

# The Transition

$$\psi(2S) \rightarrow \gamma\eta_c(1S)$$

## at CLEO-c

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QWG 2007

# The CLEO-c Experiment

CESR at Cornell University, USA

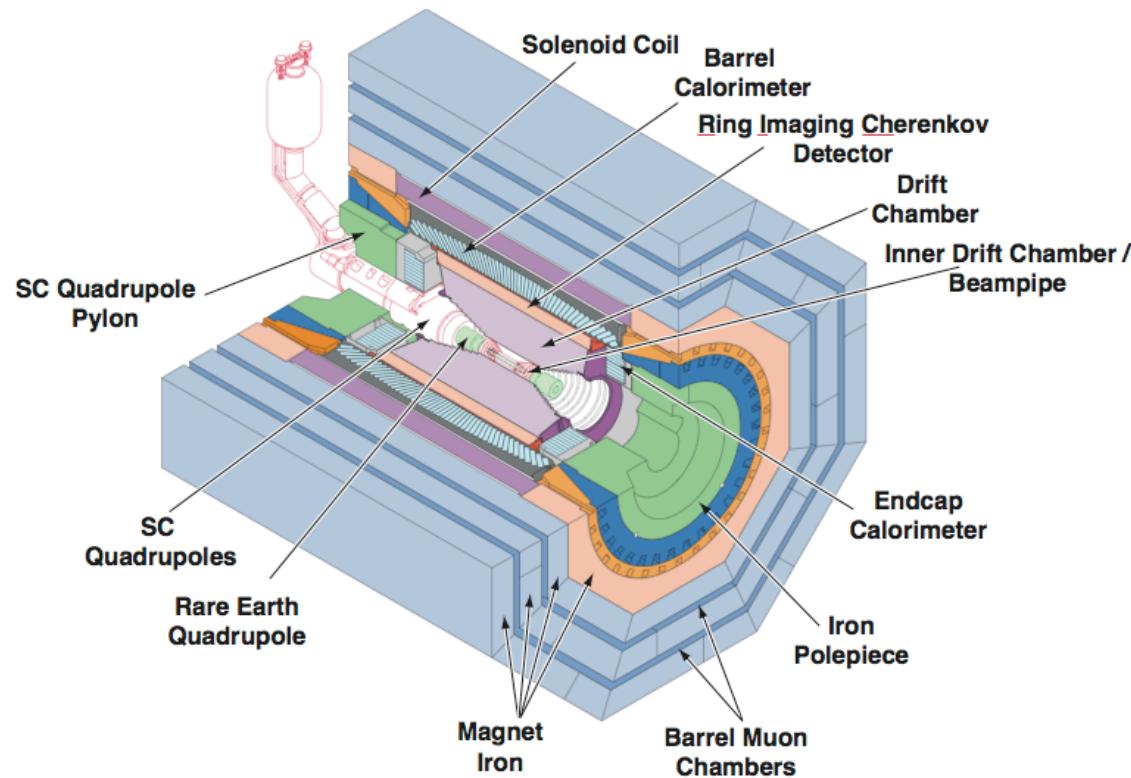
$e^+e^-$  collisions at  $\sqrt{s} \sim 4$  GeV

2003 - present

## Data Samples:

3.97 - 4.26 GeV	$\sim 60 \text{ pb}^{-1}$
4.17 GeV	$\sim 300 \text{ pb}^{-1}$
$\psi(3770)$	$\sim 800 \text{ pb}^{-1}$
$\psi(2S)$	$\sim 3\text{M (1.5M CLEO-III)} +$ $\sim 24.5\text{M events}$

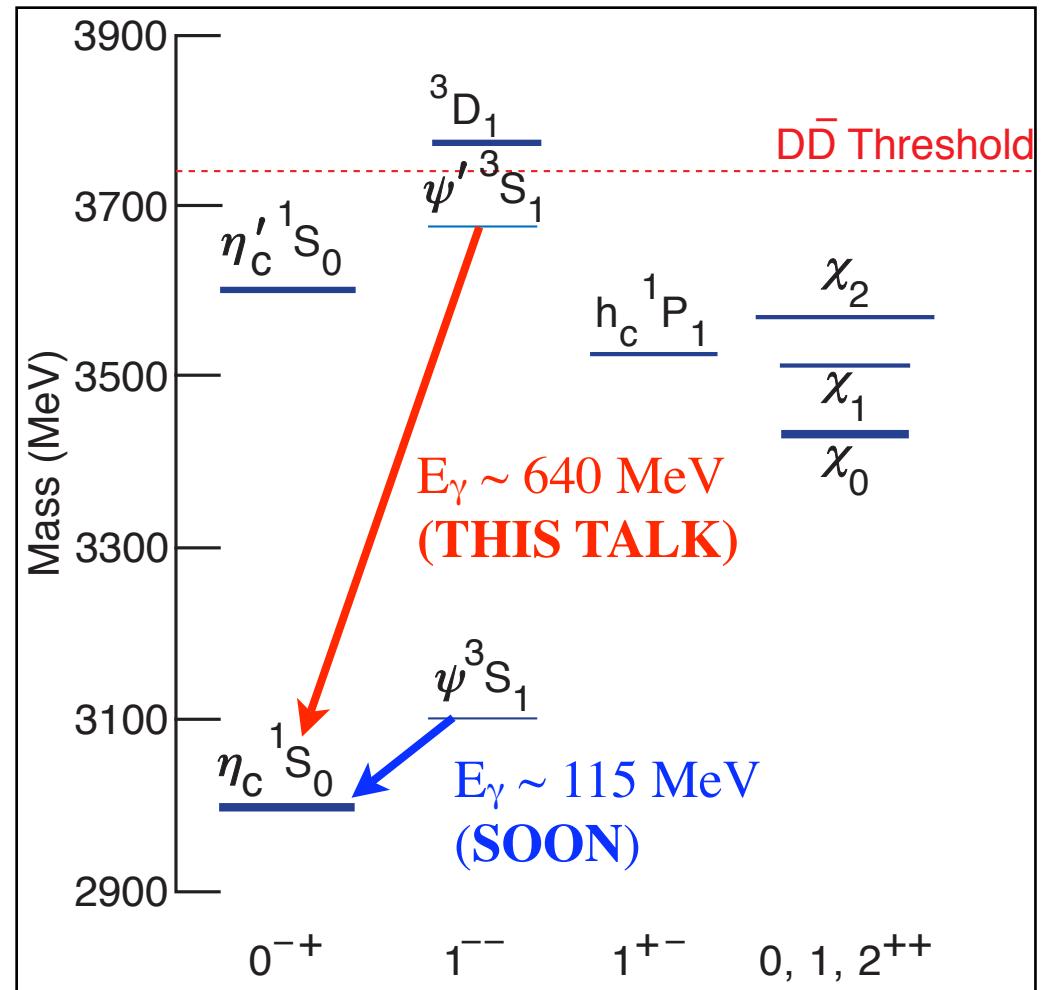
Next (*last*) run will be at 4.17 GeV



**Watch for many new results from the 27M  $\psi(2S)$  sample.**

# The Importance of $\psi(1S,2S) \rightarrow \gamma\eta_c$ (I)

- They serve as a laboratory for the study of relativistic and non-perturbative effects in QCD. (*e.g., why is  $B(J/\psi \rightarrow \gamma\eta_c)$  small?*)
- The first Lattice QCD calculations were recently performed at Jefferson Laboratory. (**PRD73, 074507 (2006)**)
- There are few previous measurements:
  - Crystal Ball (**PRD34, 711 (1986)**):
    - $B(J/\psi \rightarrow \gamma\eta_c) = 1.3 \pm 0.4 \%$
    - $B(\psi(2S) \rightarrow \gamma\eta_c) = (2.8 \pm 0.6) \times 10^{-3}$
  - CLEO (**PRD70, 112002 (2004)**):
    - $B(\psi(2S) \rightarrow \gamma\eta_c) = (3.3 \pm 0.4 \pm 0.6 \pm 0.2) \times 10^{-3}$



# The Importance of $\psi(1S,2S) \rightarrow \gamma\eta_c$ (II)

Citation: W.-M. Yao et al. (Particle Data Group), J. Phys. G **33**, 1 (2006) and 2007 partial update for edition 2008 (URL: <http://pdg.lbl.gov>)

- ALL  $\eta_c$  branching fractions are currently tied to  $\psi(1S,2S) \rightarrow \gamma\eta_c$ .  
(example page from PDG 2007) →

- These transitions (especially using exclusive  $\eta_c$  decays) are also a source of  $\eta_c$  mass and width measurements.  
(more later)

35 The quoted branching ratios use  $B(J/\psi(1S) \rightarrow \gamma\eta_c(1S)) = 0.0127 \pm 0.0036$ . Where relevant, the error in this branching ratio is treated as a common systematic in computing averages.

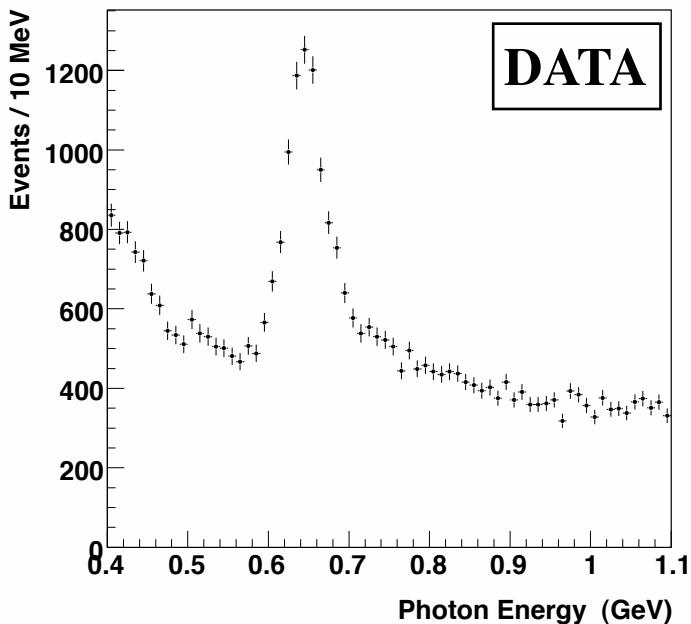
36 ABLIKIM 06A reports  $[B(\eta_c(1S) \rightarrow K^{*0}\bar{K}^{*0}\pi^+\pi^-) \times B(J/\psi(1S) \rightarrow \gamma\eta_c(1S))] = (1.91 \pm 0.64 \pm 0.48) \times 10^{-4}$ . We divide by our best value  $B(J/\psi(1S) \rightarrow \gamma\eta_c(1S)) = (1.3 \pm 0.4) \times 10^{-2}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

37 Using  $B(B^+ \rightarrow \eta_c K^+) = (1.25 \pm 0.12^{+0.10}_{-0.12}) \times 10^{-3}$  from FANG 03 and  $B(\eta_c \rightarrow K\bar{K}\pi) = (5.5 \pm 1.7) \times 10^{-2}$ .

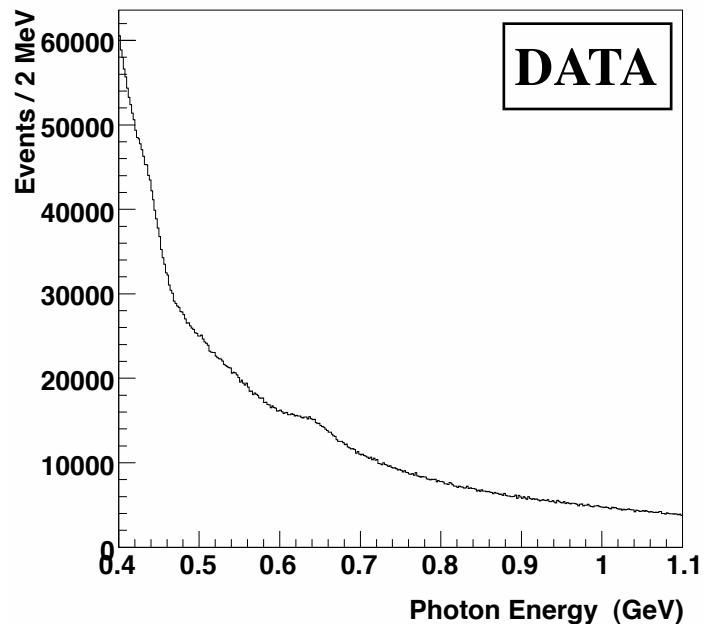
$\Gamma(\rho\rho)/\Gamma_{\text{total}}$	$\Gamma_2/\Gamma$
<u>VALUE (units <math>10^{-3}</math>)</u>	<u>CL%</u>
<b>20 <math>\pm</math> 7 OUR EVALUATION</b>	
12.6 $\pm$ 3.8 $\pm$ 5.1	72
26.0 $\pm$ 2.4 $\pm$ 8.8	113
23.6 $\pm$ 10.6 $\pm$ 8.2	32
<14	90
<b>18 <math>\pm</math> 5 OUR AVERAGE</b>	
35 ABLIKIM	05L BES2
	$J/\psi \rightarrow \pi^+\pi^-\pi^+\pi^-\gamma$
35 BISELLO	91 DM2
	$J/\psi \rightarrow \gamma\rho^0\rho^0$
35 BISELLO	91 DM2
	$J/\psi \rightarrow \gamma\rho^+\rho^-$
• • • We do not use the following data for averages, fits, limits, etc. • • •	
35 BALTRUSAIT..86	MRK3
	$J/\psi \rightarrow \eta_c\gamma$
$\Gamma(K^*(892)^0 K^- \pi^+ + \text{c.c.})/\Gamma_{\text{total}}$	$\Gamma_3/\Gamma$
<u>VALUE</u>	<u>EVTS</u>
<b>0.02 <math>\pm</math> 0.007</b>	63
35 BALTRUSAIT..86	MRK3
	$J/\psi \rightarrow \eta_c\gamma$
$\Gamma(K^*(892)\bar{K}^*(892))/\Gamma_{\text{total}}$	$\Gamma_4/\Gamma$
<u>VALUE (units <math>10^{-4}</math>)</u>	<u>EVTS</u>
<b>92 <math>\pm</math> 34 OUR EVALUATION</b>	
91 $\pm$ 26 OUR AVERAGE	
108 $\pm$ 25 $\pm$ 44	60
82 $\pm$ 28 $\pm$ 27	14
90 $\pm$ 50	9
35 ABLIKIM	05L BES2
35 BISELLO	91 DM2
35 BALTRUSAIT..86	MRK3
	$J/\psi \rightarrow K^+K^-\pi^+\pi^-\gamma$
	$e^+e^- \rightarrow \gamma K^+K^-\pi^+\pi^-$
	$J/\psi \rightarrow \eta_c\gamma$
$\Gamma(K^{*0}\bar{K}^{*0}\pi^+\pi^-)/\Gamma_{\text{total}}$	$\Gamma_5/\Gamma$
<u>VALUE (units <math>10^{-4}</math>)</u>	<u>EVTS</u>
<b>150. <math>\pm</math> 63. <math>\pm</math> 43.</b>	45
36 ABLIKIM	06A BES2
	$J/\psi \rightarrow K^{*0}\bar{K}^{*0}\pi^+\pi^-$
$\Gamma(\phi K^+ K^-)/\Gamma_{\text{total}}$	$\Gamma_6/\Gamma$
<u>VALUE (units <math>10^{-3}</math>)</u>	<u>EVTS</u>
<b>2.9 <math>\pm</math> 0.9 <math>\pm</math> 1.1</b>	14.1 $\pm$ 4.4
37 HUANG	03 BELL
	$B^+ \rightarrow (\phi K^+ K^-) K^+$
$\Gamma(\phi\phi)/\Gamma_{\text{total}}$	$\Gamma_7/\Gamma$
<u>VALUE (units <math>10^{-4}</math>)</u>	<u>EVTS</u>
<b>27 <math>\pm</math> 9 OUR EVALUATION</b>	
<b>27 <math>\pm</math> 5 OUR AVERAGE</b>	
25.3 $\pm$ 5.1 $\pm$ 9.1	72
26 $\pm$ 9	357 $\pm$ 64
18 $\pm$ 8 $\pm$ 7	7.0 $\pm$ 3.0
31 $\pm$ 7 $\pm$ 10	19
30 $\pm$ 18 $\pm$ 10	5
74 $\pm$ 18 $\pm$ 24	80
67 $\pm$ 21 $\pm$ 24	35 BAI
	90B MRK3
	90B MRK3
	$J/\psi \rightarrow K^+K^-K^+K^-$
	$J/\psi \rightarrow \gamma K^+K^-K^+K^-$
	$B^+ \rightarrow (\phi\phi) K^+$
	$J/\psi \rightarrow \gamma K^+K^-K^+K^-$
	$J/\psi \rightarrow \gamma K^+K^-K^0 S_K^0$
	$J/\psi \rightarrow \gamma K^+K^-K^0 S_L^0$
	$J/\psi \rightarrow \gamma K^+K^-K^0 S_K^0$
	$J/\psi \rightarrow \gamma K^+K^-K^0 S_L^0$

# This Talk: $\psi(2S) \rightarrow \gamma \eta_c$

1. Measure the line shape (empirically) using **exclusive** decays of the  $\eta_c$ .



2. Use this shape to fit the **inclusive** photon energy spectrum from  $\psi(2S)$ .



*We find a non-trivial and unexpected  $\eta_c$  line-shape.*

- ⇒ Prevents (for now)  $\eta_c$  mass and width extraction.
- ⇒ Forces us to resort to empirical methods.

*We measure:*

$$B(\psi(2S) \rightarrow \gamma \eta_c) = (4.02 \pm 0.11 \pm 0.52) \times 10^{-3}$$

(CLEO preliminary)

# I. The $\eta_c$ Line Shape in $\psi(2S) \rightarrow \gamma\eta_c$ using Exclusive $\eta_c$ Decays

# Exclusive $\psi(2S) \rightarrow \gamma\eta_c$ Reconstruction

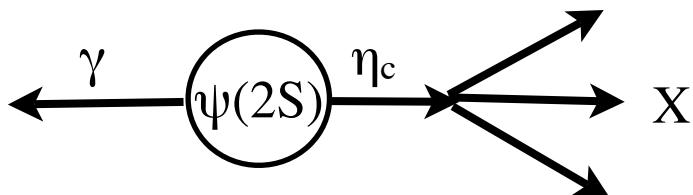
## $\eta_c$ Decay Modes

Decay Mode	Branching Fraction (PDG 2007)	Notes
$\pi^+\pi^-\pi^+\pi^-$	$(1.2 \pm 0.3)\%$	
$\pi^+\pi^-\pi^0\pi^0$	NEW	
$\pi^+\pi^-\pi^+\pi^-\pi^+\pi^-$	$(2.0 \pm 0.7)\%$	
$\pi^+\pi^-\pi^+\pi^-\pi^0\pi^0$	NEW	
$K^+K_S\pi^- + \text{c.c.}$	$1/3 \times (7.0 \pm 1.2)\%$	based on $KK\pi$
$K^+K^-\pi^0$	$1/6 \times (7.0 \pm 1.2)\%$	based on $KK\pi$
$K^+K^-\pi^+\pi^-$	$(1.5 \pm 0.6)\%$	
$K^+K_S\pi^+\pi^-\pi^- + \text{c.c.}$	NEW	
$K^+K^-\pi^+\pi^-\pi^0$	NEW	
$K^+K^-\pi^+\pi^-\pi^+\pi^-$	$(1.0 \pm 0.4)\%$	
$K^+K^-K^+K^-$	$(0.15 \pm 0.07)\%$	
$\eta_{\gamma\gamma}\pi^+\pi^-$	$2/3 \times 0.39 \times (4.9 \pm 1.8)\%$	based on $\eta\pi\pi$
$\eta_{+-0}\pi^+\pi^-$	$2/3 \times 0.23 \times (4.9 \pm 1.8)\%$	based on $\eta\pi\pi$
$\eta_{\gamma\gamma}\pi^+\pi^-\pi^+\pi^-$	$2/3 \times 0.39 \times (4.1 \pm 1.7)\%$	based on $\eta'\pi\pi$
$\eta_{+-0}\pi^+\pi^-\pi^+\pi^-$	$2/3 \times 0.23 \times (4.1 \pm 1.7)\%$	based on $\eta'\pi\pi$

- All modes from the PDG are included (except  $p^+p^-$ ).
- A few new modes were chosen from a comprehensive search.

## Technique:

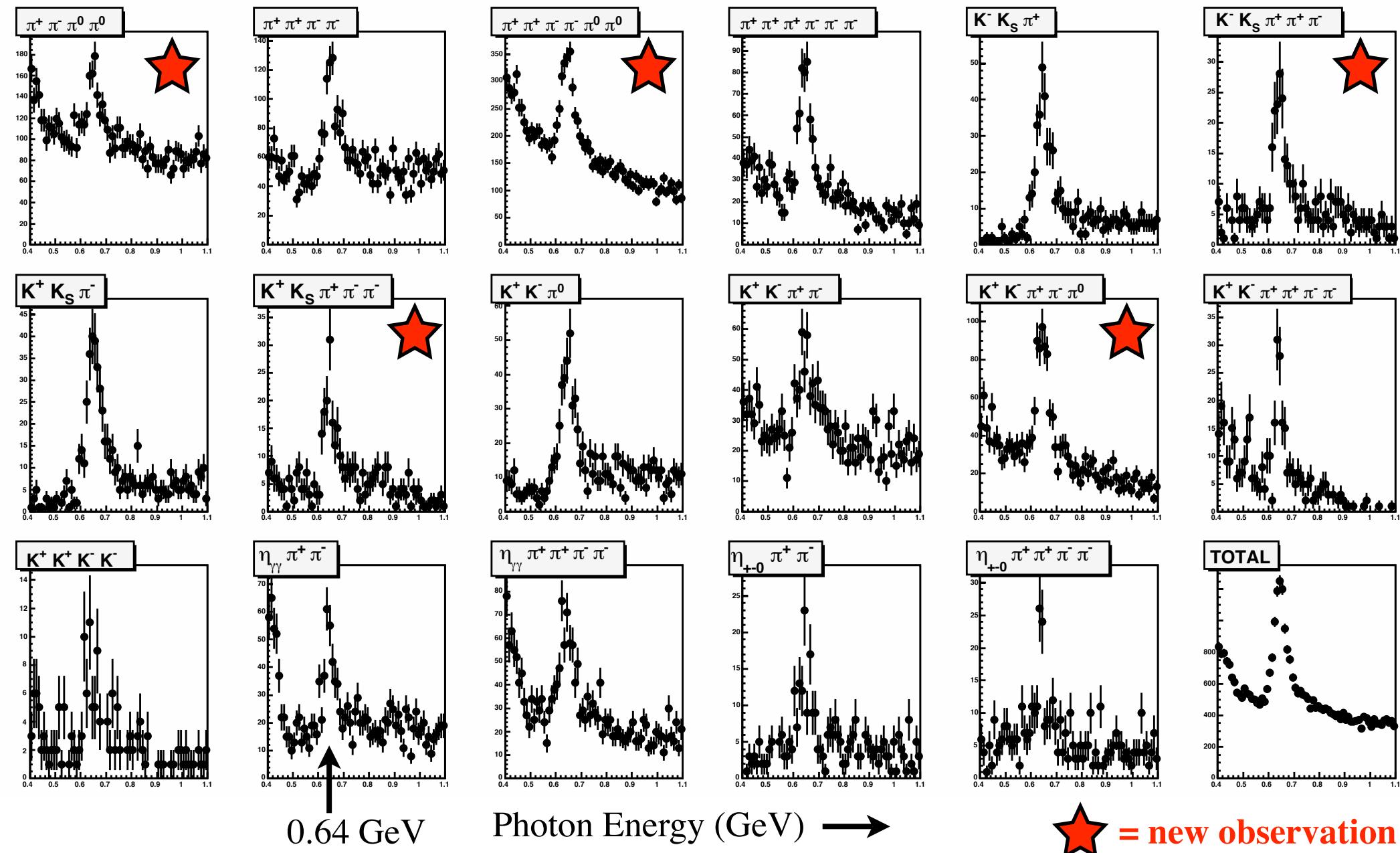
Perform a kinematic fit of  $\gamma X$  to the  $\psi(2S)$  4-momentum. Use  $\chi^2$  to select events.



## Use the measured photon energy:

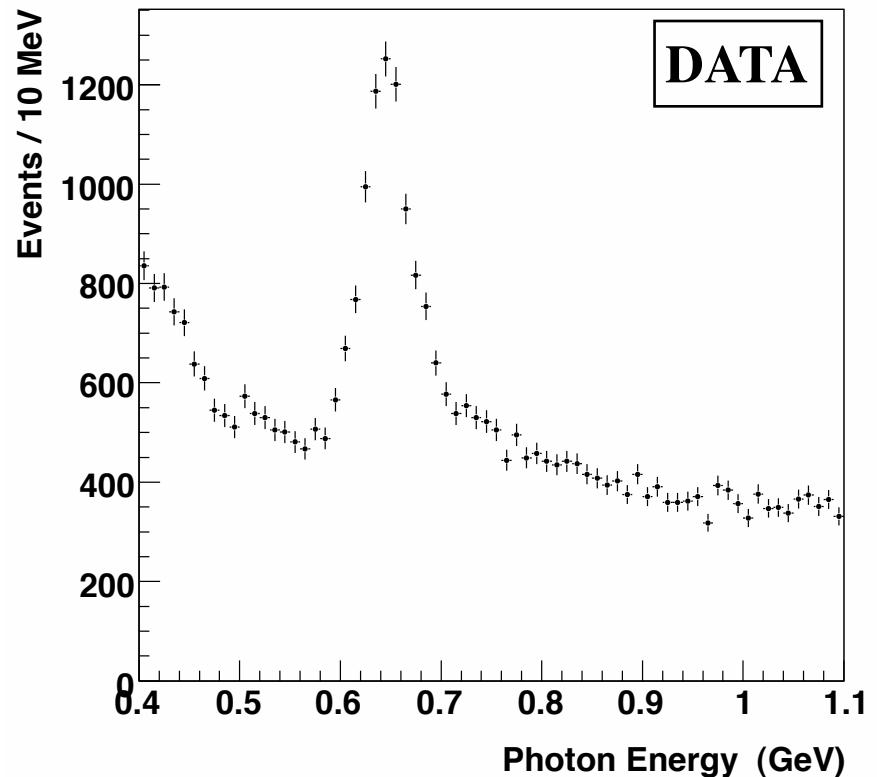
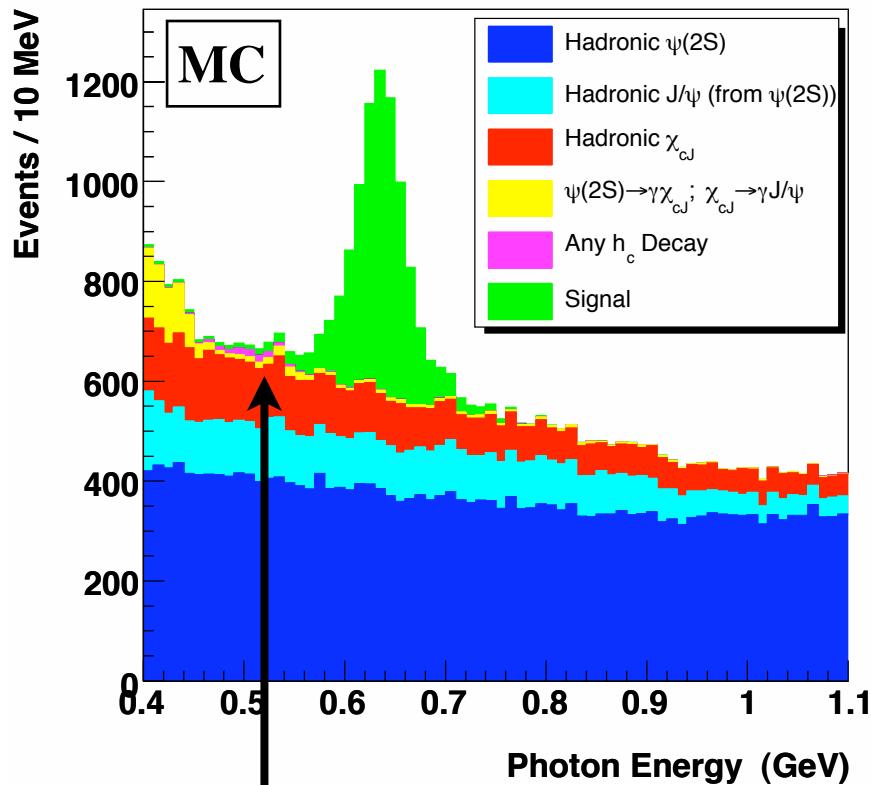
- The resolution (14.6 MeV) is independent of X.
- Modes can be added.
- Modes can be compared to the inclusive spectrum.

# Exclusive $\psi(2S) \rightarrow \gamma \eta_c$ Signals



# Sum of Exclusive $\eta_c$ Modes

Measured Photon Energy



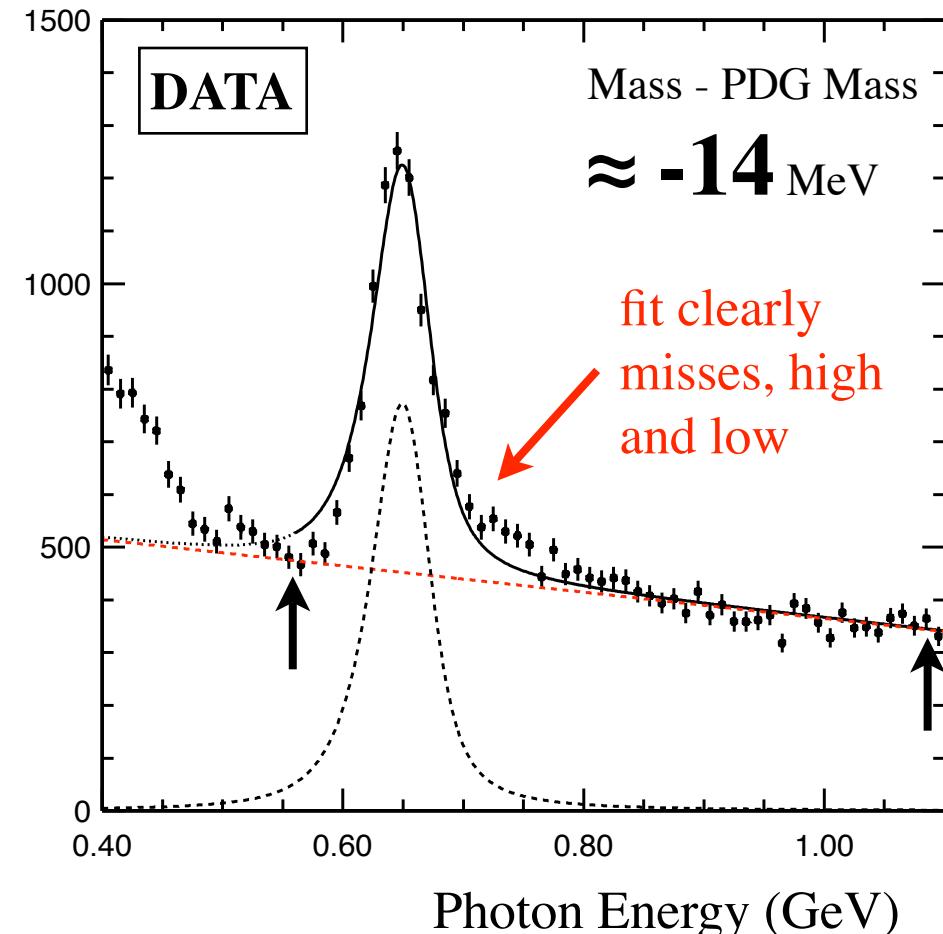
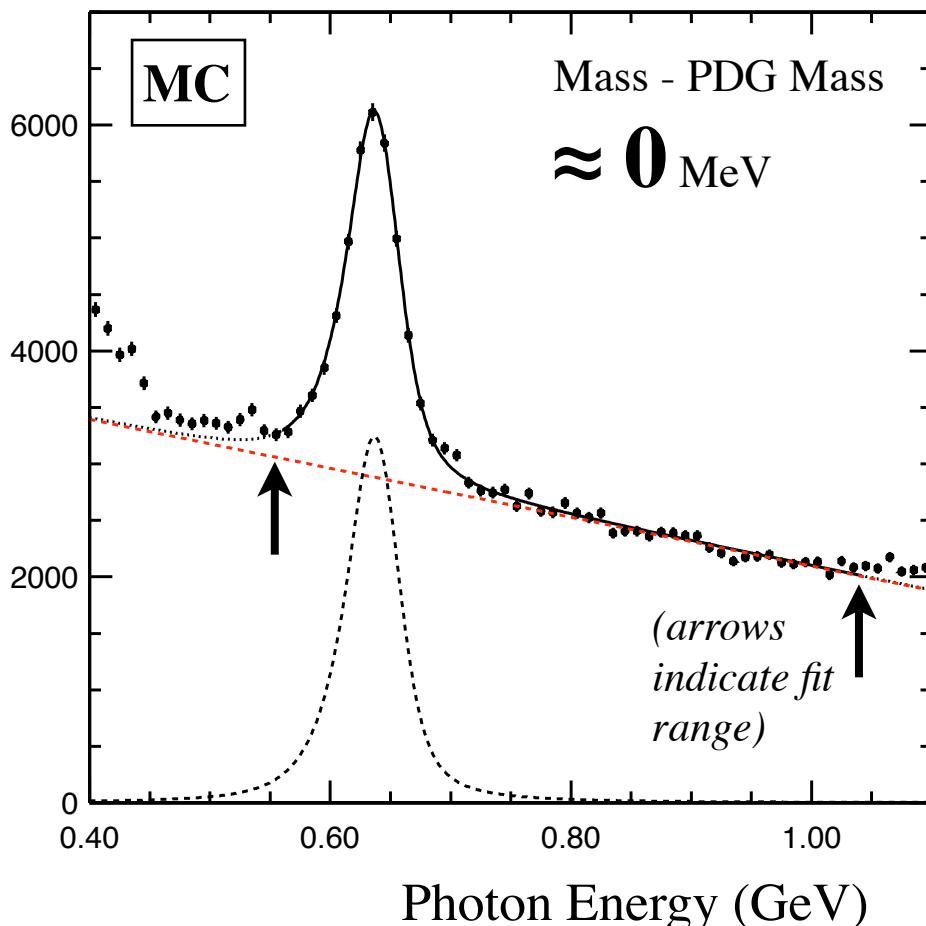
### 3 peaking backgrounds:

- $\psi(2S) \rightarrow \gamma \chi_{cJ}; \chi_{cJ} \rightarrow \gamma J/\psi$
- $\psi(2S) \rightarrow \pi^0 J/\psi$
- $\psi(2S) \rightarrow \pi^0 h_c; h_c \rightarrow \gamma \eta_c$

1. Good, qualitative agreement between data and MC.
2. Smooth backgrounds above 550 MeV.
3. Small peaking backgrounds around 500 MeV.
4. Signal shapes are apparently different...

# Fits Using a Non-Relativistic BW

1. Try a non-relativistic Breit-Wigner convoluted with a resolution function (Crystal Ball) with parameters fixed from signal Monte Carlo.



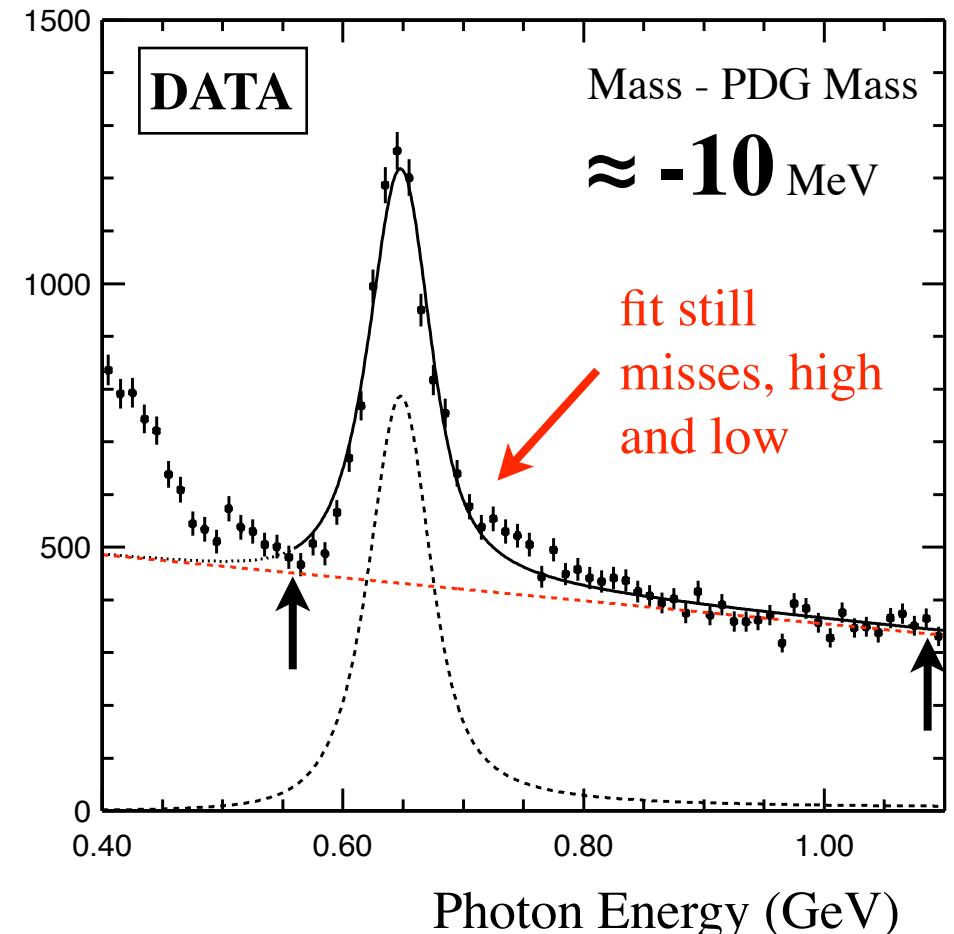
# Fit Using a BW $\times$ $E_\gamma^3$

2. Try a Breit-Wigner with an  $E_\gamma^3$  term convoluted with a resolution function (Crystal Ball) with parameters fixed from signal Monte Carlo.

A non-relativistic calculation of the partial width has an  $E_\gamma^3$  dependence...

$$\Gamma_{n^3S_1 \rightarrow \gamma n'{}^1S_0} = \frac{4}{3} \alpha e_Q^2 \frac{k_\gamma^3}{m^2} \left| \int_0^\infty dr r^2 R_{n'0}(r) R_{n0}(r) j_0\left(\frac{k_\gamma r}{2}\right) \right|^2$$

... assuming no energy dependence in the matrix element.



# Fit Using a BW $\times$ $E_\gamma^7$

3. Try a Breit-Wigner with an  $E_\gamma^7$  term convoluted with a resolution function (Crystal Ball) with parameters fixed from signal Monte Carlo.

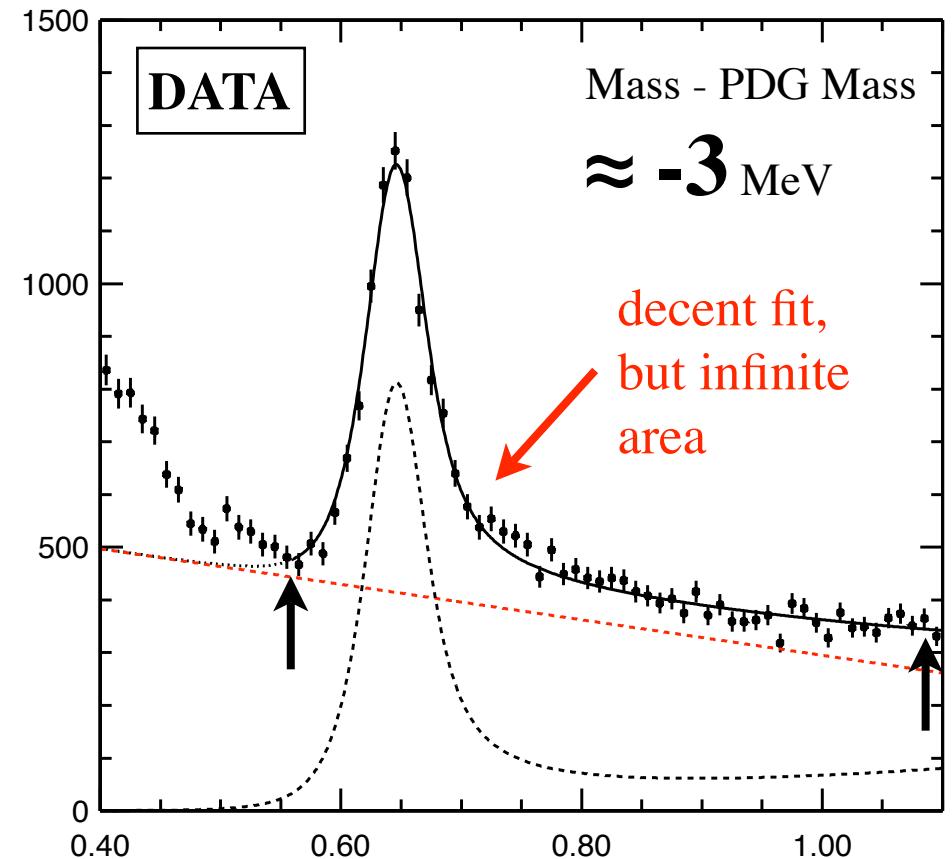
A non-relativistic calculation of the partial width has an  $E_\gamma^3$  dependence:

$$\Gamma_{n^3S_1 \rightarrow \gamma n'{}^1S_0} = \frac{4}{3} \alpha e_Q^2 \frac{k_\gamma^3}{m^2} \left| \int_0^\infty dr r^2 R_{n'0}(r) R_{n0}(r) j_0\left(\frac{k_\gamma r}{2}\right) \right|^2$$

Expanding the spherical Bessel function:

$$j_0\left(\frac{k_\gamma r}{2}\right) = 1 - \frac{(k_\gamma r)^2}{24} + \dots$$

The first order term vanishes when  $n \neq n'$ .  
The second term gives another  $E_\gamma^4$ .



**⇒ We are yet to find an adequate, physically meaningful description of the line-shape.**

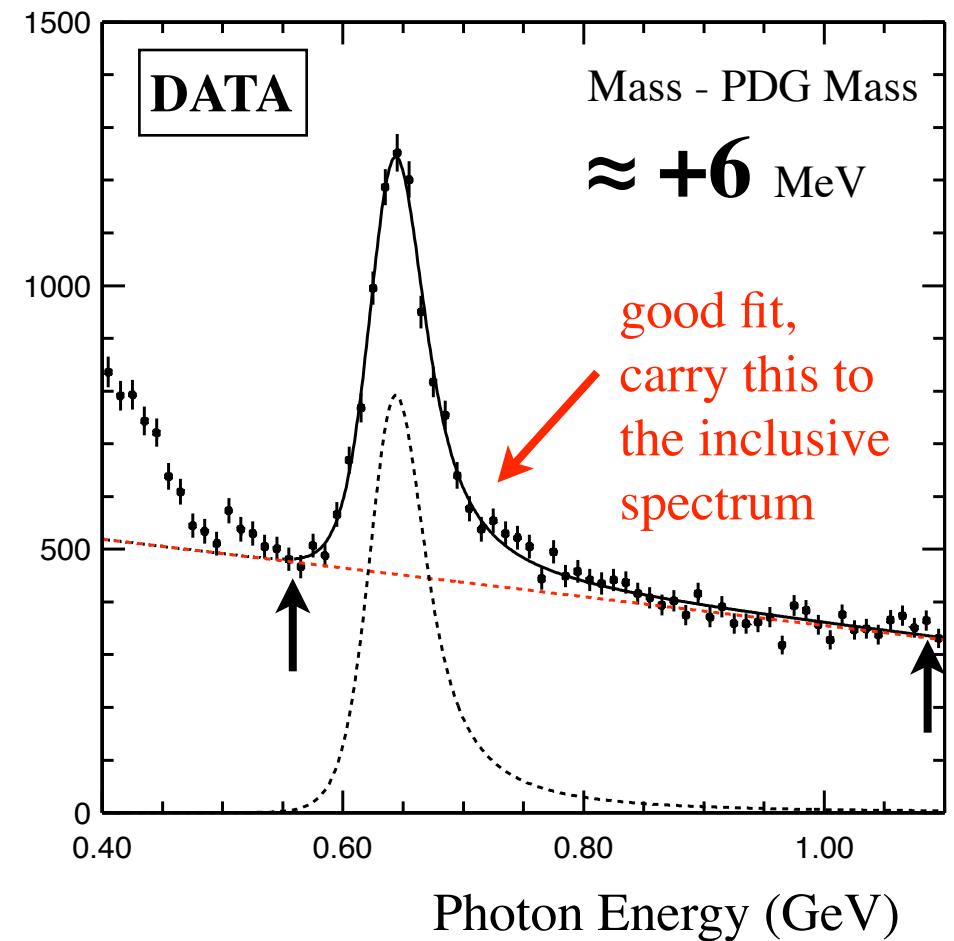
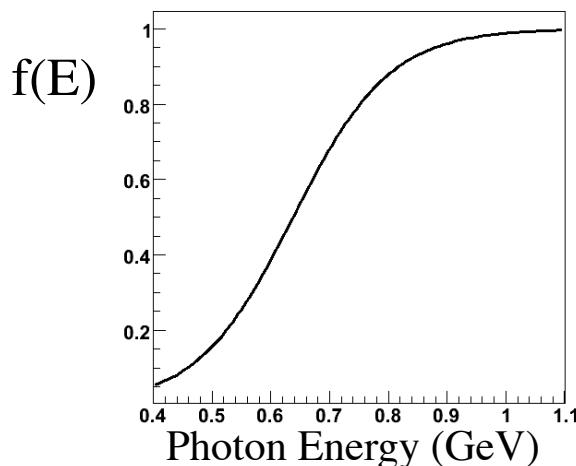
# Fit Using a BW $\times$ f(E)

4. Try a Breit-Wigner  $\times$  f(E), where f(E) is an empirical function, again convoluted with a resolution function from signal Monte Carlo.

f(E) is an empirical function,  
i.e., no physics inspiration:

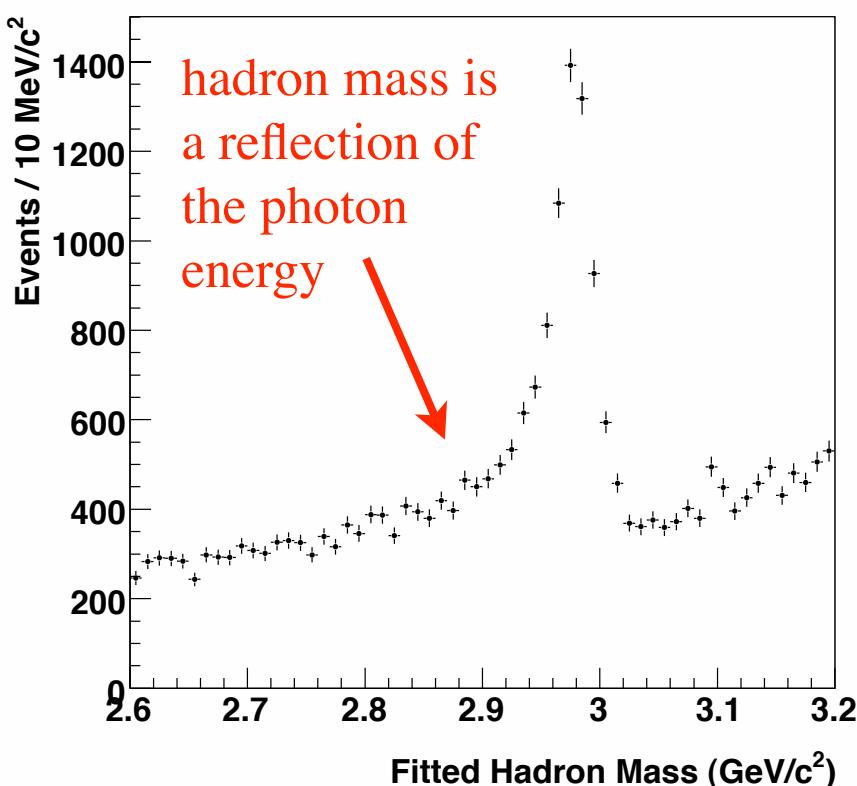
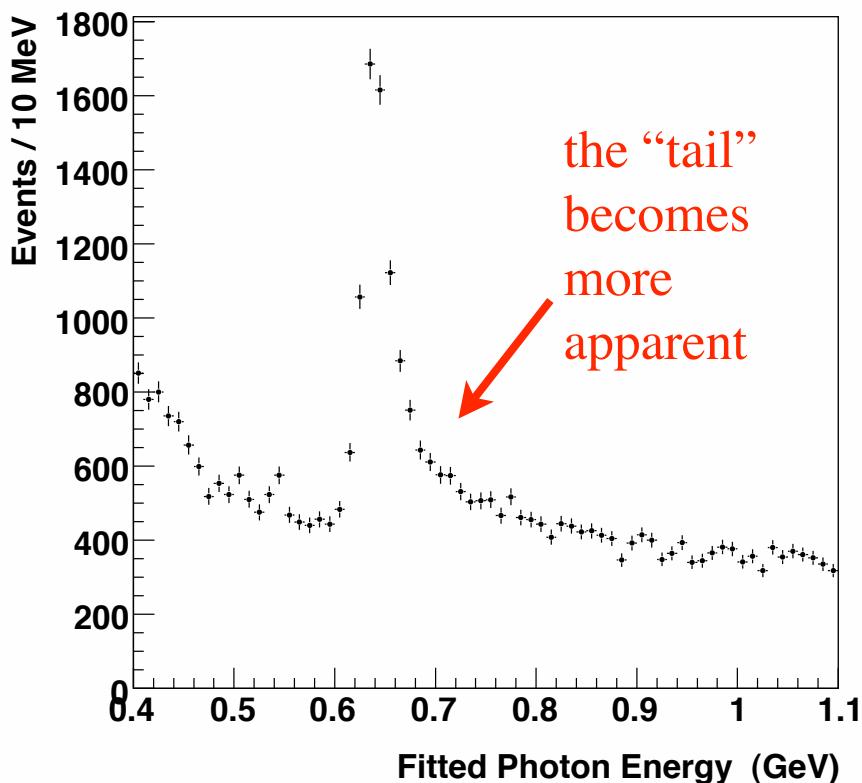
$$f(E) = \frac{1}{1 + e^{\frac{E_0 - E}{2\Gamma}}}$$

where  $E_0$  and  $\Gamma$  are BW parameters.



# Checks (I): Sharpening the Resolution with a Kinematic Fit

*Constrain particle 4-momenta in  $\psi(2S) \rightarrow \gamma X$  to the 4-momentum of the  $\psi(2S)$ .*



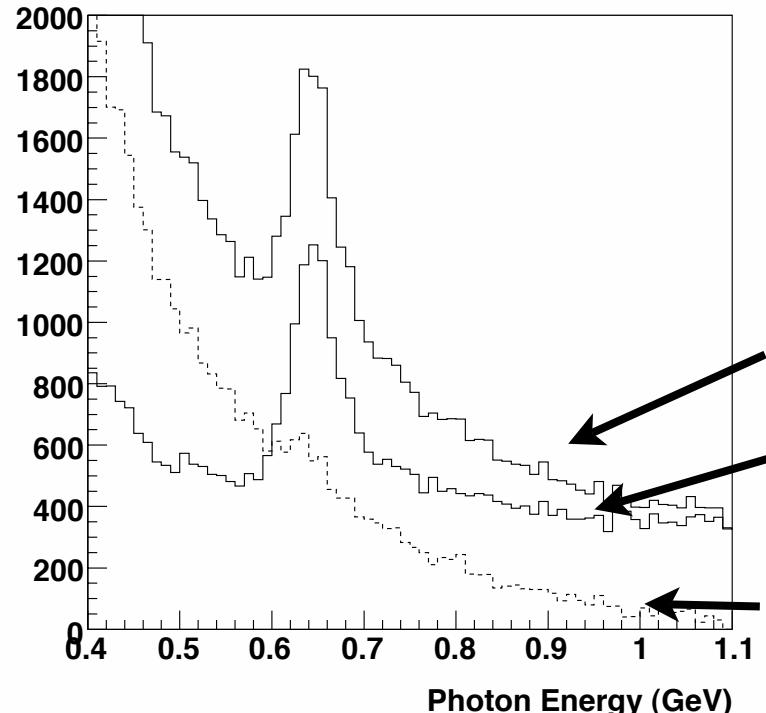
# Checks (II): Artifact of Kinematic Fitting?

Replace the  $\chi^2$  cut with cuts on total mass and hadronic recoil mass (i.e. photon mass).

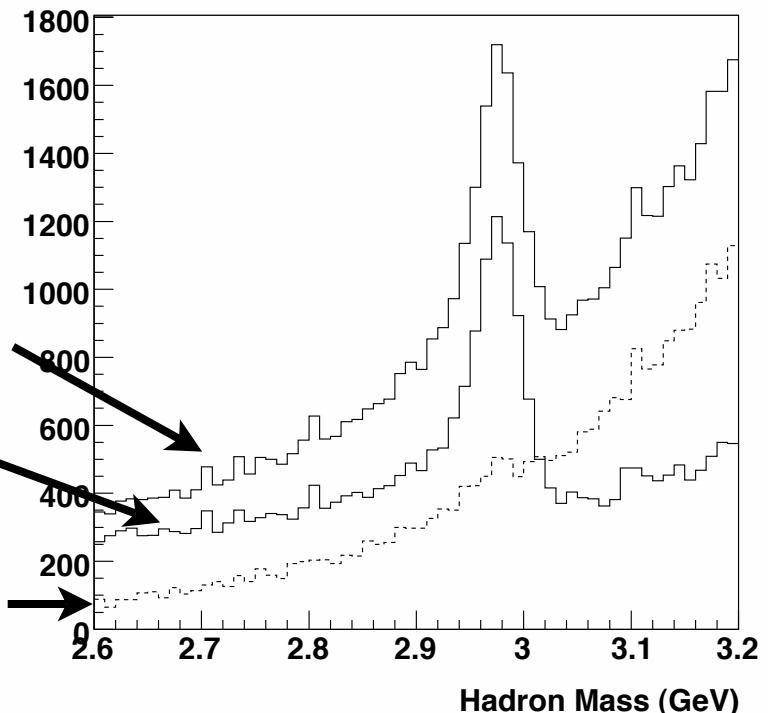
*Tail appears independently in measured photon energy and measured mass.*

- not an artifact of kinematic fitting
- not something peculiar to  $\gamma$  measurement
- not something peculiar to tracking

Measured  $\gamma$  energy with and without  $\chi^2$  cut



Measured mass with and without  $\chi^2$  cut

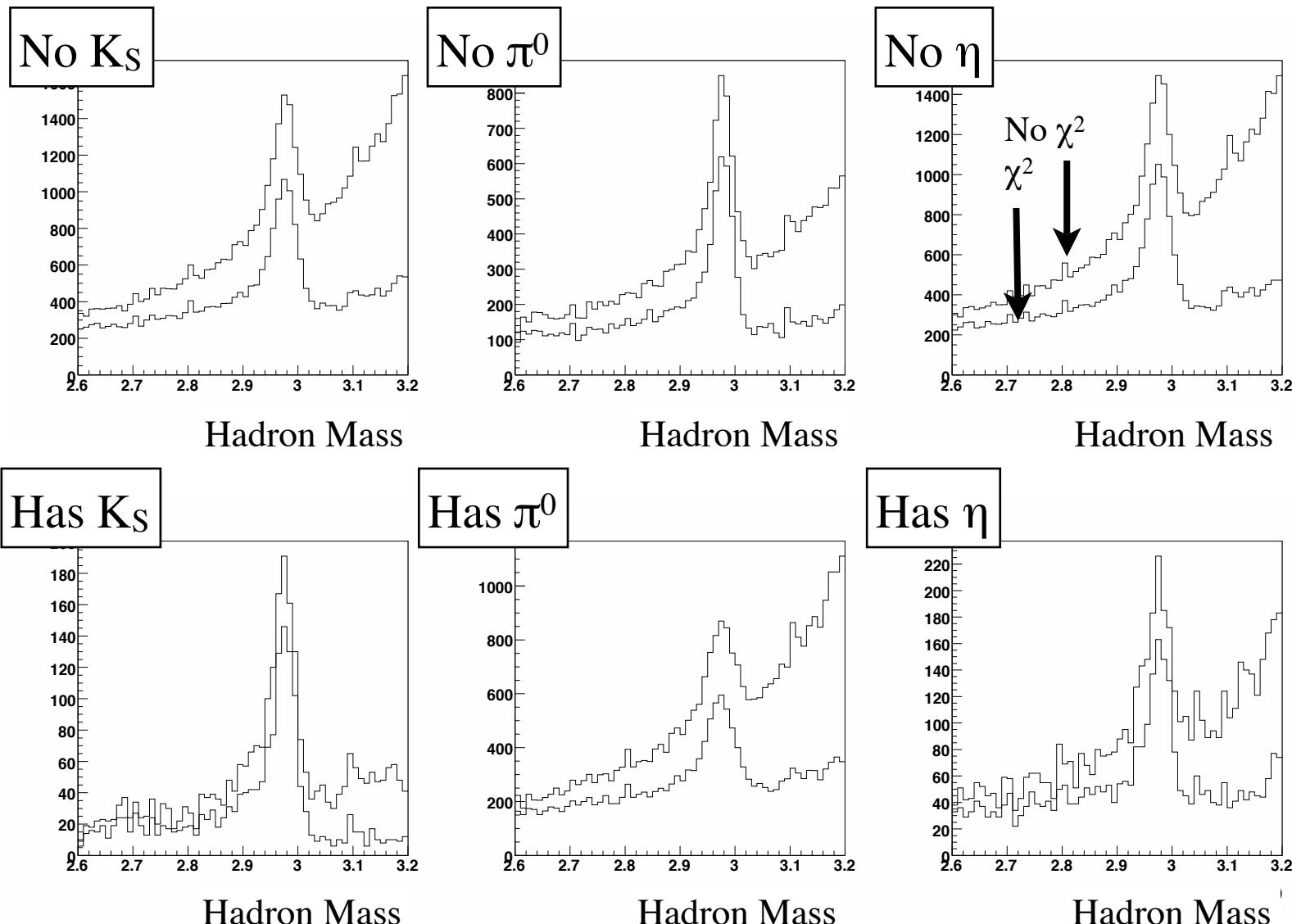


# Checks (III): Is it due to $\pi^0$ , $\eta$ , $K_S$ .... ?

*The tail appears in all combinations of modes, with and without  $\chi^2$  cut.*

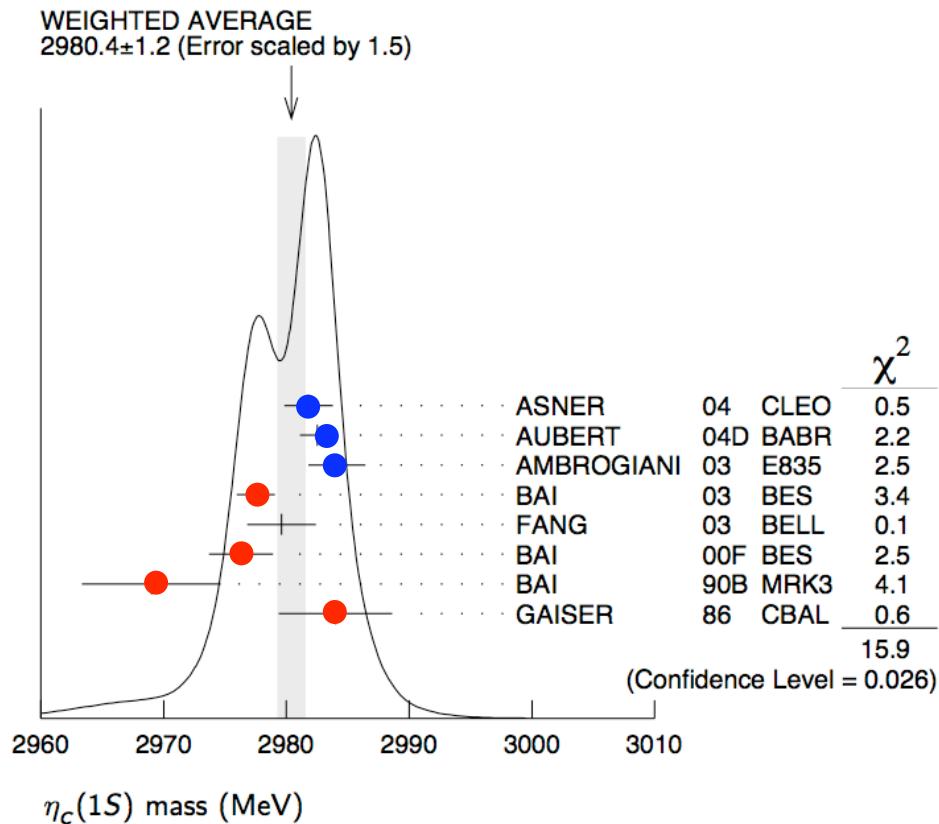
→ e.g. not due to a  
 $K_S$  systematic problem

→ physics bg would  
have to be peculiar

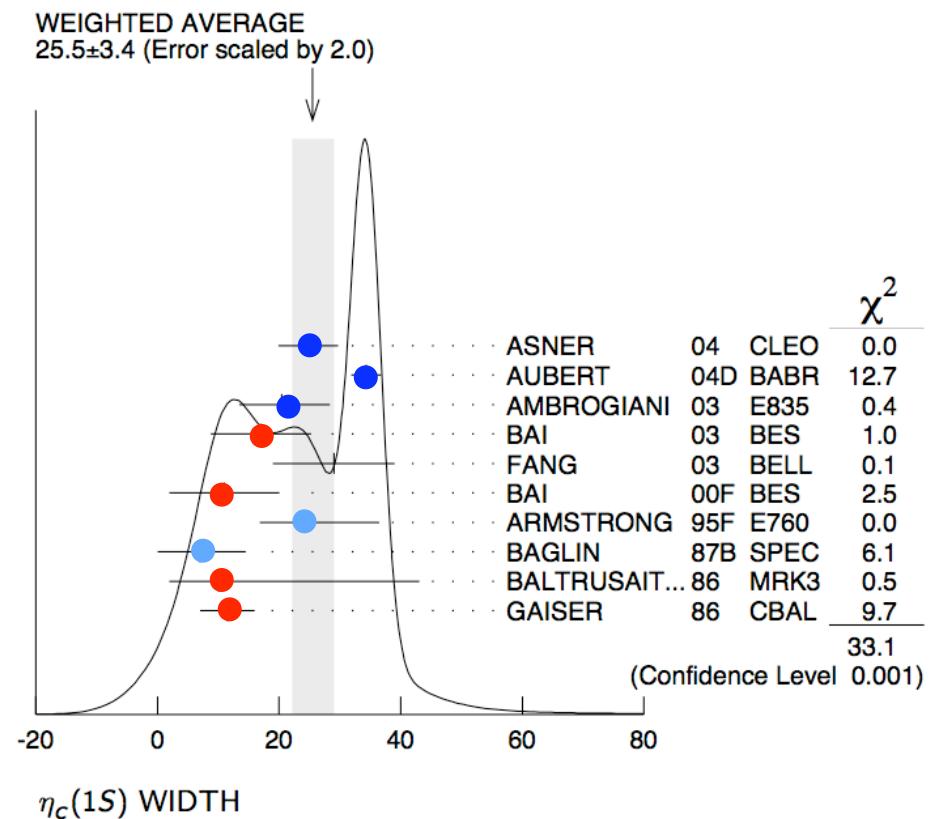


# Line Shape Problems in the Past?

PDG 2006 Mass



PDG 2006 Width

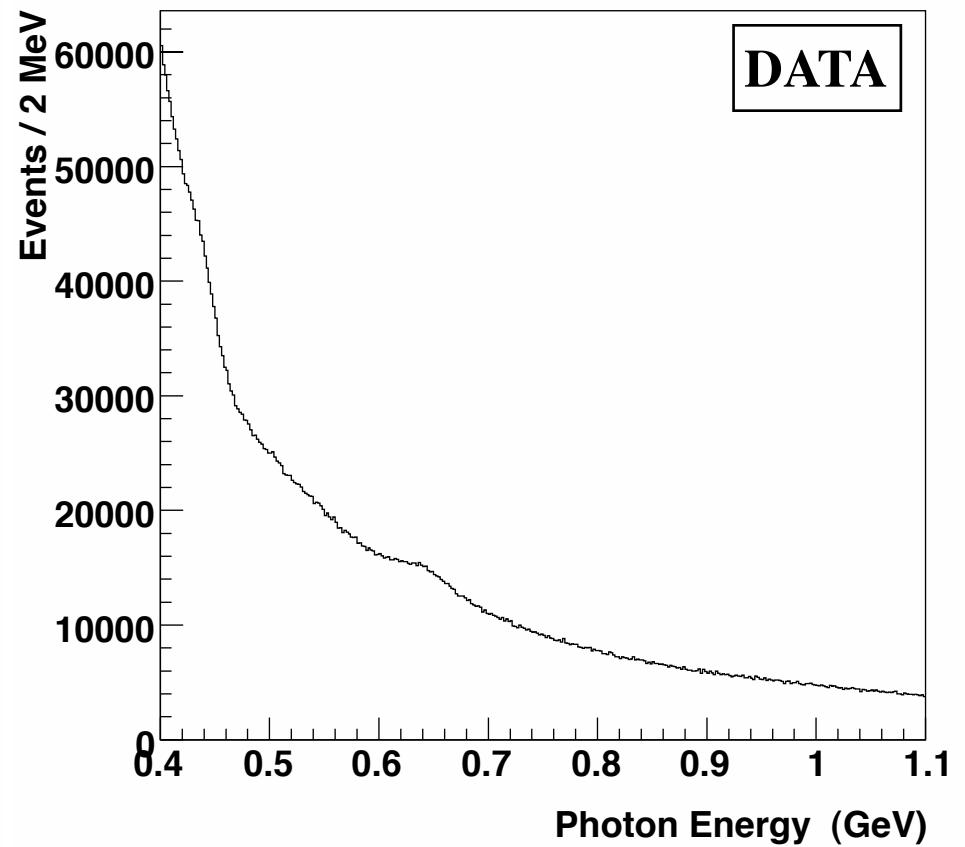
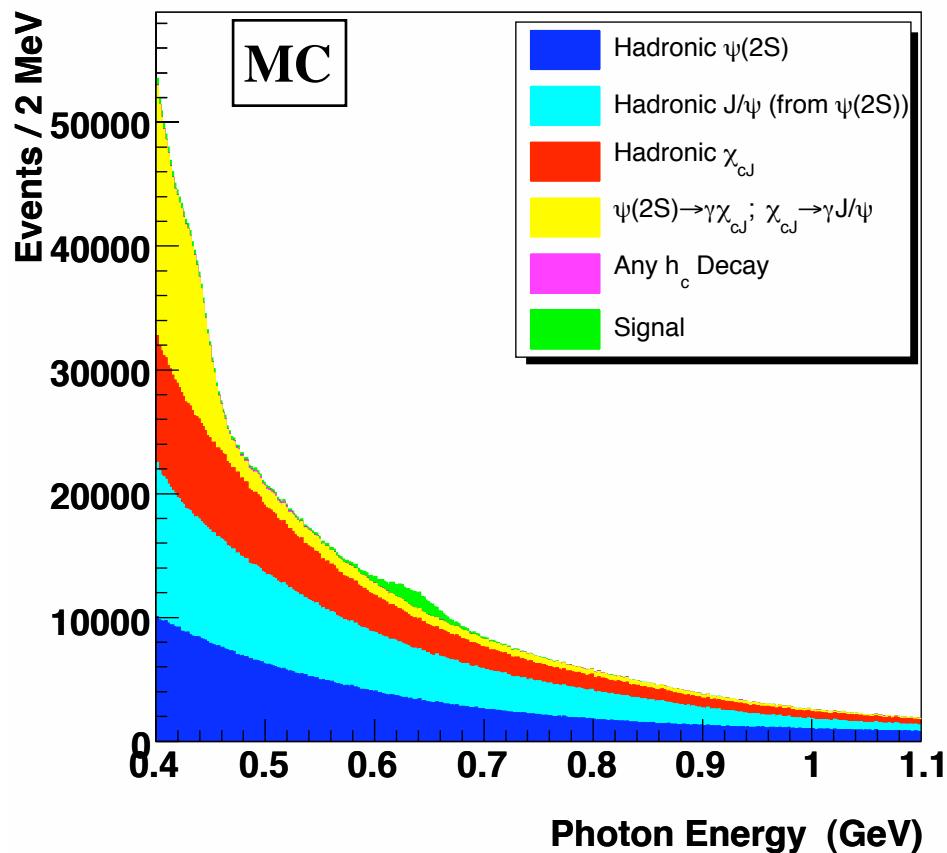


- $\gamma\gamma$  or  $p^+p^-$
- $\gamma\gamma$  or  $p^+p^-$  (used for width, but not mass)
- $\psi(1S,2S) \rightarrow \gamma\eta_c$

## II. Measurement of $B(\psi(2S) \rightarrow \gamma\eta_c)$ from the Inclusive Photon Spectrum

# Inclusive Photon Energy Spectrum From $\psi(2S)$

- Use loose criteria to select photons:
  - Reject events from  $\psi(2S) \rightarrow \pi^+ \pi^- J/\psi$ .
  - Reject photons that pair with another photon to create a  $\pi^0$ .
- Smooth backgrounds, plus nice agreement between MC and data.

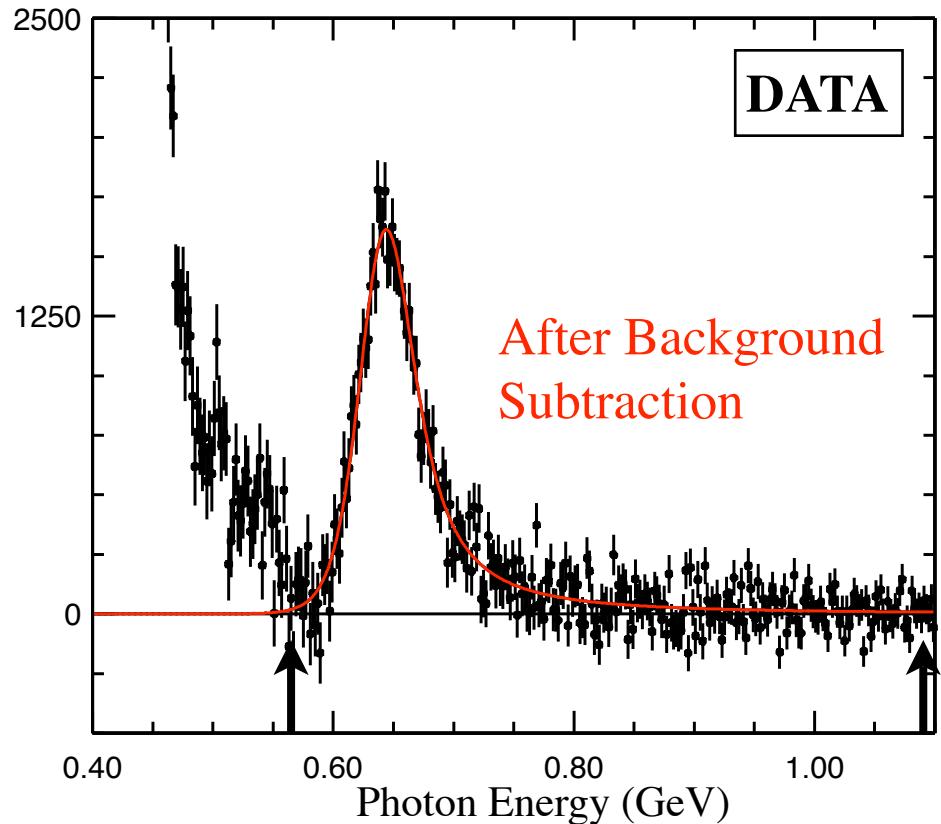
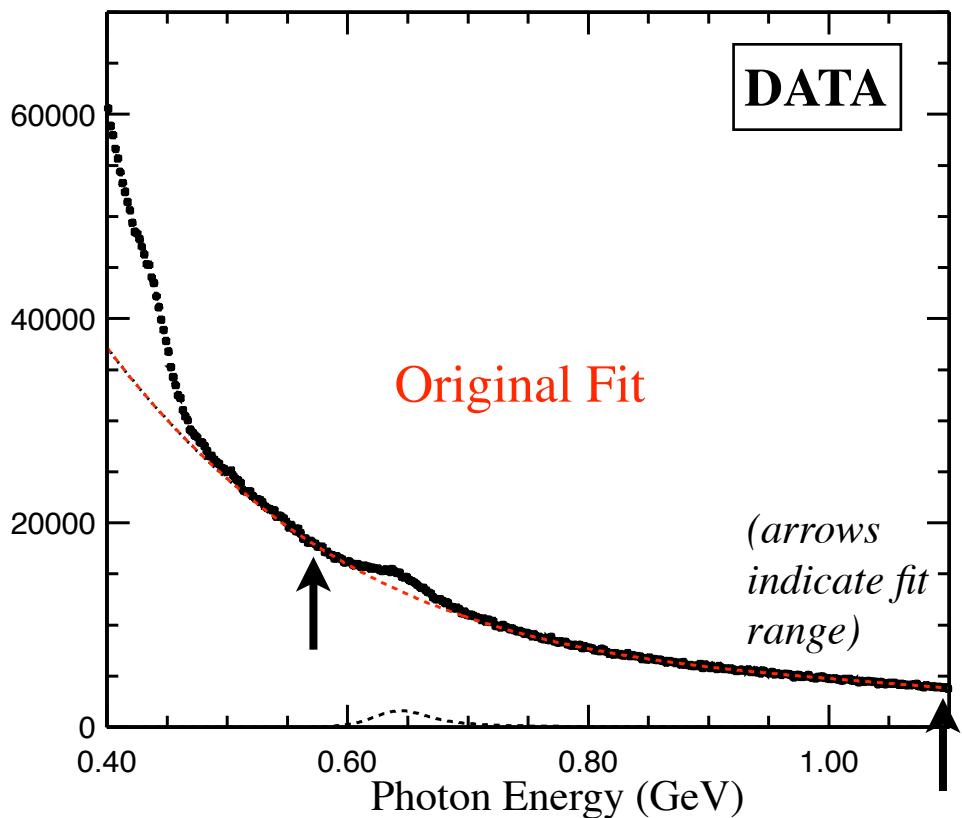


# Fit to the Inclusive Spectrum

*Use a BW  $\times f(E)$  with all parameters fixed from the exclusive fit.*

Measured Events =  $60500 \pm 1700$   
Efficiency = 61.7%  
Number  $\psi(2S)$  = 24.45 million

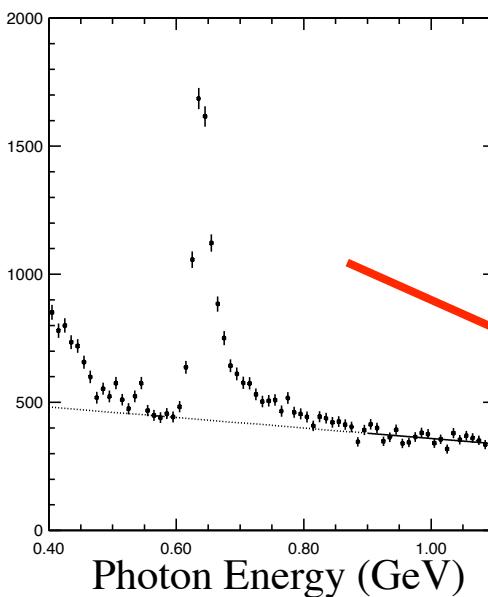
$B(\psi(2S) \rightarrow \gamma \eta_c) = (4.02 \pm 0.11) \times 10^{-3}$   
*(CLEO Preliminary, statistical only)*



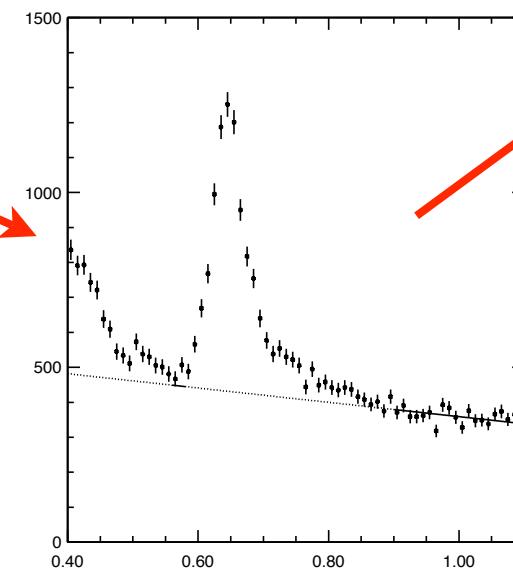
# Evaluating a Fitting Systematic

*Use the exclusive histogram to parameterize the line shape.*

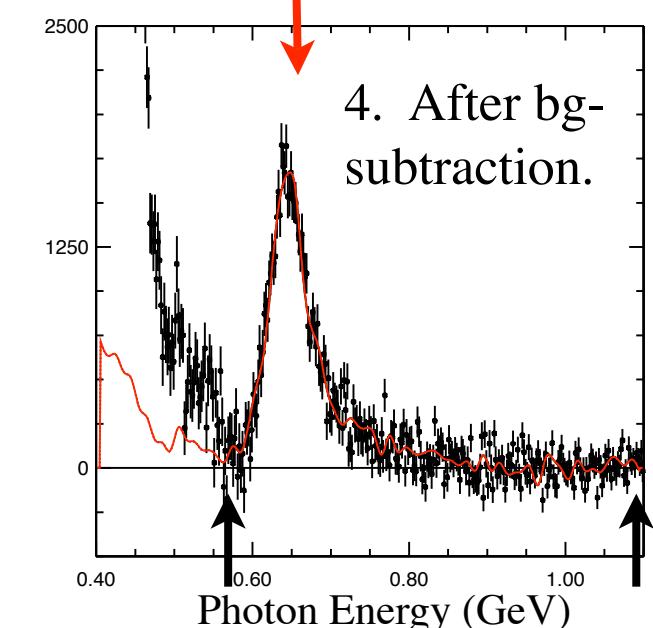
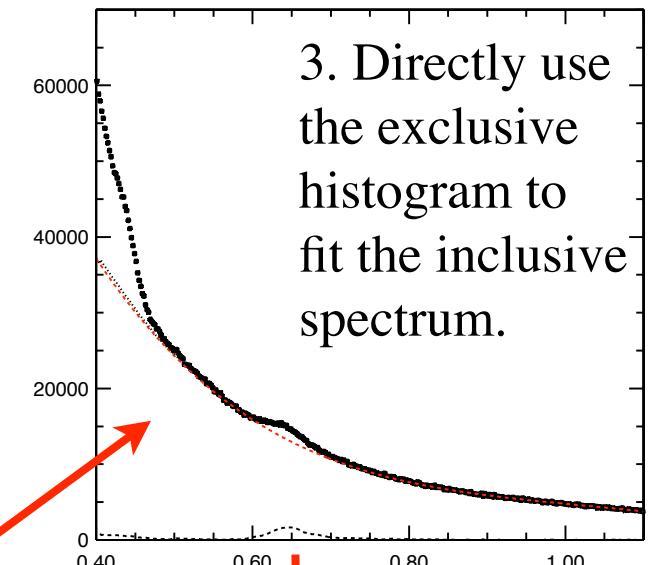
1. Fit the background shape from the fitted photon energy spectrum from exclusive modes.



2. Carry this shape to the measured spectrum and subtract to get a signal shape.



⇒ Vary background shapes and ranges.  
⇒ Assign a 10% systematic error.



3. Directly use the exclusive histogram to fit the inclusive spectrum.

4. After bg-subtraction.

# Other Systematic Errors

Systematic	Value
Line Shape and Fitting	10%
MC Modeling	8%
Photon Efficiency	2%
Number of $\psi(2S)$	2%
Total	13%



*i.e., modeling unknown decays of the  $\eta_c$ .*

CLEO Preliminary:

$$B(\psi(2S) \rightarrow \gamma \eta_c) = (4.02 \pm 0.11 \pm 0.52) \times 10^{-3}$$

# Summary

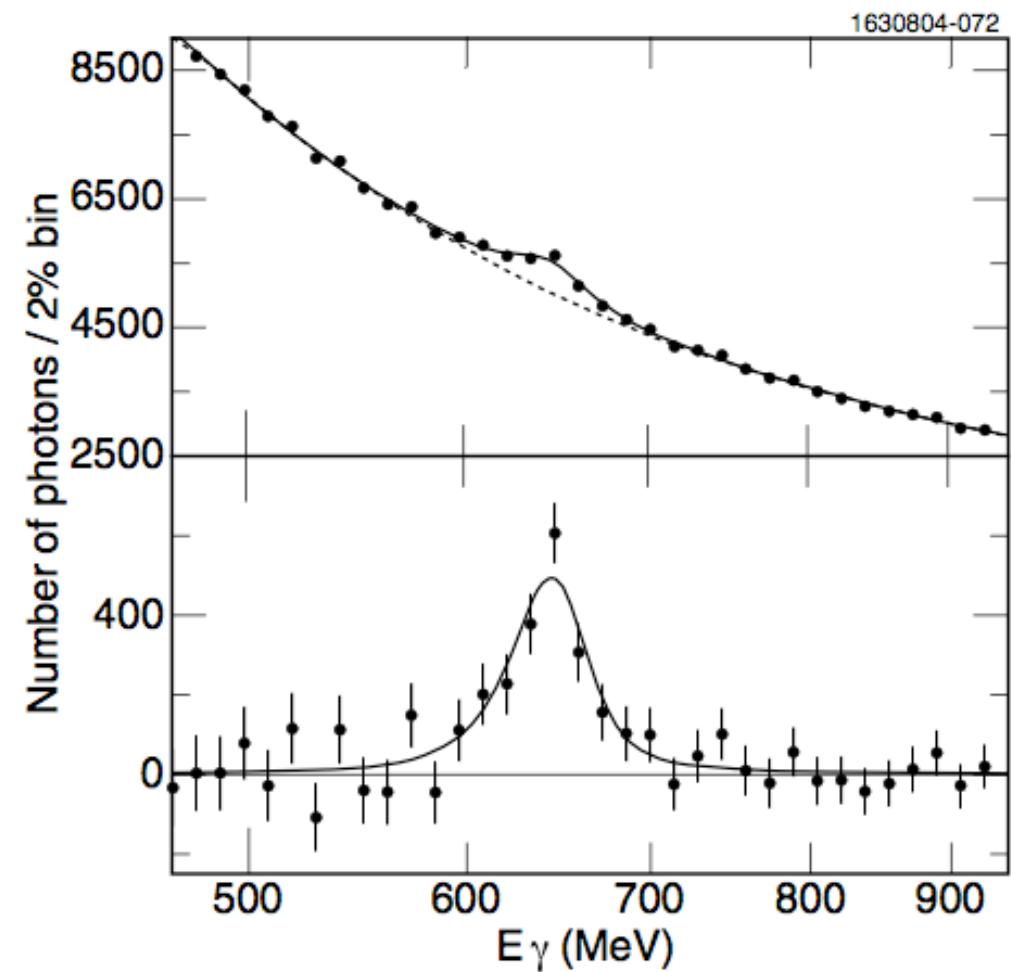
- The  $\eta_c$  line shape in  $\psi(2S) \rightarrow \gamma \eta_c$  is non-trivial.
  - Extracting the mass and width of the  $\eta_c$  from this process requires theoretical help.
  - Perhaps this is one factor causing the wide variation in measurements of the  $\eta_c$  mass and width.
  - We resorted to empirical methods to count events.
- We measure (CLEO preliminary):
  - $B(\psi(2S) \rightarrow \gamma \eta_c) = (4.02 \pm 0.11 \pm 0.52) \times 10^{-3}$
  - Compared to (2004) CLEO's  $(3.3 \pm 0.4 \pm 0.6 \pm 0.2) \times 10^{-3}$  using 1.5 million  $\psi(2S)$  and assuming the PDG  $\eta_c$  width.
  - Compared to (1986) Crystal Ball's  $(2.8 \pm 0.6) \times 10^{-3}$ .
- These techniques will carry over into our measurement of  $B(J/\psi \rightarrow \gamma \eta_c)$ .

# Backup Slides

# $B(\psi(2S) \rightarrow \gamma \eta_c)$ from CLEO (2004)

PHYSICAL REVIEW D **70**, 112002 (2004)

Photon transitions in  $\psi(2S)$  decays to  $\chi_{cJ}(1P)$  and  $\eta_c(1S)$



$$\mathcal{B} = \left( 0.324 + 0.028 \frac{\Gamma_{\eta_c(1S)} - 24.8 \text{ MeV}}{4.9 \text{ MeV}} \right) \%$$

and the errors are

$$(\pm 0.039 \pm 0.055) \frac{\mathcal{B}}{0.324\%} \quad \pm \left( 0.028 \frac{\Delta \Gamma_{\eta_c(1S)}}{4.9 \text{ MeV}} \right) \%$$