reconstruct the two charged particles and vertex  
constrain them. Use this as a starting point for neutral
- Add a radiated photon and constrain total decay  $\psi(2S)$   
4-momentum (accounting for crossing angle) and cut at  $\chi^2 < 25$
- Plot the mass spectra of hadron combinations

# $\chi_{cJ} \rightarrow \eta^{(\prime)} \eta^{(\prime)}$

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- Measurement of  $\mathcal{BR}$  or set an UL
  - $\chi_{cJ} \rightarrow \eta\eta$
  - $\chi_{cJ} \rightarrow \eta\eta'$
  - $\chi_{cJ} \rightarrow \eta'\eta'$

# Invariant mass spectra $\chi_{cJ} \rightarrow \eta^{(')}\eta^{(')}$



- $\chi_{c1} \rightarrow \text{PP}$  spin-parity violated, not seen
- From signal MC:
  - Resolution  $\sigma = 4.7\text{-}8.3 \text{ MeV}/c^2$
  - Efficiency  $\sim 4\text{-}6\%$  (includes  $\mathcal{BR}$ )

# Preliminary results for $\chi_{cJ} \rightarrow \eta^{(')}\eta^{(')}$

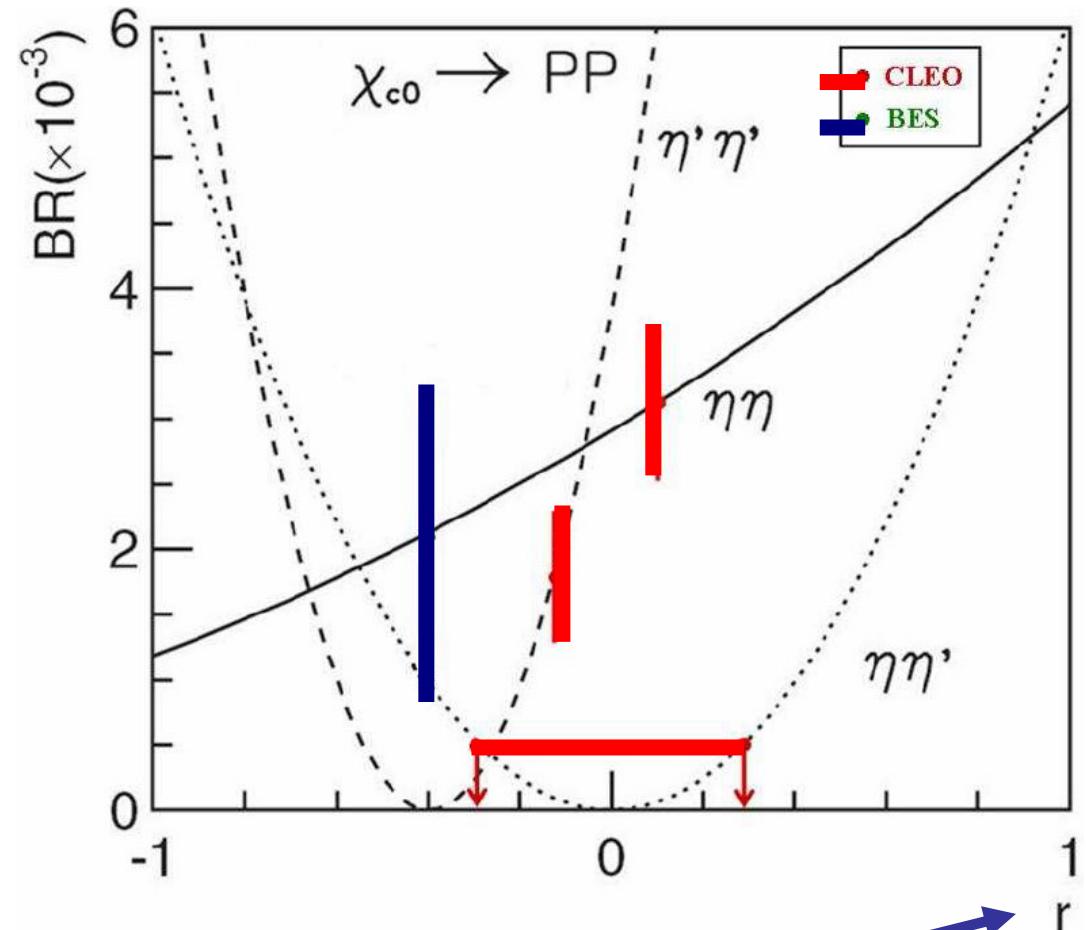
$\chi_{c0} \rightarrow \eta\eta$

E835:  $0.198 \pm 0.068 \pm 0.038 \%$

BES:  $0.194 \pm 0.084 \pm 0.059 \%$

$\chi_{c0} \rightarrow \eta^{(')}\eta^{(')}$

**CLEO preliminary**



Qiang Zhao, Phys. Rev. D72:074001, 2005

$r = A(\text{DOZI}) / A(\text{SOZI})$

# $\chi_{cJ} \rightarrow VV$

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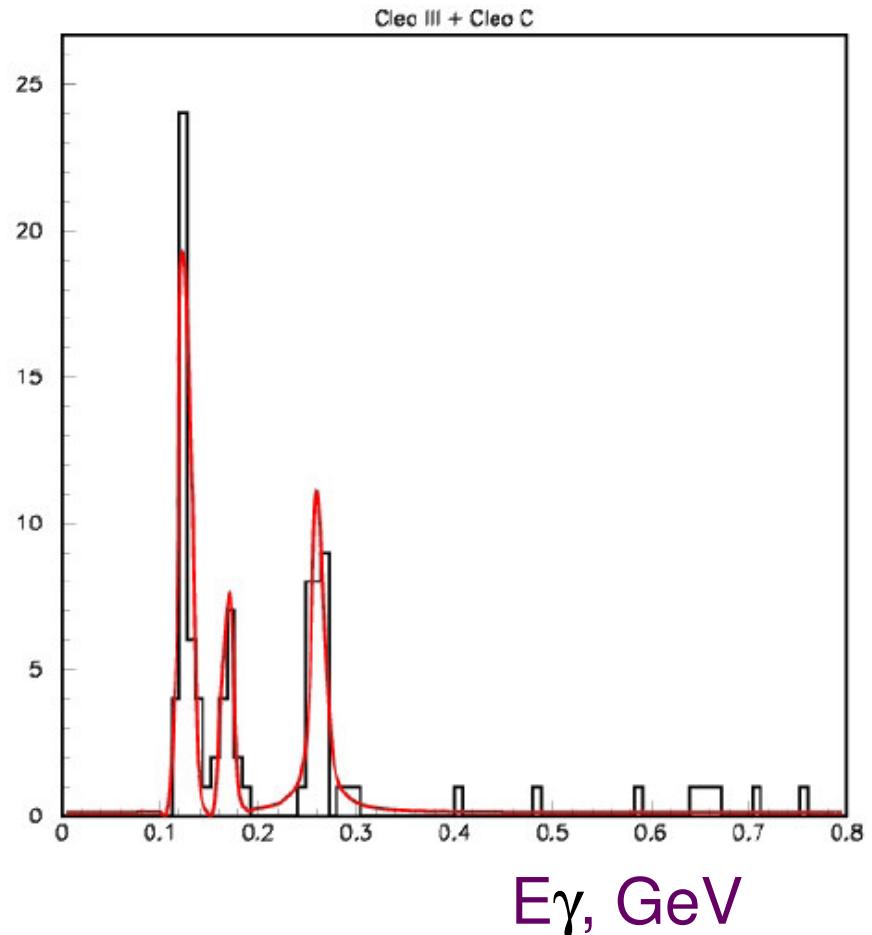
- Measurement of BR or set an UL on
  - $\chi_{cJ} \rightarrow \phi\phi$
  - $\chi_{cJ} \rightarrow \omega\omega$
  - $\chi_{cJ} \rightarrow VV$  other modes are not studied yet

# Observation of $\chi_{cJ} \rightarrow \phi\phi$

$\chi_{cJ} \rightarrow \phi\phi$

➤  $\phi \rightarrow K^+K^-$

- We observe:
  - Strong correlation in  $m(K^+K^-)$  vs  $m(K^+K^-)$
  - Signal for  $J=0,1,2$
- Analysis is in progress



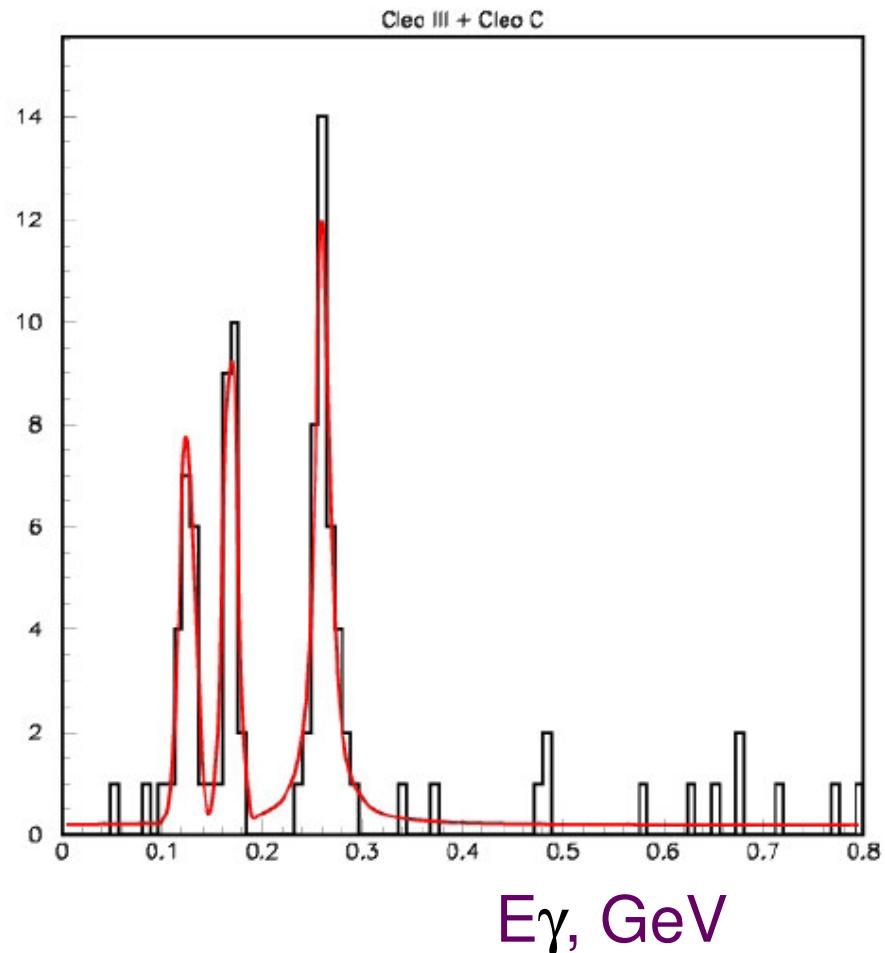
Quantity	$\chi_{c0} \rightarrow \phi\phi$	$\chi_{c1} \rightarrow \phi\phi$	$\chi_{c2} \rightarrow \phi\phi$
BES2: $\text{BR}(\chi_c \rightarrow \phi\phi) \times 10^{-3}$	$0.94 \pm 0.21 \pm 0.14$	—	$1.48 \pm 0.26 \pm 0.23$

# Observation of $\chi_{cJ} \rightarrow \omega\omega$

$\chi_{cJ} \rightarrow \omega\omega$

➤  $\omega \rightarrow \pi^+\pi^-\pi^0$

- We observe:
  - Strong correlation in  $m(\pi^+\pi^-\pi^0)$  vs  $m(\pi^+\pi^-\pi^0)$
  - Signal for  $J=0,1,2$
- Analysis is in progress



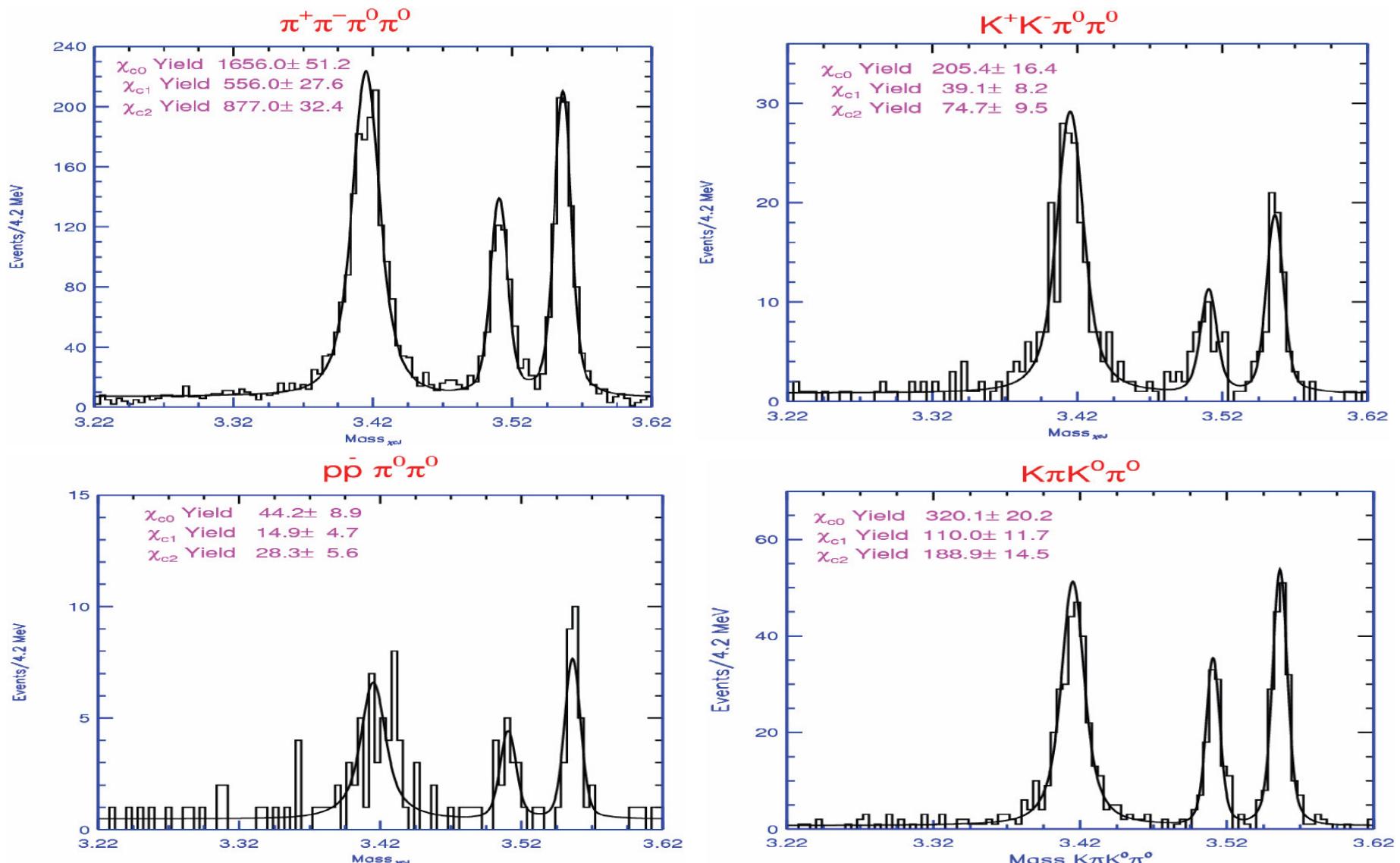
Quantity	$\chi_{c0} \rightarrow \phi\phi$	$\chi_{c1} \rightarrow \phi\phi$	$\chi_{c2} \rightarrow \phi\phi$
BES: $\text{BR}(\chi_c \rightarrow \omega\omega) \times 10^{-3}$	$2.29 \pm 0.58 \pm 0.41$	—	$1.77 \pm 0.47 \pm 0.36$

$$\chi_{cJ} \rightarrow h^+ h^- h^0 h^0$$

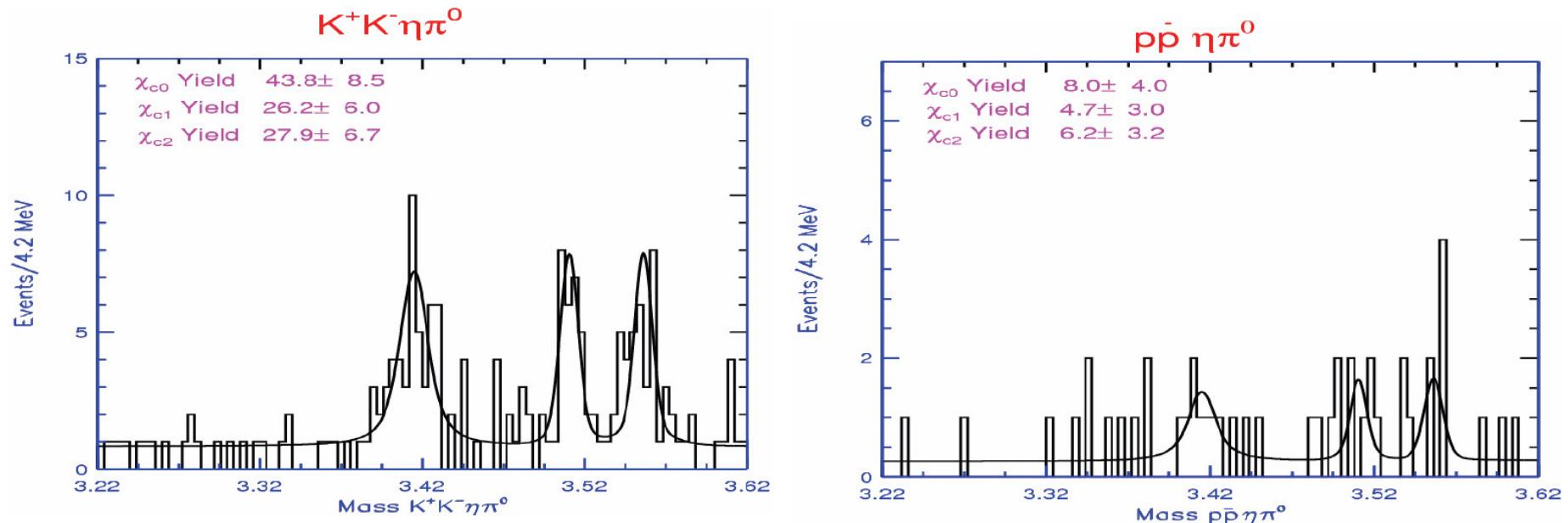
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- Measurement of BR or set UL on
  - $\chi_{cJ} \rightarrow h^+ h^- \pi^0 \pi^0$  ( $h = \pi, K, p$  - tracks)
  - $\chi_{cJ} \rightarrow h^+ h^- \eta \pi^0$
  - $\chi_{cJ} \rightarrow K \pi K^0 \pi^0$
- Motivation
  - modes with two neutral particles  $\pi^0$  and  $\eta$  have not been seen before

# $\chi_{cJ} \rightarrow h^+h^-\pi^0\pi^0, K\pi K^0\pi^0$



# $\chi_{cJ} \rightarrow h^+h^-\eta\pi^0$



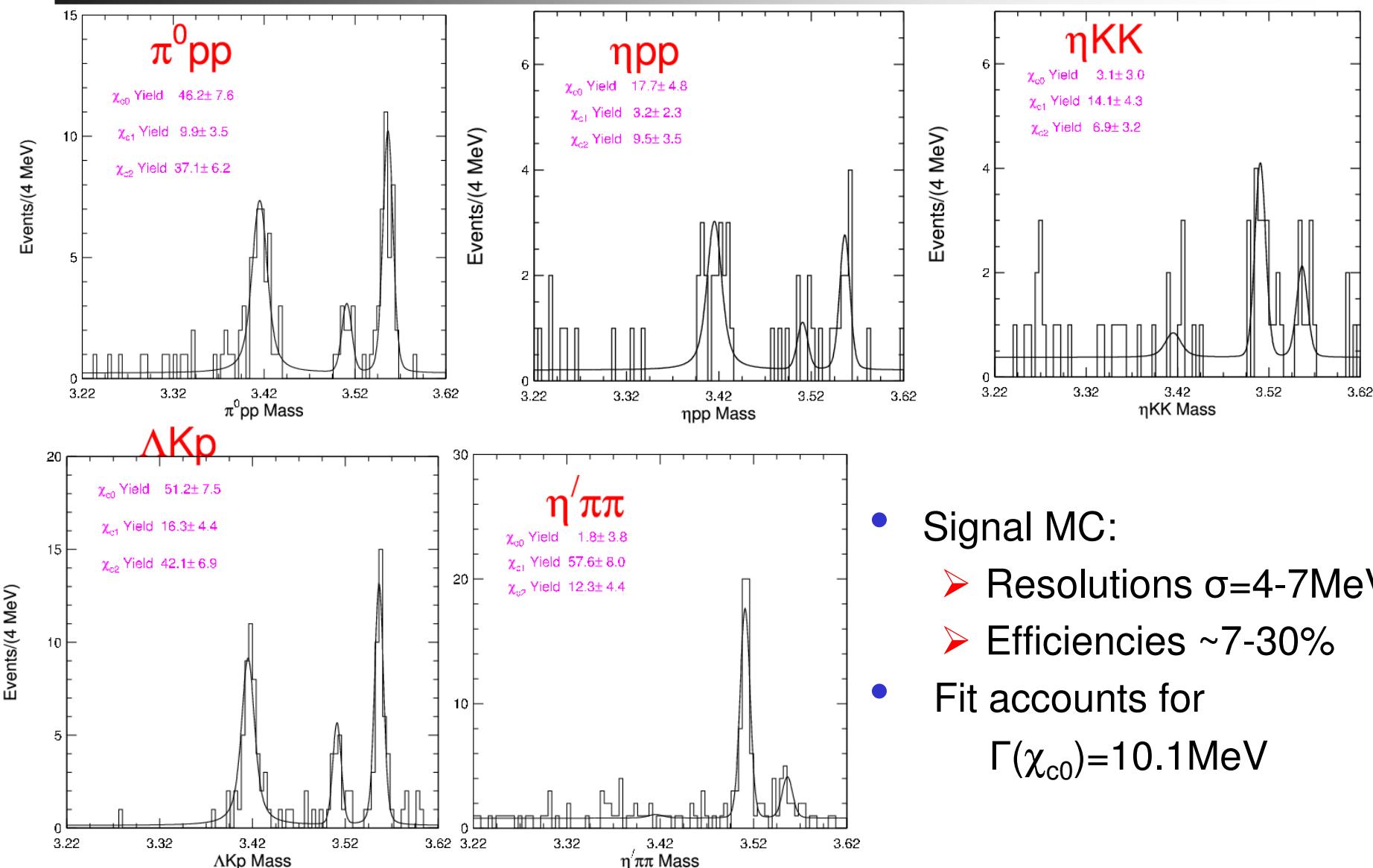
- Resolution  $\sigma=4-9$  MeV/c<sup>2</sup>, Efficiency ~3-19%
- Work on systematic uncertainties in progress
- Investigate an event substructure (w/o PWA)
- Other 4-body modes need to be studied

# $\chi_{cJ} \rightarrow h^0 h^+ h^-$

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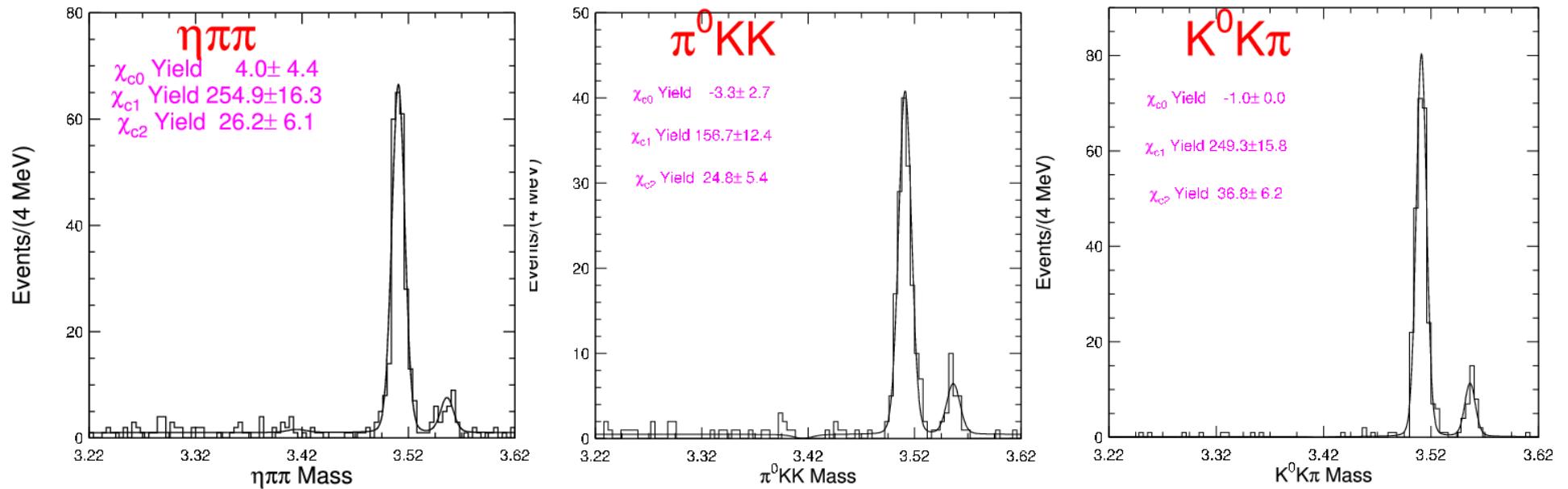
- Study 3-body decays of  $\chi_{cJ} \rightarrow h^0 h^+ h^-$ 
  - Measurement of BR or set UL  
 $\chi_{cJ} \rightarrow \eta\pi^+\pi^-$ ,  $K^+K^-\pi^0$ ,  $K^0_S K\pi$ ,  $\eta K^+K^-$ ,  $\eta'\pi^+\pi^-$ ,  
 $\eta p\bar{p}$ ,  $\pi^0 p\bar{p}$ ,  $\Lambda K\bar{p}$
  - Dalitz plot analysis of 3 modes with high statistics:  $\chi_{c1} \rightarrow \eta\pi^+\pi^-$ ,  $K^+K^-\pi^0$ ,  $K^0_S K\pi$

# Yield $\chi_{cJ} \rightarrow \pi^0 p\bar{p}$ , $\eta p\bar{p}$ , $\eta K^+K^-$ , $\Lambda K\bar{p}$ , $\eta' \pi^+\pi^-$



- Signal MC:
  - Resolutions  $\sigma=4-7\text{MeV}$
  - Efficiencies  $\sim 7-30\%$
- Fit accounts for  $\Gamma(\chi_{c0})=10.1\text{MeV}$

# Yield $\chi_{cJ} \rightarrow \eta\pi^+\pi^-$ , $K^0_S K\pi$ , $K^+K^-\pi^0$



Take  $\chi_{c1}$  statistics for DP analysis

# Dalitz plot formalism

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- Log likelihood

$$\mathcal{L} = -2 \sum_{n=1}^N \log PDF(x_n, y_n)$$

- PDF

$$PDF(x, y) = \begin{cases} \varepsilon(x, y) \\ B(x, y) \\ f N_S |\mathcal{M}(x, y)|^2 \varepsilon(x, y) + (1 - f) N_B B(x, y) \end{cases}$$

- Matrix element

$$\mathcal{M} = \sum_R c_R PW_R \Omega_R F_R$$

- DP for J=1 ?

➤ Angular distributions  $\Omega_R$  from  
 V.Filippini, A.Fontany, A.Rotondi,  
 PR D51(1995) 2247

- Partial waves ( $PW_R$ ):

➤ Breit-Wigner,

➤  $\pi^+ \pi^-$  S-waves:

❖ Oller

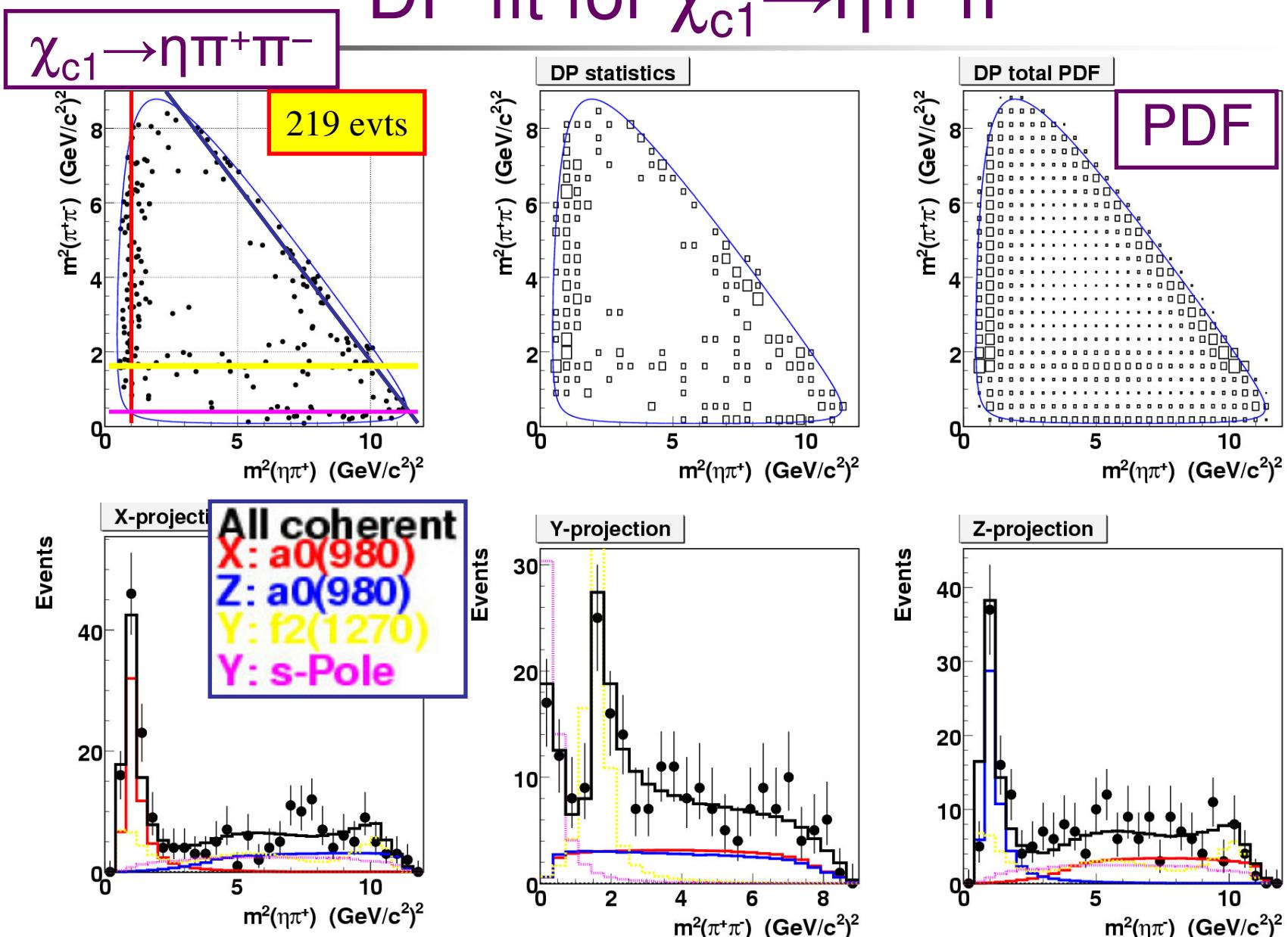
❖ Flatte

$$Pole_A(s) = \frac{1}{s - s_A} \quad s_\sigma = (0.47 - i0.22)^2 \text{ GeV}^2 \text{ for } \pi\pi \text{ S-wave.}$$

$$Flatte_{f_0(980)}(m) = \frac{1}{m_{f_0}^2 - m^2 - i(g_{\pi\pi}^2 \rho_{\pi\pi} + g_{K\bar{K}}^2 \rho_{K\bar{K}})}$$

Fit output

# DP fit for $\chi_{c1} \rightarrow \eta\pi^+\pi^-$



# Sources of systematic uncertainties

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- Event selection
- Efficiency
  - Simultaneous fit to data and MC events with float pars
- Model dependence
  - Angular distributions
  - Other models for  $\pi\pi$  S waves, add/remove resonances/waves, free resonance parameters, etc.

# Results for $\chi_{c1} \rightarrow \eta\pi^+\pi^-$

Mode	Nominal fit
$a_0(980)^+$	1 0
$2\times$	$28.1 \pm 1.8 \pm 0.7$
$f_2(1270)$	$0.186 \pm 0.017 \pm 0.003$ $-118 \pm 10 \pm 4$ $35.1 \pm 2.9 \pm 1.8$
$\sigma$ -pole	$0.68 \pm 0.07 \pm 0.05$ $-85 \pm 18 \pm 15$ $21.7 \pm 3.3 \pm 0.5$
$\sum_i FF_i, \%$	113.1
$-2 \sum \log L$	-460.1
Pearson/ $N_{d.o.f.}$	22.0/24
P(Pearson, $N_{d.o.f.}$ )	58.1%

Amplitude, a.u.  
Phase, degree  
Fit fraction, %

Clebsch-Gordan decomposition for  $\chi_{c1} \rightarrow \eta\pi^+\pi^-$  gives:

$$a_{a(980)^+} = a_{a(980)^-}$$

$$\phi_{a(980)^+} = \phi_{a(980)^-}$$

# Isospin symmetry for $\chi_{c1} \rightarrow K\bar{K}\pi\pi$

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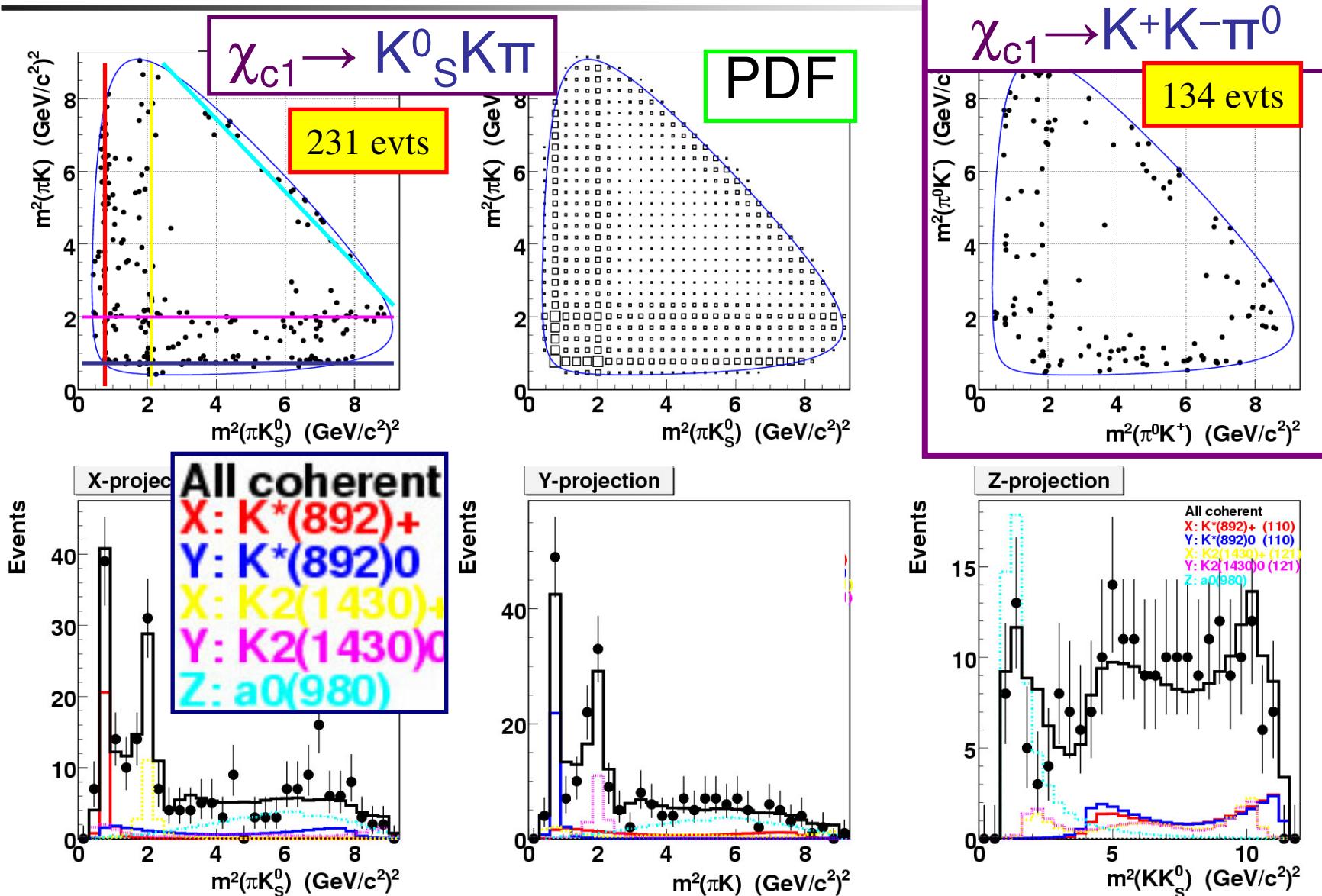
- Rates for  $K^0_S K\pi$  and  $K^+ K^- \pi^0$  modes

$$\Gamma(\chi_{c1} \rightarrow \pi^+ K^- K^0) + \Gamma(\chi_{c1} \rightarrow \pi^- K^+ \overline{K^0}) = 4\Gamma(\chi_{c1} \rightarrow \pi^0 K^+ K^-)$$

- Constrains for the Dalitz plot parameters  
@ individual PDF normalization:

$$\begin{aligned} a_{K^*+} &= a_{K^*-} = a_{K^{*0}} = a_{\overline{K^{*0}}} \equiv a_{K^*}, \\ \phi_{K^*+} &= \phi_{K^*-} = \phi_{K^{*0}} = \phi_{\overline{K^{*0}}} \equiv \phi_{K^*}, \\ a_{a(980)+} &= a_{a(980)-} = a_{a(980)^0} \equiv a_{a(980)}, \\ \phi_{a(980)+} &= \phi_{a(980)-} = \phi_{a(980)^0} \equiv \phi_{a(980)}. \end{aligned}$$

# Combined fit for $\chi_{c1} \rightarrow K^0_S K\pi$ , $K^+ K^- \pi^0$



# Combined fit for $\chi_{c1} \rightarrow K^0_S K\pi$ , $K^+ K^- \pi^0$

Mode	Nominal fit
$K^*(892)$	1 0
$K^+ K^- \pi^0$ : 2x, %	$9.8 \pm 2.0 \pm 1.0$
$K^0_S K\pi$ : 2x, %	$9.9 \pm 2.0 \pm 0.9$
$K_2^*(1430)$	$0.50 \pm 0.09 \pm 0.12$ $-2 \pm 13 \pm 6$
$K^+ K^- \pi^0$ : 2x, %	$9.1 \pm 3.4 \pm 3.4$
$K^0_S K\pi$ : FF( $K_2^*(1430)^+$ ), %	$9.3 \pm 3.4 \pm 1.6$
$K^0_S K\pi$ : FF( $K_2^*(1430)^0$ ), %	$8.4 \pm 3.0 \pm 1.5$
$K_0^*(1430)$	$5.3 \pm 1.0 \pm 0.1$ $77 \pm 12 \pm 16$
$K^+ K^- \pi^0$ : 2x, %	$17.8 \pm 6.3 \pm 1.3$
$K^0_S K\pi$ : 2x, %	$18.2 \pm 6.4 \pm 1.6$
$K^*(1680)$	$2.3 \pm 0.5 \pm 0.5$ $-38 \pm 12 \pm 12$
$K^+ K^- \pi^0$ : 2x, %	$5.5 \pm 2.7 \pm 1.7$
$K^0_S K\pi$ : 2x, %	$5.6 \pm 2.6 \pm 1.0$
$a_0(980)$	$10.8 \pm 1.2 \pm 1.2$ $-112 \pm 12 \pm 3$
$K^+ K^- \pi^0$ , %	$29.5 \pm 7.3 \pm 2.8$
$K^0_S K\pi$ , %	$29.4 \pm 6.9 \pm 2.2$
$\sum_i FF_i$ , %	$\sim 115$
$-\sum \log L$	$-545.7$
Pearson/ $N_{d.o.f.}$	$57.2/53$
P(Pearson, $N_{d.o.f.}$ ), %	32.1

Amplitude, a.u.  
 Phase, degree  
 Fit fraction(s), %

- $K^*(892)$ ,  $K_2^*(1430)$ ,  $a_0(980)$  are clearly seen but not sufficient to provide good fit.
- We find several models with good fit quality with additional
  - +  $K_0^*(1430)$ ,  $K^*(1680)$ , Prob.~30%
  - + NR, Prob.~17%
  - + K, Prob.~10%
- With larger statistics we hope to resolve this ambiguity.

# Preliminary $\mathcal{B} (\%)$ for $\chi_{cJ} \rightarrow h^0 h^+ h^-$

Mode	$\chi_{c0}$	$\chi_{c1}$	$\chi_{c2}$
$\eta\pi^+\pi^-$	$< 0.021$	$0.52 \pm .03 \pm .03 \pm .03$	$0.051 \pm .011 \pm .004 \pm .003$
$\eta K^+K^-$	$< 0.024$	$0.034 \pm .010 \pm .003 \pm .002$	$< 0.033$
$\eta p\bar{p}$	$0.038 \pm .010 \pm .003 \pm .02$	$< 0.015$	$.019 \pm .007 \pm .002 \pm .002$
$\eta'\pi^+\pi^-$	$< 0.038$	$0.24 \pm .03 \pm .02 \pm .02$	$< 0.053$
$\pi^0 K^+K^-$	$< 0.006$	$0.200 \pm .015 \pm .018 \pm .014$	$0.032 \pm .007 \pm .002 \pm .002$
$\pi^0 p\bar{p}$	$0.059 \pm .010 \pm .006 \pm .004$	$0.059 \pm .010 \pm .005 \pm .004$	$0.045 \pm .007 \pm .004 \pm .003$
$\Lambda K^+\bar{p}$	$0.114 \pm .016 \pm .009 \pm .007$	$0.034 \pm .009 \pm .003 \pm .002$	$0.088 \pm .014 \pm .07 \pm .006$
$K^0 K^+\pi^-$	$< 0.005$	$0.84 \pm .05 \pm .06 \pm .05$	$0.13 \pm .02 \pm .01 \pm .01$

PDG 2004, $K^0_S K\pi$ : $< 0.08$	$0.25 \pm 0.07$	$< 0.13$ BES '99
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x2

- Uncertainties: *stat.*, *syst.*,  $\mathcal{B}(\psi(2S) \rightarrow \gamma \chi_{cJ})$
- Dalitz plot analysis gives splitting of  $\mathcal{BR}$  for sub-modes of  $\chi_{c1} \rightarrow \eta\pi^+\pi^-, K^+K^-\pi^0, K^0_S K\pi$

# Summary

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- Using  $\sim 3M$   $\Psi(2S)$  we study  $\Psi(2S) \rightarrow \gamma \chi_{cJ}$ ,  $J=0,1,2$
- We search for and find a strong signal in numerous  $\chi_{cJ}$  hadronic decay modes.
- Today we present a few of them:
  - $\chi_{cJ} \rightarrow \eta^{(')} \eta^{(')}$  3 modes
  - $\chi_{cJ} \rightarrow VV$  ( $V = \varphi, \omega$ ) 2 modes
  - $\chi_{cJ} \rightarrow h^+ h^- h^0 h^0$  ( $h = \pi, K, \eta, p$ ) 7 modes
  - $\chi_{cJ} \rightarrow h^+ h^- h^0$  8 modes
- Measurement of BR or set UL for **20** modes  $\times 3$   $\chi_{cJ}$  states
- Dalitz plot analysis of 3 modes:  $\chi_{c1} \rightarrow \eta \pi^+ \pi^-$ ,  $K^+ K^- \pi^0$ ,  $K_S^0 K \pi$
- $\times 10$   $\psi(2S)$  statistics is expected by the end of the year