

# CLEO-c Measurement of the Pseudoscalar Decay Constant $f_{D_s}$ & the Ratio $f_{D_s}/f_{D^+}$

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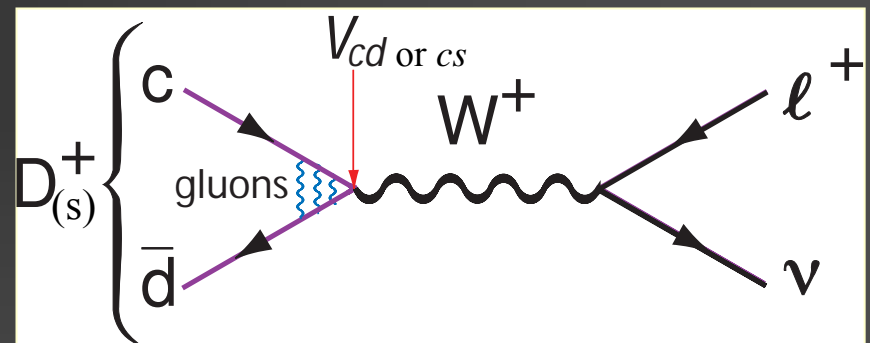


# Leptonic Decays: $D_{(s)} \rightarrow \ell^+ \nu$

Introduction: Pseudoscalar decay constants

$c$  and  $\bar{q}$  can annihilate, probability is  $\propto$  to wave function overlap

Example :



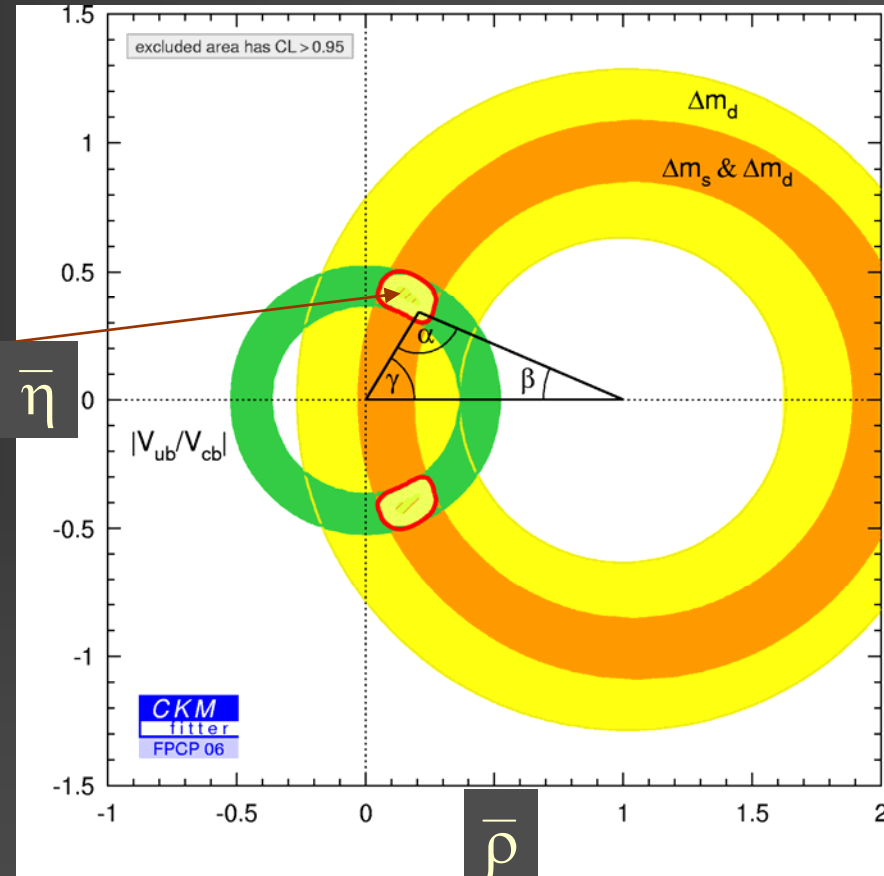
In general for all pseudoscalars:

$$\Gamma(P^+ \rightarrow \ell^+ \nu) = \frac{1}{8\pi} G_F^2 f_P^2 m_\ell^2 M_P \left(1 - \frac{m_\ell^2}{M_P^2}\right)^2 |V_{Qq}|^2$$

Calculate, or measure if  $V_{Qq}$  is known

# Goals in Leptonic Decays

- Test theoretical calculations in strongly coupled theories in non-perturbative regime
- $f_B$  &  $f_{B_s}/f_B$  needed to improve constraints from  $\Delta m_d$  &  $\Delta m_s/\Delta m_d$ . Hard to measure directly (i.e.  $B \rightarrow \tau^+ \nu$  measures  $V_{ub} f_B$ ), but we can determine  $f_D$  &  $f_{D_s}$  using  $D \rightarrow \ell^+ \nu$  and use them to test theoretical models (i.e. Lattice QCD)



Constraints from  $V_{ub}$ ,  $\Delta m_d$ ,  $\Delta m_s$  &  $B \rightarrow \tau^+ \nu$

# Experimental methods

- $D\bar{D}$  production at threshold: used by Mark III, and more recently by CLEO-c and BES-II.

- Unique event properties
  - Only  $D\bar{D}$  not  $D\bar{D}x$  produced

- Large cross sections:

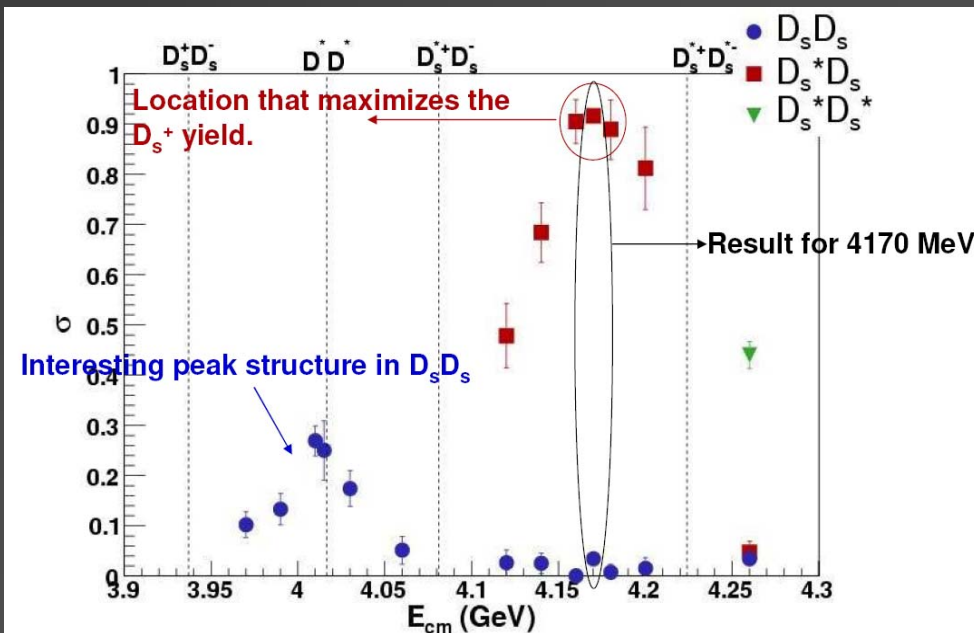
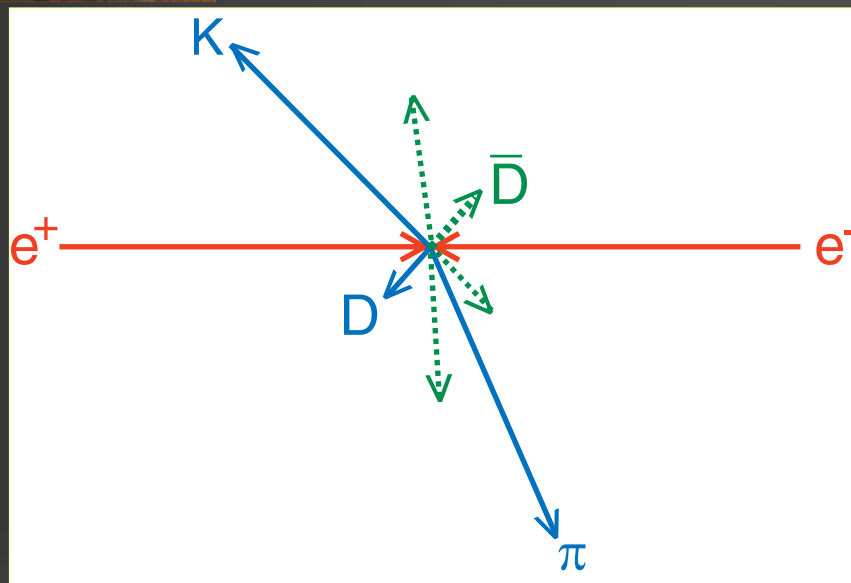
$$\left. \begin{aligned} \sigma(D^0\bar{D}^0) &= 3.72 \pm 0.09 \text{ nb} \\ \sigma(D^+D^-) &= 2.82 \pm 0.09 \text{ nb} \end{aligned} \right\} \begin{array}{l} \text{World} \\ \text{Ave} \end{array}$$

$$\sigma(D_s D_s^*) = \sim 0.9 \text{ nb}$$

Continuum  $\sim 14 \text{ nb}$

- Ease of B measurements using "double tags"

- $\mathcal{B}_A = \# \text{ of } A / \# \text{ of } D\text{'s}$



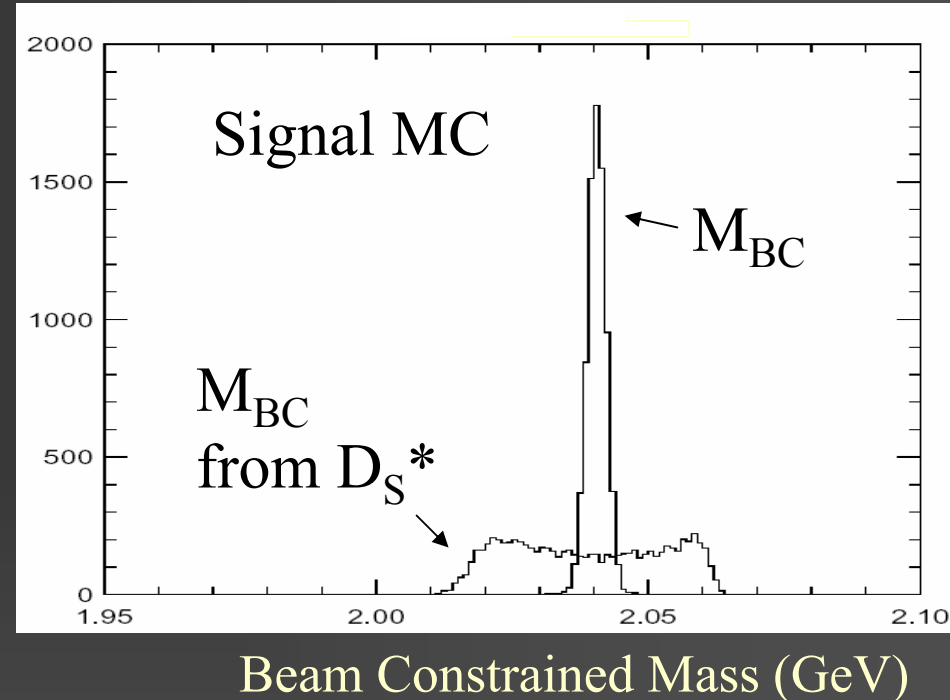
# CLEO $D_S^+$ Results at 4170 MeV

- Since  $e^+e^- \rightarrow D_S^* D_S$ , the  $D_S$  from the  $D_S^*$  will be smeared in beam-constrained mass.

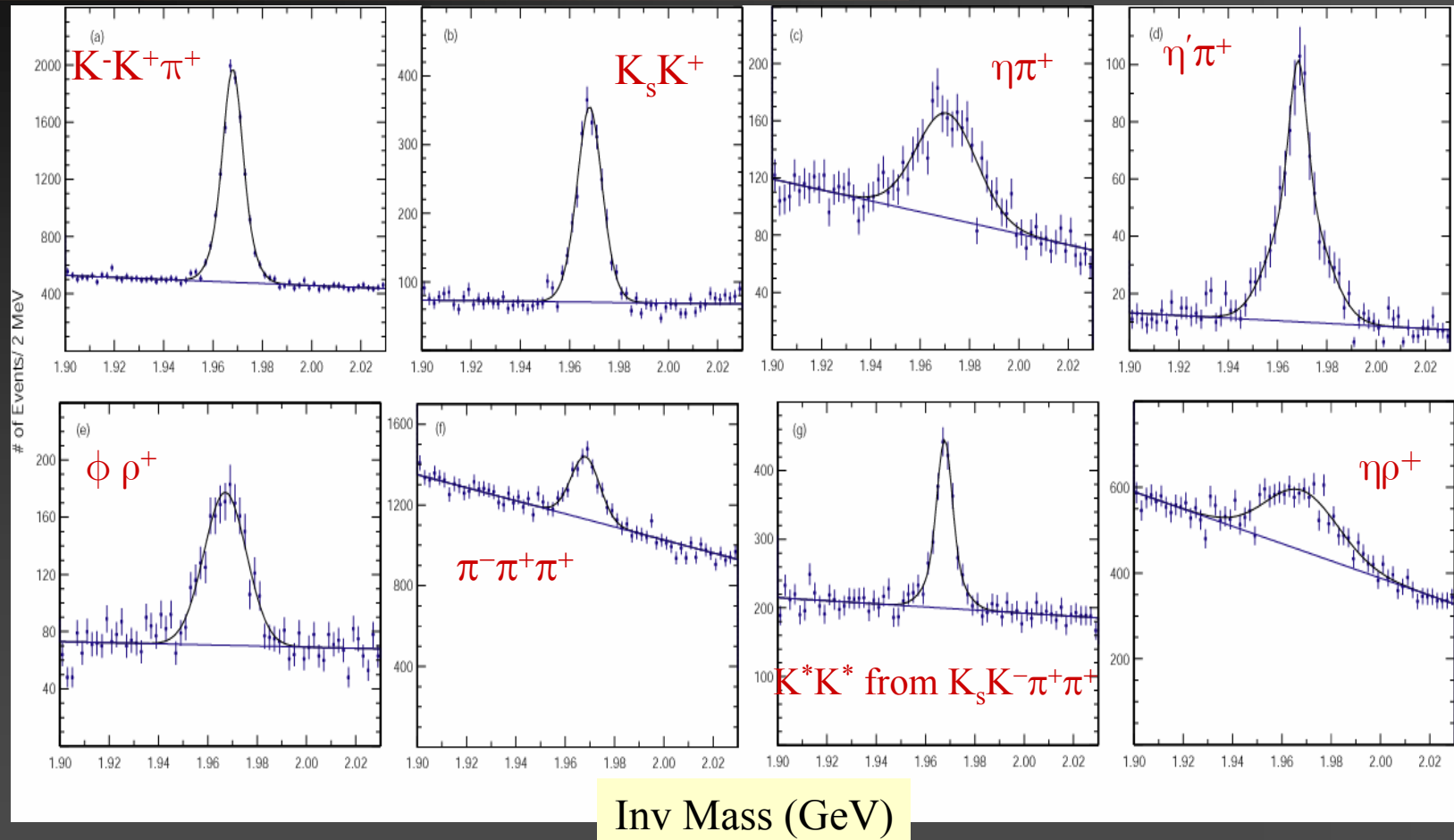
- $$M_{BC}^2 = E_{\text{beam}}^2 - \sum_i \vec{p}_i^2$$

- $\therefore$  cut on  $M_{BC}$  & plot invariant mass (equivalent to a p cut)

- We use  $\sim 200 \text{ pb}^{-1}$  of data



# Invariant masses



Total # of Tags =  $19,185 \pm 325$  (stat)

# New Measurements of $f_{D_s}$

- Two separate techniques
- (1) Measure  $D_s^+ \rightarrow \mu^+ \nu$  along with  $D_s \rightarrow \tau^+ \nu$ ,  $\tau \rightarrow \pi^+ \nu$ . This requires finding a  $D_s^-$  tag, a  $\gamma$  from either  $D_s^{*-} \rightarrow \gamma D_s^-$  or  $D_s^{*+} \rightarrow \gamma \mu^+ \nu$ . Then finding the muon or pion using kinematical constraints
- (2) Find  $D_s^+ \rightarrow \tau^+ \nu$ ,  $\tau \rightarrow e^+ \nu \nu$  opposite a  $D_s^-$  tag

# Measurement of $D_S^+ \rightarrow \mu^+ \nu$

- In this analysis we use  $D_S^* D_S$  events where we detect the  $\gamma$  from the  $D_S^* \rightarrow \gamma D_S$  decay
- We see all the particles from  $e^+ e^- \rightarrow D_S^* D_S, \gamma, D_S$  (tag) +  $\mu^+$  except for the  $\nu$
- We use a kinematic fit to (a) improve the resolution & (b) remove ambiguities
  - Constraints include: total p & E, tag  $D_S$  mass,  $\Delta m = M(\gamma D_S) - M(D_S)$  [or  $\Delta m = M(\gamma \mu \nu) - M(\mu \nu) = 143.6$  MeV, E of  $D_S$  (or  $D_S^*$ ) fixed
  - Lowest  $\chi^2$  solution in each event is kept
  - No  $\chi^2$  cut is applied

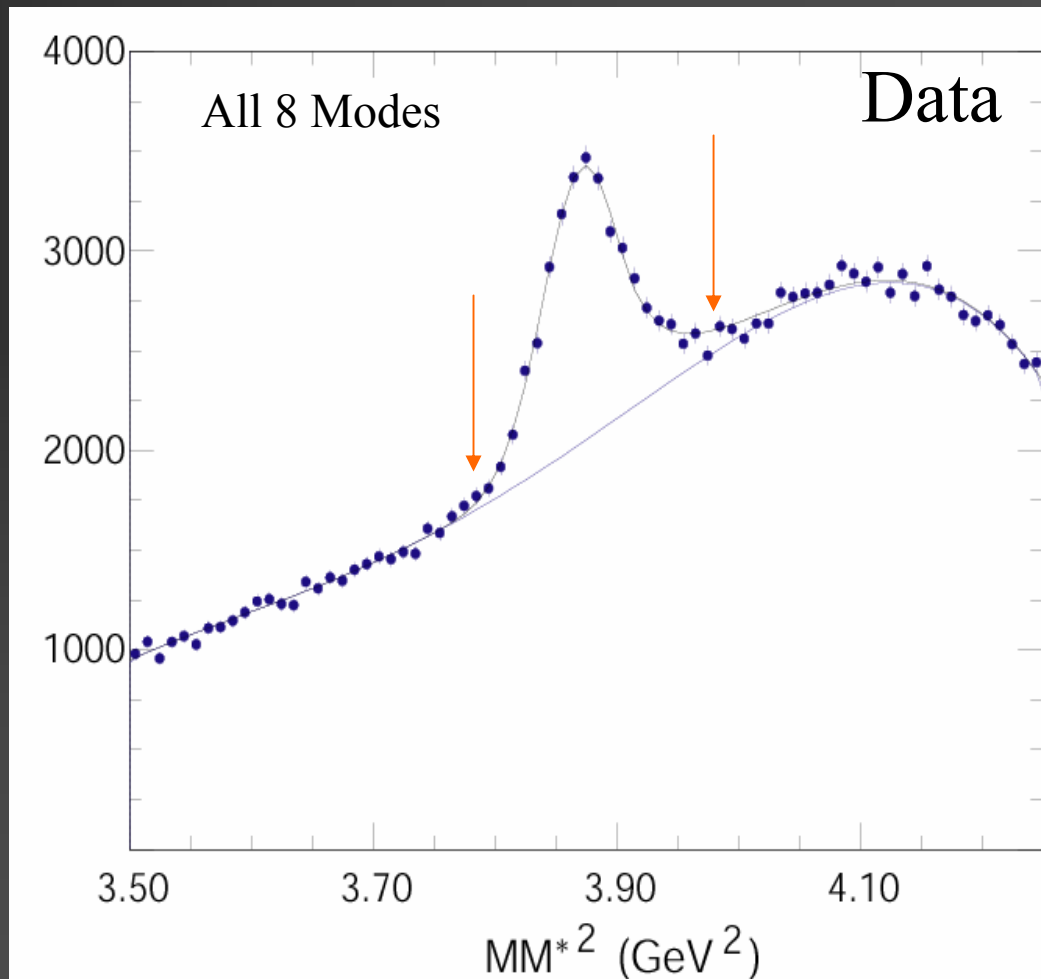


# Tag Sample using $\gamma$

- First we define the tag sample by computing the  $MM^{*2}$  off of the  $\gamma$  &  $D_s$  tag

$$MM^{*2} = (E_{CM} - E_{D_s} - E_{\gamma})^2 - (-\vec{p}_{D_s} - \vec{p}_{\gamma})^2$$

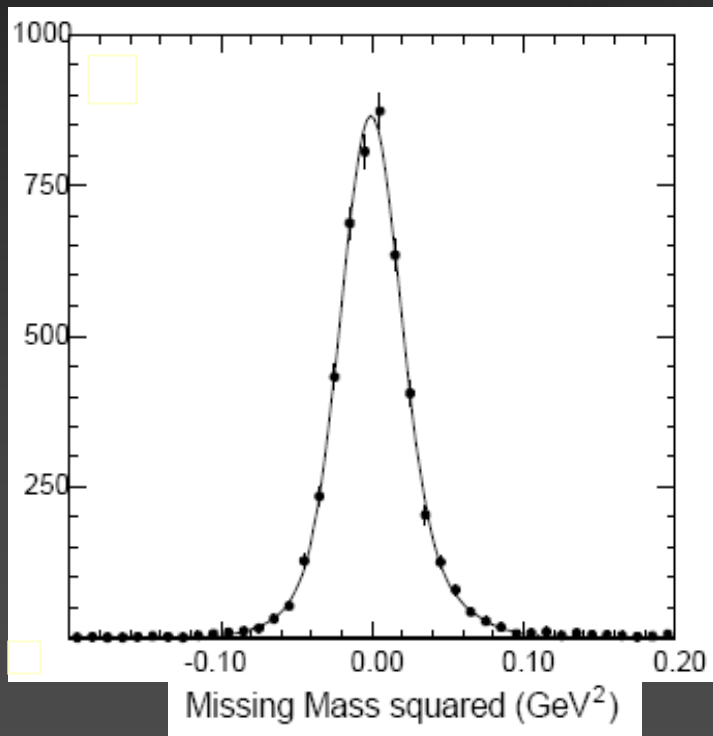
- Total of  $11880 \pm 399 \pm 504$  tags, after the selection on  $MM^{*2}$ .



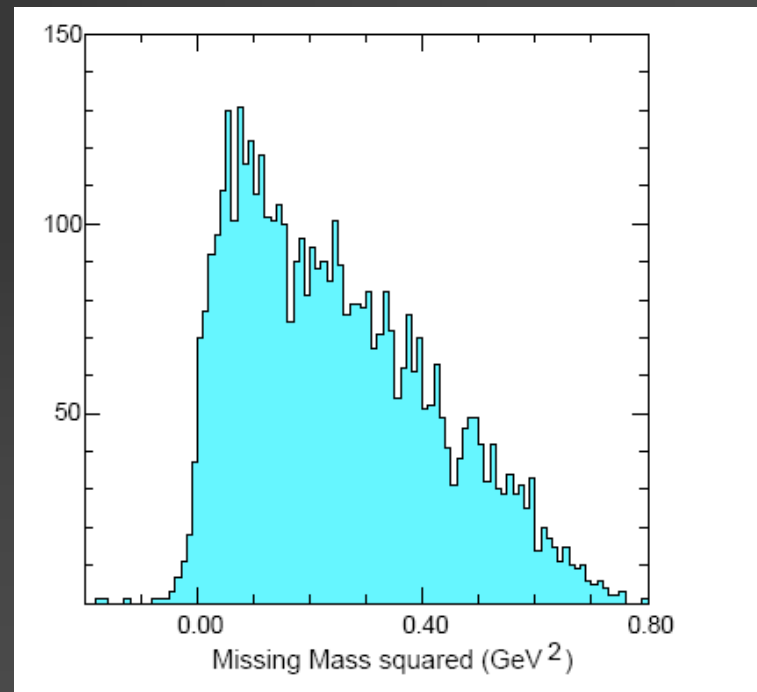
# The $MM^2$

- To find the signal events, we compute

$$MM^2 = (E_{CM} - E_{D_S} - E_{\gamma} - E_{\mu})^2 - (-\vec{p}_{D_S} - \vec{p}_{\gamma} - \vec{p}_{\mu})^2$$



Signal  $\mu\nu$



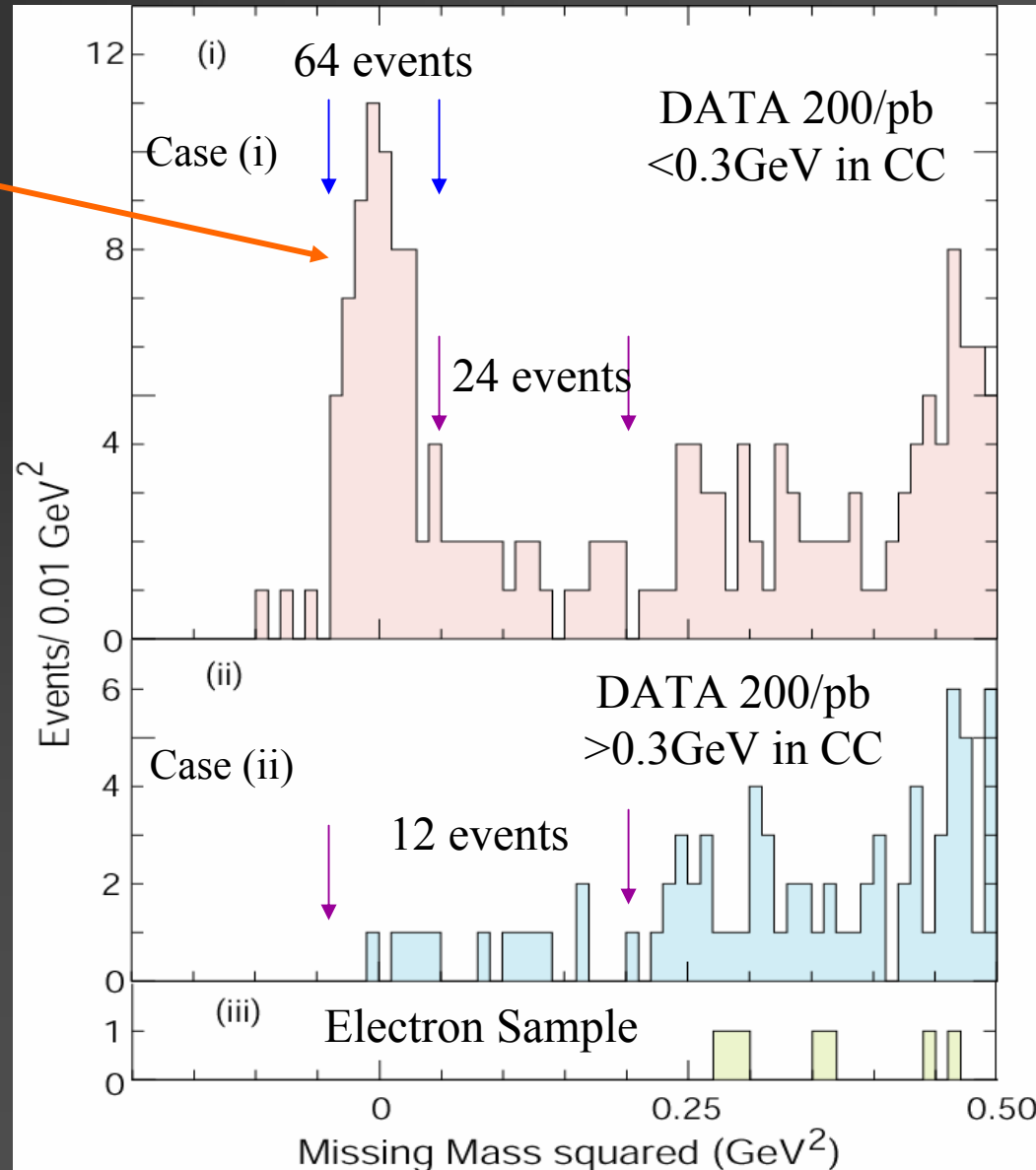
Signal  $\tau\nu, \tau \rightarrow \pi\nu$

# Define Three Classes

- Class (i), single track deposits  $< 300$  MeV in calorimeter (consistent with  $\mu$ ) & no other  $\gamma > 300$  MeV. (accepts 99% of muons and 60% of kaons & pions)
- Class (ii), single track deposits  $> 300$  MeV in calorimeter & no other  $\gamma > 300$  MeV (accepts 1% of muons and 40% of kaons & pions)
- Class (iii) single track consistent with electron & no other  $\gamma > 300$  MeV

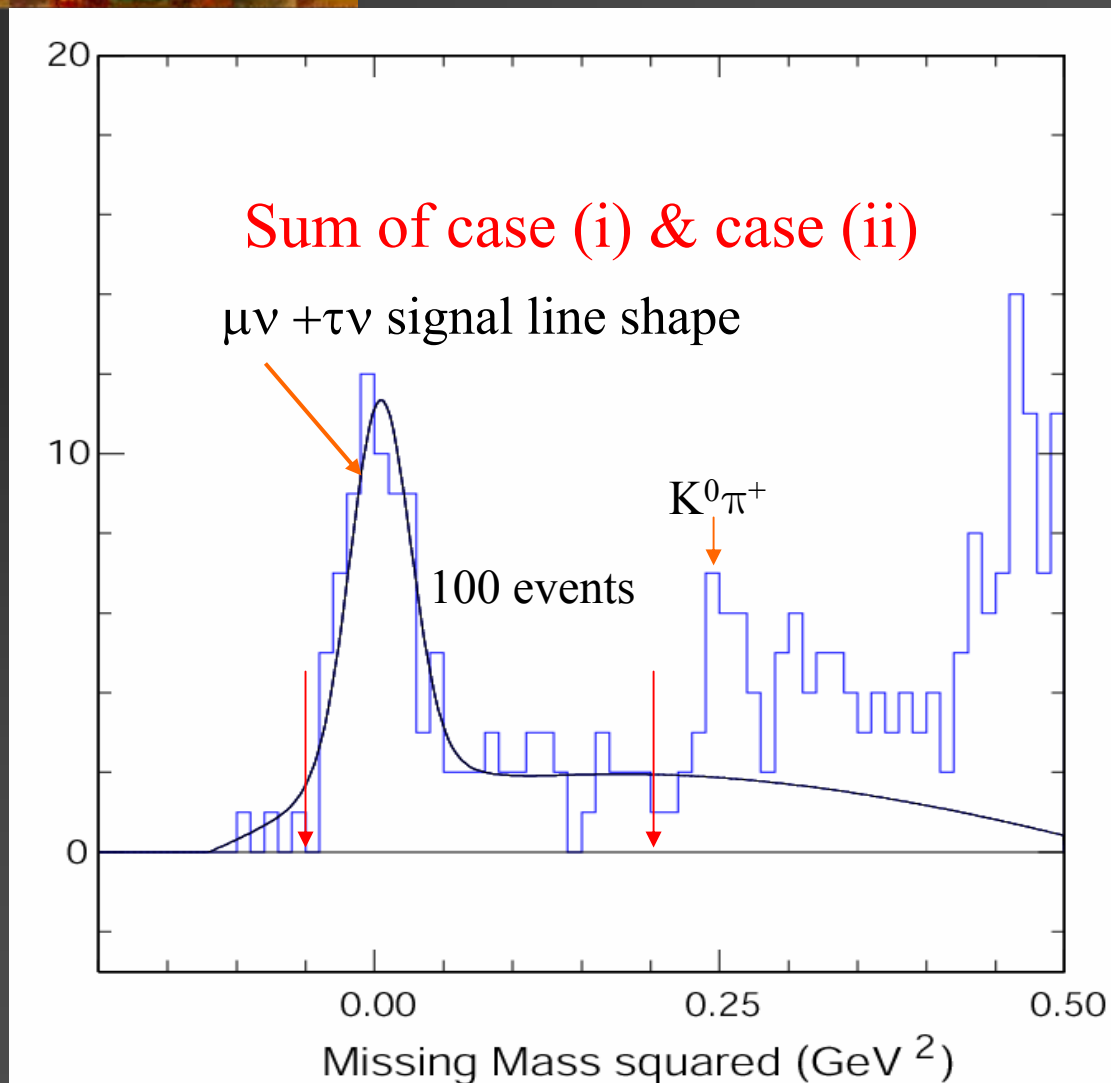
# MM<sup>2</sup> Results from 200 pb<sup>-1</sup>

- Clear  $D_S^+ \rightarrow \mu^+ \nu$  signal for case (i)
- Will show that events  $< 0.2 \text{ GeV}^2$  are mostly  $D_S \rightarrow \tau^+ \nu$ ,  $\tau \rightarrow \pi^+ \nu$  in cases (i) & (ii)
- No  $D_S \rightarrow e^+ \nu$  seen, case (iii)



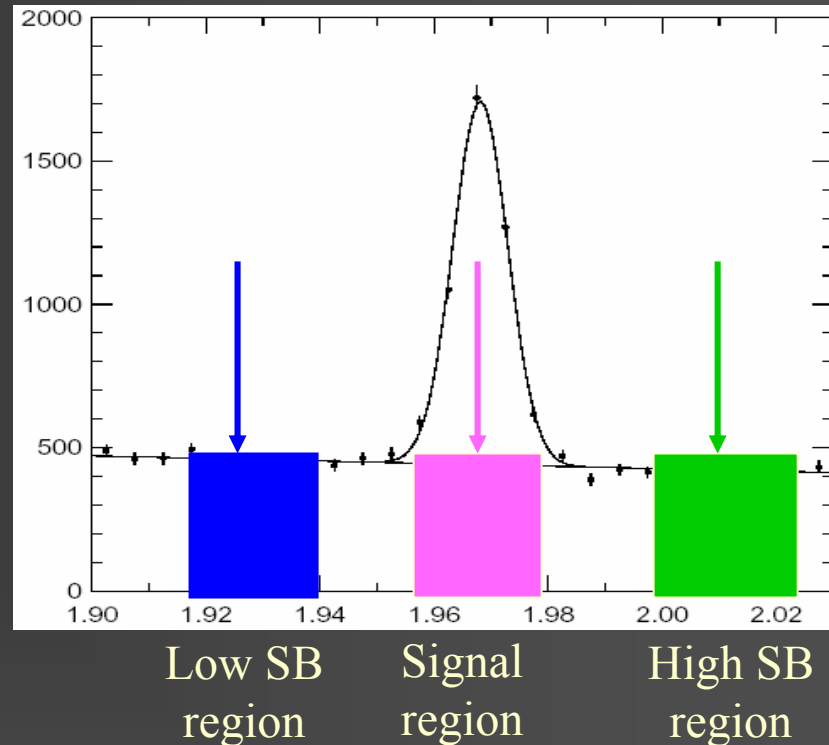
# Sum of $D_S^+ \rightarrow \mu^+ \nu + \tau^+ \nu$ , $\tau \rightarrow \pi^+ \nu$

- Sum contains 100  $\mu^+ \nu + \tau^+ \nu$  events for  $MM^2 < 0.2$   $\text{GeV}^2$



# Background Samples

- Two sources of background
- A) Backgrounds under invariant mass peaks – Use sidebands to estimate
- In  $\mu^+\nu$  signal region 2 background (64 signal)
- Total sideband bkgrnd  $5.5 \pm 1.9$
- B) Backgrounds from real  $D_S$  decays, e.g.  $\pi^+\pi^0\pi^0$ , or  $D_S \rightarrow \tau^+\nu$ ,  $\tau \rightarrow \pi^+\pi^0\nu \dots < 0.2 \text{ GeV}^2$ , none in  $\mu\nu$  signal region
- $B(D_S \rightarrow \pi^+\pi^0) < 1.1 \times 10^{-3}$  &  $\gamma$  energy cut yields  $< 0.1$  evts



Backgrounds from real  $D_S^+$

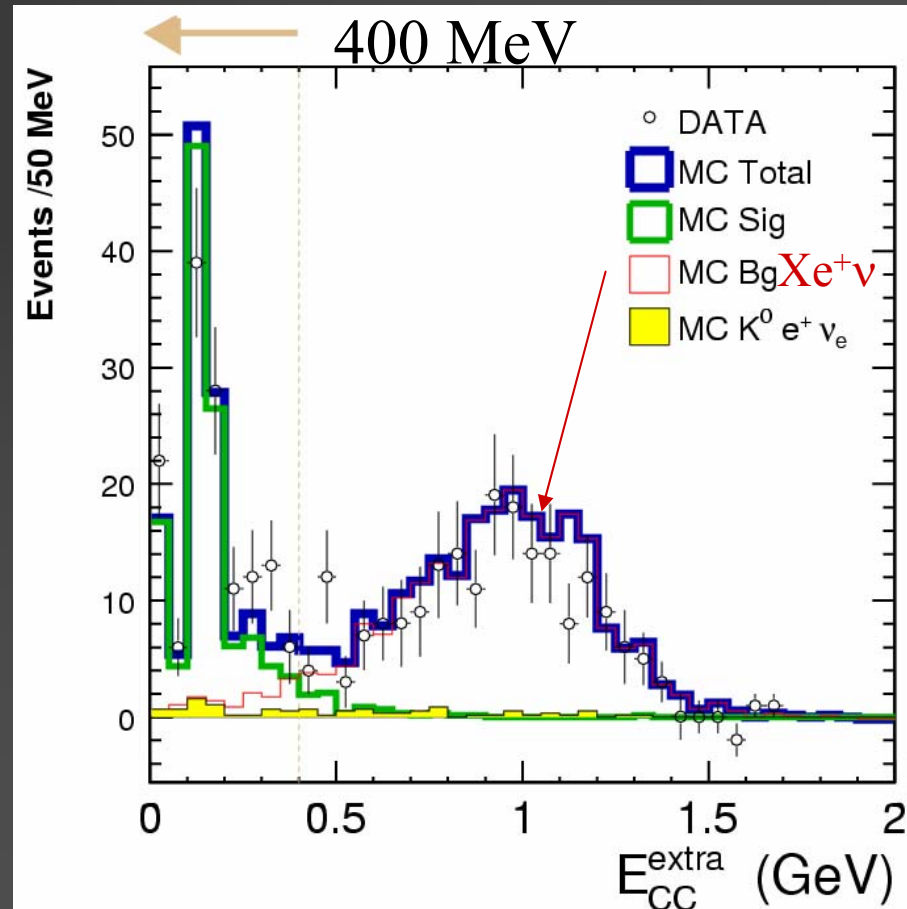
Mode	$\mathcal{B}(\%)$	# of events case(i)	# of events case(ii)	Sum
$\pi^+\pi^0\pi^0$	1.0	0.1	0.3	0.4
$D_s^+ \rightarrow \tau^+\nu$	6.2			
$\tau^+ \rightarrow \pi^+\pi^0\nu$	1.6	0.3	0.4	0.7
$\tau^+ \rightarrow \mu^+\bar{\nu}\nu$	1.1	0	0	0
$\tau^+ \rightarrow e^+\bar{\nu}\nu$	1.1	0.2	0	0.2
Sum		0.6	0.7	1.3

# Branching Ratio & Decay Constant

- $D_S^+ \rightarrow \mu^+ \nu$ 
  - 64 signal events, 2 background, use SM to calculate  $\tau \nu$  yield near 0  $MM^2$  based on known  $\tau \nu / \mu \nu$  ratio
  - $B(D_S^+ \rightarrow \mu^+ \nu) = (0.657 \pm 0.090 \pm 0.028)\%$
- $D_S^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow \pi^+ \nu$ 
  - Sum case (i)  $0.2 > MM^2 > 0.05 \text{ GeV}^2$  & case (ii)  $MM^2 < 0.2 \text{ GeV}^2$ . Total of 36 signal and 4.8 bkgrnd
  - $B(D_S^+ \rightarrow \tau^+ \nu) = (7.1 \pm 1.4 \pm 0.03)\%$
- By summing both cases above, find  
 $B^{\text{eff}}(D_S^+ \rightarrow \mu^+ \nu) = (0.664 \pm 0.076 \pm 0.028)\%$
- $f_{D_S} = 282 \pm 16 \pm 7 \text{ MeV}$
- $B(D_S^+ \rightarrow e^+ \nu) < 3.1 \times 10^{-4}$

# Measuring $D_S^+ \rightarrow \tau^+ \nu$ , $\tau^+ \rightarrow e^+ \nu \nu$

- $B(D_S^+ \rightarrow \tau^+ \nu) \cdot B(\tau^+ \rightarrow e^+ \nu \nu) \sim 1.3\%$  is “large” compared with expected  $B(D_S^+ \rightarrow X e^+ \nu) \sim 8\%$
- Technique is to find events with an  $e^+$  opposite  $D_S^-$  tags & no other tracks, with  $\Sigma$  calorimeter energy  $< 400$  MeV
- No need to find  $\gamma$  from  $D_S^*$
- $B(D_S^+ \rightarrow \tau^+ \nu) = (6.29 \pm 0.78 \pm 0.52)\%$
- $f_{D_S} = 278 \pm 17 \pm 12$  MeV





# $f_{D_s}$ & $f_{D_s} / f_{D^+}$

- **Weighted Average:**  $f_{D_s} = 280.1 \pm 11.6 \pm 6.0$  MeV, the systematic error is mostly uncorrelated between the measurements

- Previously CLEO-c measured

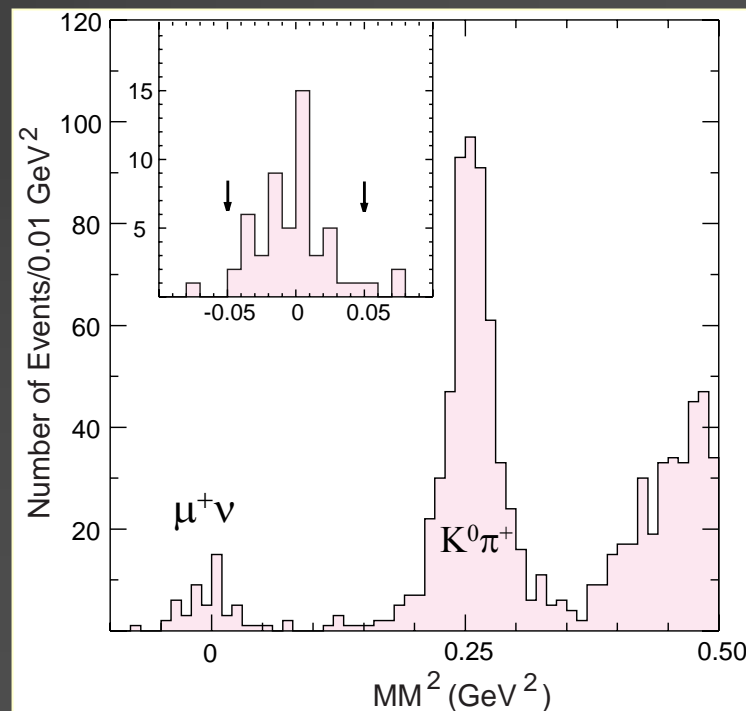
$$f_{D^+} = (222.6 \pm 16.7^{+2.3}_{-3.4}) \text{ MeV}^\dagger$$

<sup>†</sup> M. Artuso et al., Phys. Rev. Lett. 95 (2005) 251801

- Thus  $f_{D_s} / f_{D^+} = 1.26 \pm 0.11 \pm 0.03$

- $\Gamma(D_s^+ \rightarrow \tau^+ \nu) / \Gamma(D_s^+ \rightarrow \mu^+ \nu) = 9.9 \pm 1.7 \pm 0.7$ , SM = 9.72, consistent with lepton universality

$D^+ \rightarrow \mu^+ \nu$

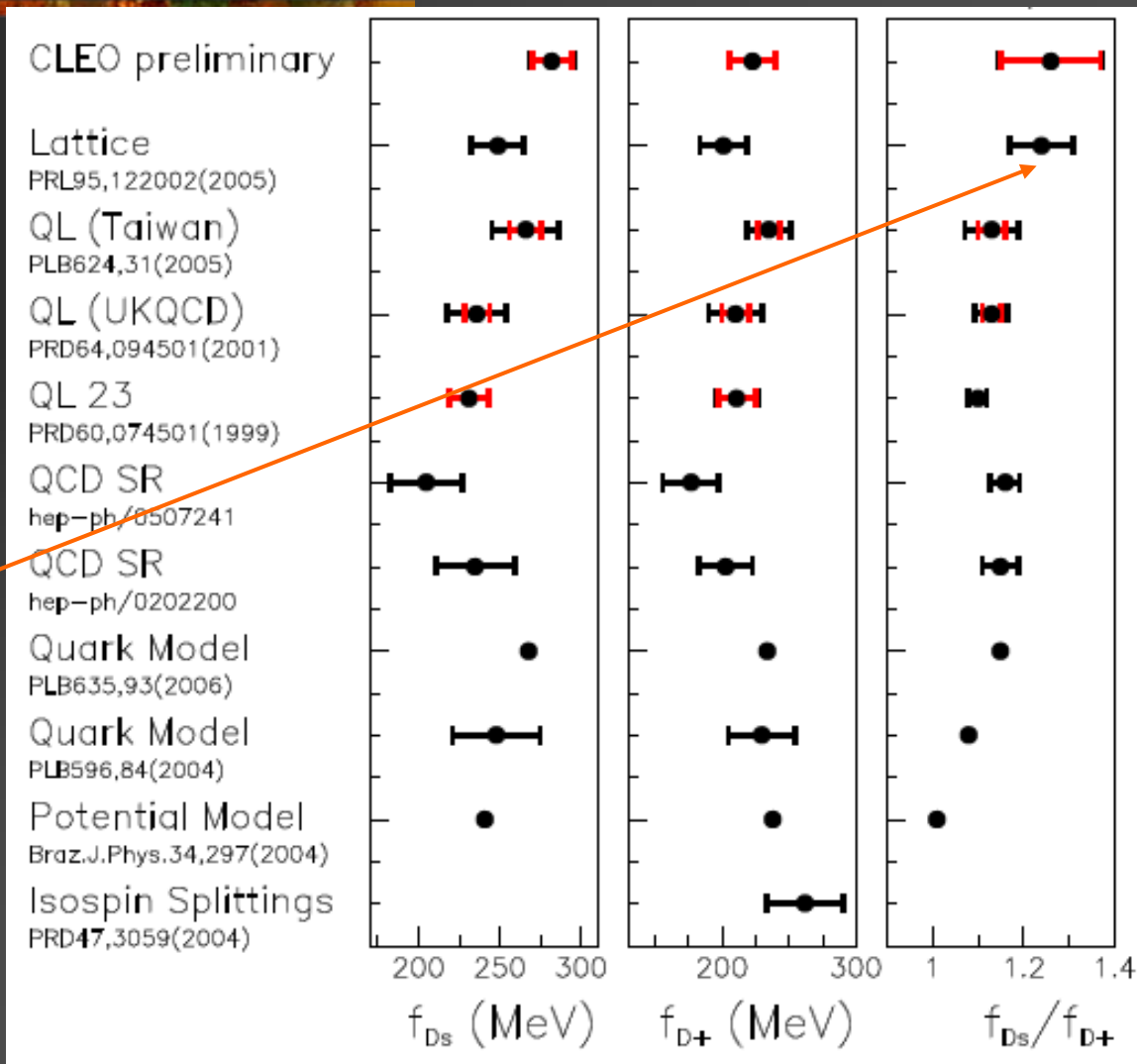


# Comparisons with Theory

- We are consistent with most models, more precision needed

- Using Lattice ratio find

$$|V_{cd}/V_{cs}| = 0.22 \pm 0.03$$



# Comparison with Previous Experiments

TABLE VI: These results compared with previous measurements. Results have been updated for new values of the  $D_s$  lifetime. ALEPH uses both measurements to derive a value for the decay constant.

Exp.	Mode	$\mathcal{B}$	$\mathcal{B}_{\phi\pi}$ (%)	$f_{D_s^+}$ (MeV)
CLEO-c	combined	-		<b>280.1±11.6±6.0</b>
CLEO [30]	$\mu^+\nu$	$(6.2 \pm 0.8 \pm 1.3 \pm 1.6)10^{-3}$	$3.6 \pm 0.9$	$273 \pm 19 \pm 27 \pm 33$
BEATRICE [31]	$\mu^+\nu$	$(8.3 \pm 2.3 \pm 0.6 \pm 2.1)10^{-3}$	$3.6 \pm 0.9$	$315 \pm 43 \pm 12 \pm 39$
ALEPH [32]	$\mu^+\nu$	$(6.8 \pm 1.1 \pm 1.8)10^{-3}$	$3.6 \pm 0.9$	$285 \pm 19 \pm 40$
ALEPH [32]	$\tau^+\nu$	$(5.8 \pm 0.8 \pm 1.8)10^{-2}$		
OPAL [34]	$\tau^+\nu$	$(7.0 \pm 2.1 \pm 2.0)10^{-3}$	?	$286 \pm 44 \pm 41$
L3 [33]	$\tau^+\nu$	$(7.4 \pm 2.8 \pm 1.6 \pm 1.8)10^{-3}$	?	$302 \pm 57 \pm 32 \pm 37$
BaBar [36]	$\mu^+\nu$	$(6.5 \pm 0.8 \pm 0.3 \pm 0.9)10^{-3}$	$4.8 \pm 0.5 \pm 0.4$	$279 \pm 17 \pm 6 \pm 19$

- CLEO-c is most precise result to date for both  $f_{D_s}$  &  $f_{D^+}$



*The End*

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