

Precision Charm Meson Decays

Leptonic, Semileptonic, Hadronic

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(+ CLEO & BESIII)

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Carnegie Mellon



? Why Charm ?

Previous "wisdom":

charm is a bit boring for flavor physics

Cabibbo-allowed decays dominate: hard to see rare processes

*D Mixing is suppressed in SM & hard to estimate
CP violation suppressed*

*Light enough to make theory difficult (tough for HQET, etc.)
and lots of strong-interaction physics obscuring the weak*



Better wisdom:

Charm is a gift!

B physics very productive... but limited by theory in many cases.

✦ Lattice QCD can help & charm can test it ✦

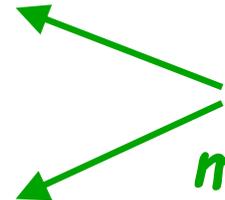
Today's Topics

*Leptonic Decays $D_{(s)} \rightarrow \mu\nu$
to extract decay constants*

*$D \rightarrow Kl\nu, \pi l\nu$
to measure form factors*

*$D^0 \rightarrow K\pi, D^+ \rightarrow K\pi\pi, D_s \rightarrow KK\pi$
normalization from golden-mode branching ratios*

*Testbeds for
modern Lattice QCD*



NOTE:

Precision lifetimes (dominated by FOCUS) are also useful !

Current Leaders

CLEO-c: Tagging with D pairs very clean

Belle/BaBar: Continuum charm large statistics

↪ Sometimes using "continuum tagging"

Key issue:

Agreement with latest unquenched Lattice QCD ?

Techniques



CLEO-c uses Tagging:

$e^+e^- \rightarrow \psi(3770) \rightarrow D^0D^0, D^+D^-$
 e^+e^- @4170 MeV: $D_s^+D_s^{*-}$ & c.c.
creates **ONLY D pairs**

Fully reconstruct one $D_{(s)}$

- Can then infer neutrinos (constrained kinematics)
- or get absolute hadronic BFs

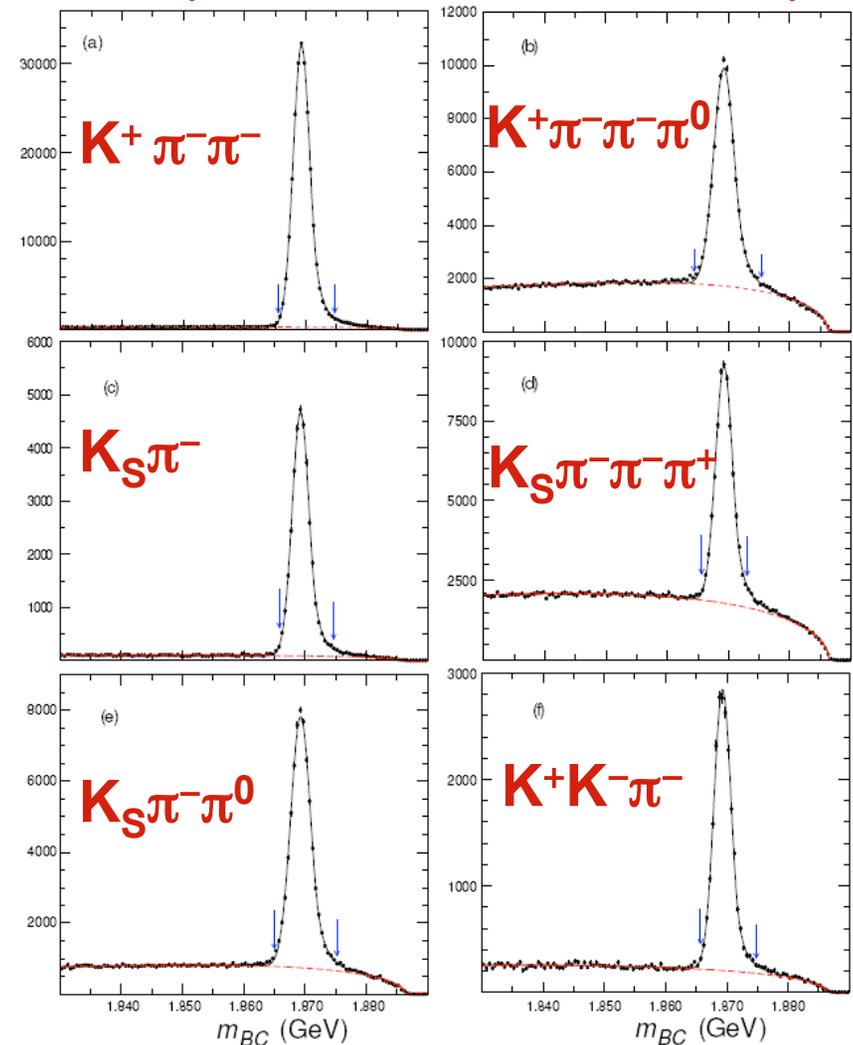
Typical tag rate per D:
15% / 10% / 5%
 D^0 / D^+ / D_s

Belle:

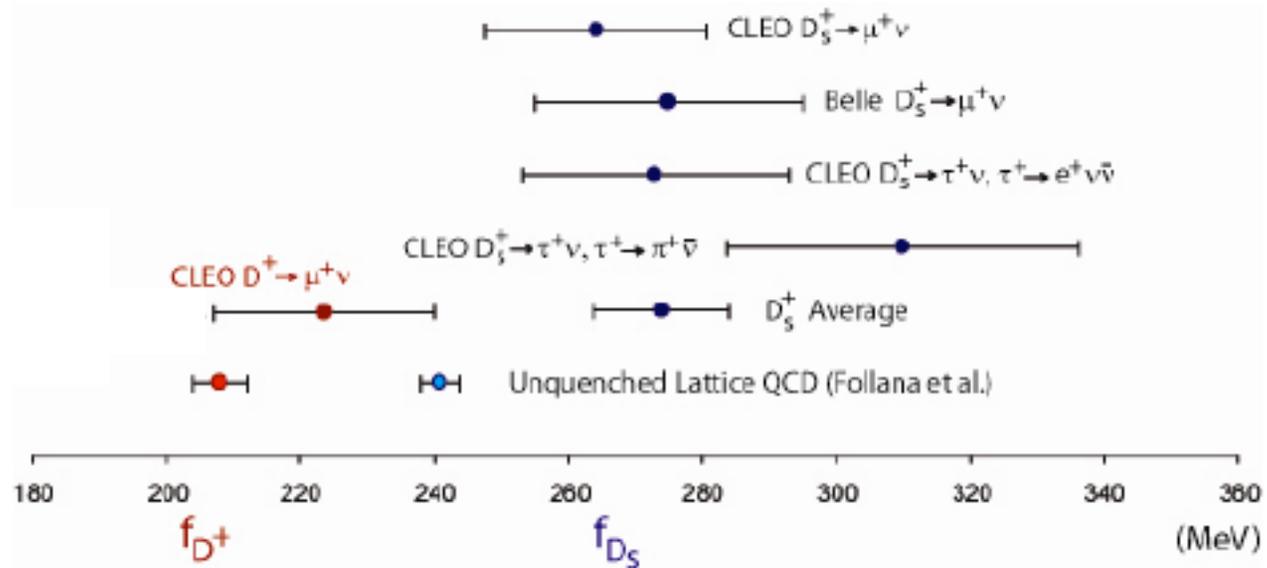
Has used a similar technique, with exclusive final states from continuum at 10 GeV



CLEO-c D^- Tags
= fully-recon. hadronic decay



Decay Constants: Pre-FPCP2008



D^+ : Consistent with LQCD,
but tests limited by
experimental precision

D_s : Disagreement with
latest Lattice result

D Decay Constant Status

Previous CLEO & Belle results average to give $f_{D_s} = 274 \pm 10 \text{ MeV}$
(see Rosner & Stone arXiv:0802.1043)

Best 2+1 unquenched lattice QCD obtains $241 \pm 3 \text{ MeV}$

v (Follana et.al, PRL 100, 062002 (2008))

■ Dobrescu & Kronfeld argue that this could be the effect of NP,
either charged Higgs (their own model) or leptoquarks
(see arXiv:0803.0512)

Kundu & Nandi suggest R-parity violating SUSY to explain
large f_{D_s} and B_s mixing phase (see arXiv:0803.1898)

Modest update from CLEO-c at FPCP2008 recapped here,
along with 2007 Belle result.

Next, recall the previous CLEO f_{D^+} result: $f_D = 223 \pm 17 \text{ MeV}$

Imprecise, compared to Follana et al., lattice: $207 \pm 4 \text{ MeV}$

Significant update from CLEO-c at FPCP2008 recapped here.

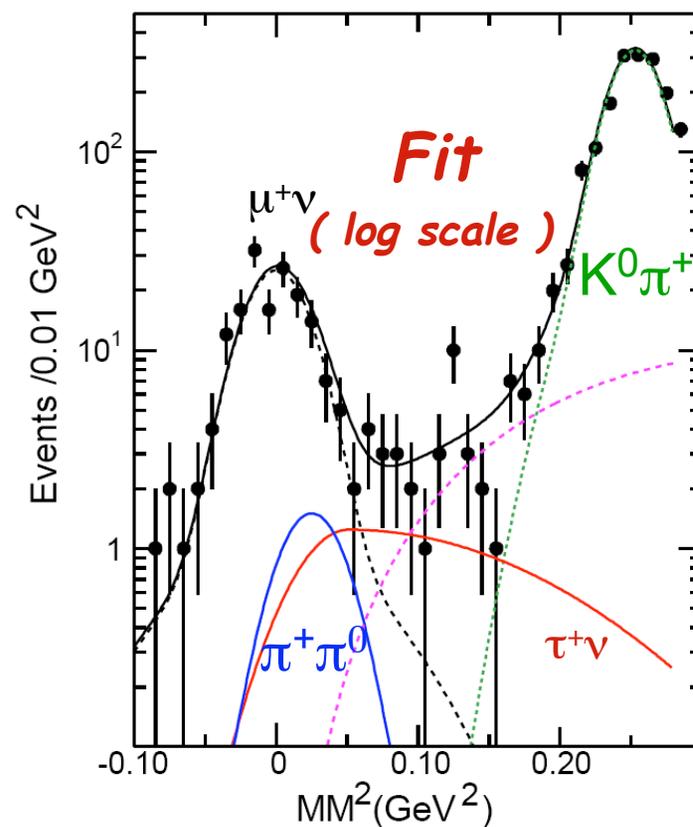
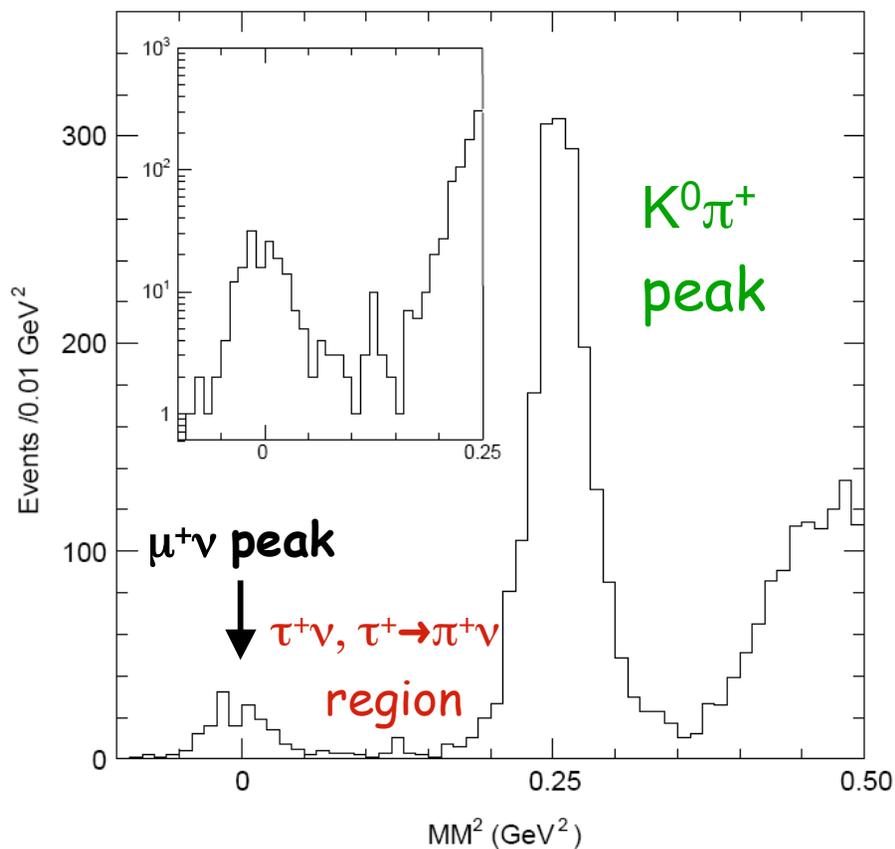


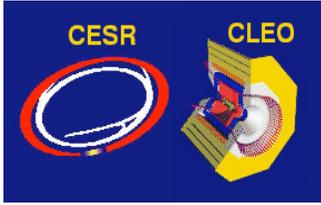
$D^+ \rightarrow \mu^+ \nu$ Update

PRELIMINARY
FPCP2008
818 pb⁻¹

Neutrino from 4-momentum balance
can plot (missing mass)²: MM^2

Clean, isolated signal peak: Power of D-tagging:
Recall that the signal is one track + neutrino !





$D^+ \rightarrow \mu^+ \nu$ Results

PRELIMINARY
FPCP2008
818 pb⁻¹

Fix τ_{ν}/μ_{ν} at SM ratio of 2.65 :

$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu) = (3.86 \pm 0.32 \pm 0.09) \times 10^{-4}$$

$$f_{D^+} = (206.7 \pm 8.5 \pm 2.5) \text{ MeV}$$

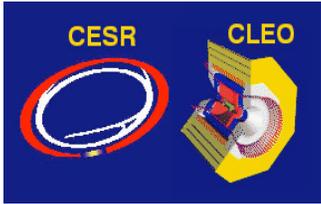
Best number in context of SM

Float τ_{ν}/μ_{ν} :

$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu) = (3.96 \pm 0.35 \pm 0.10) \times 10^{-4}$$

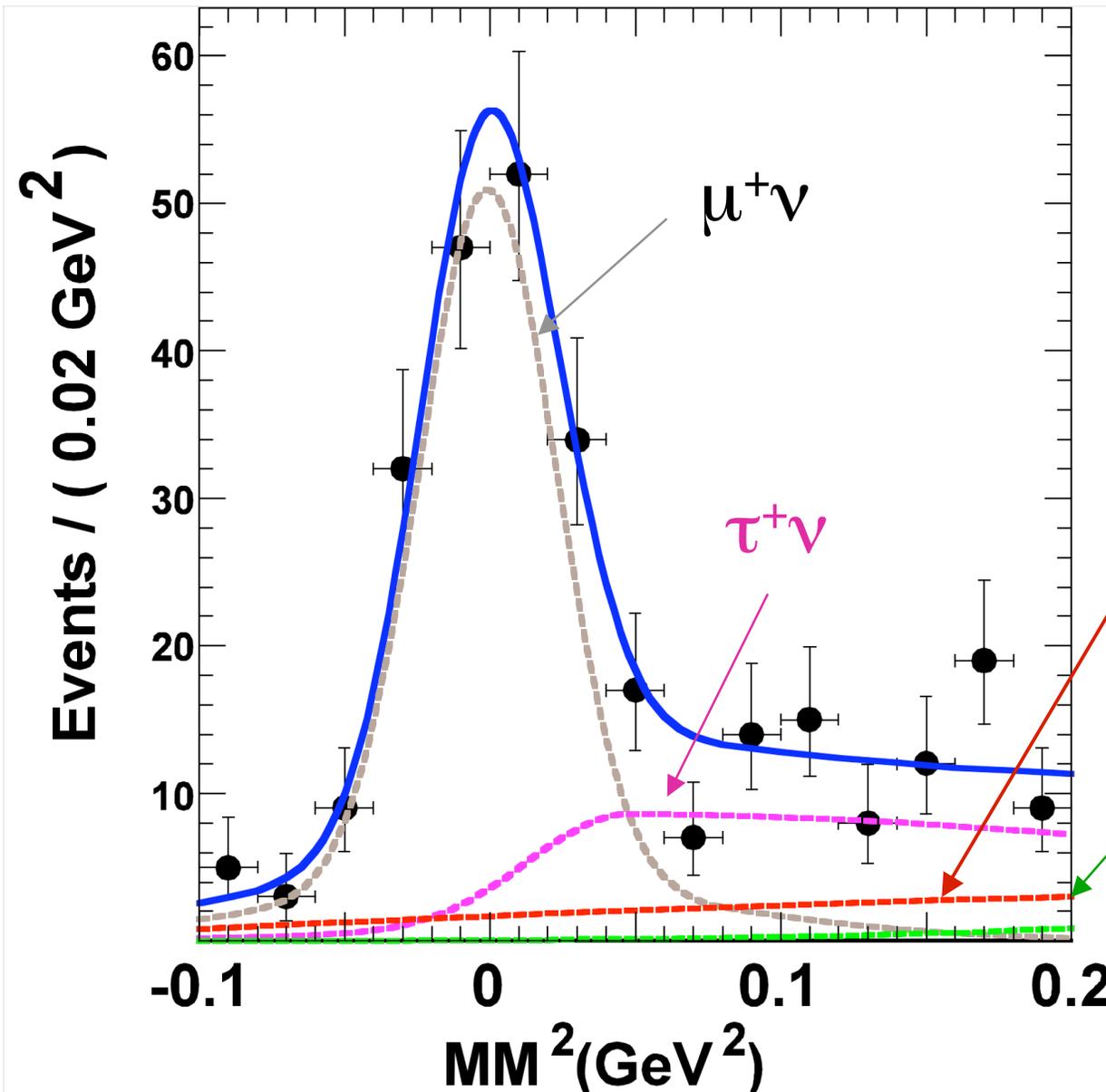
$$f_{D^+} = (208.5 \pm 9.3 \pm 2.5) \text{ MeV} \quad \text{consistent}$$

Best number for use with Non-SM models



$$D_s \rightarrow \mu^+ \nu \text{ \& \ } \tau^+ \nu$$
$$(\text{w/ } \tau^+ \rightarrow \pi \nu)$$

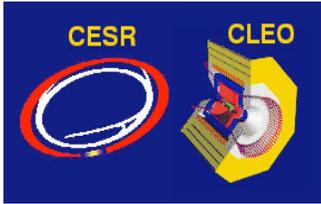
PRELIMINARY
FPCP2008
~400 pb⁻¹
(& 200 more soon)



Background
 D_s sidebands

Extra g
background

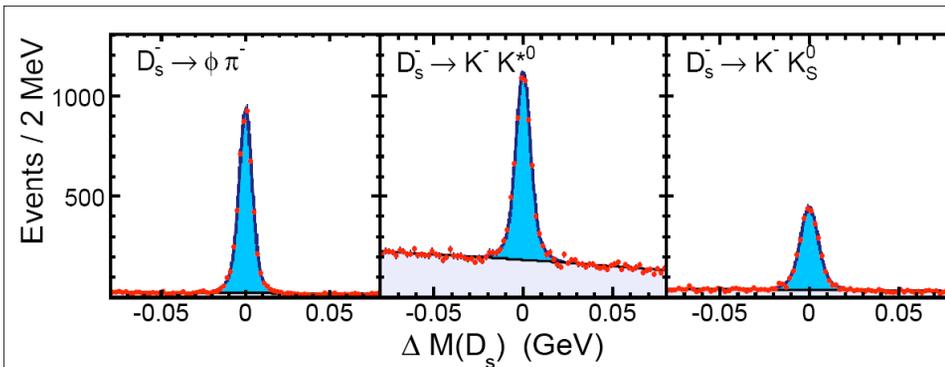
Have published:
PRL99, 071802
PRD76, 072002
(2007) 314 pb⁻¹



$$D_s \rightarrow \tau^+ \nu \quad (\tau^+ \rightarrow e^+ \nu \nu)$$

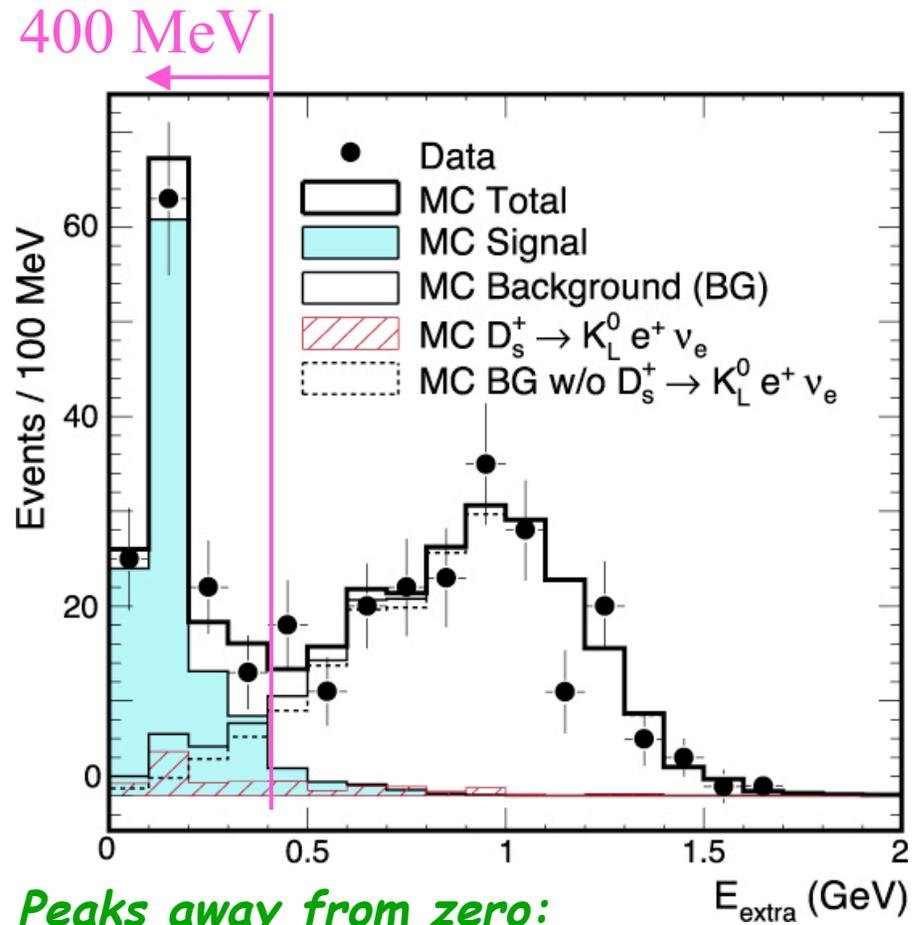
PRL100, 161801
(2007) 298 pb⁻¹

Use only cleanest tags (for now)

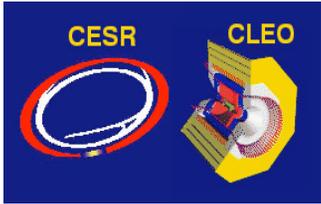


Always have >1 neutrino!
Abandon use of MM²
Semileptonic events tend to have hadronic Energy in CsI (but careful re: K_L !)

Plot E_{extra} in Calorimeter (Extra: not tag or e)



Peaks away from zero:
E_{extra} can include γ from D_s^{} decay*



CLEO-c D_s Summary

PRELIMINARY
FPCP2008

| Mode | \mathcal{B} (%) | f_{D_s} (MeV) |
|--|---|----------------------------|
| (1) $\mu\nu + \tau\nu$ (fix SM ratio) | $\mathcal{B}^{\text{eff}}(D_s \rightarrow \mu\nu) =$ (0.613 \pm 0.044 \pm 0.020) | 268.2 \pm 9.6 \pm 4.4 |
| (2) $\mu\nu$ only | $\mathcal{B}(D_s \rightarrow \mu\nu) =$ (0.600 \pm 0.054 \pm 0.020) | 265.4 \pm 11.9 \pm 4.4 |
| (3) $\tau\nu, \tau \rightarrow \pi\nu$ | $\mathcal{B}(D_s \rightarrow \tau\nu) =$ (6.1 \pm 0.9 \pm 0.2) | 271 \pm 20 \pm 4 |
| (4) $\tau\nu, \tau \rightarrow e\nu$ | $\mathcal{B}(D_s \rightarrow \tau\nu) =$ (6.17 \pm 0.71 \pm 0.36) | 273 \pm 16 \pm 8 |
| CLEO Average of (1) & (4) | | 269.4 \pm 8.2 \pm 3.9 |

- ✓ *CLEO-c updated both D and D_s at FPCP2008:*
- ✓ *Due to time, I can't do justice to the many nice cross-checks...*
- ✓ *please see S. Stone's FPCP talk for more details.*



Belle: $D_s \rightarrow \mu^+ \nu$

arXiv:0709.1340
(2007) 548 fb⁻¹

Use "Continuum tagging":

$$e^+e^- \rightarrow D^{\pm,0} K^{\pm,0} X D_s^*,$$

$$X = n\pi \text{ -or- } n\pi \gamma \text{ (fragmentation)}$$

about 25% of D BF used

Use recoil mass:

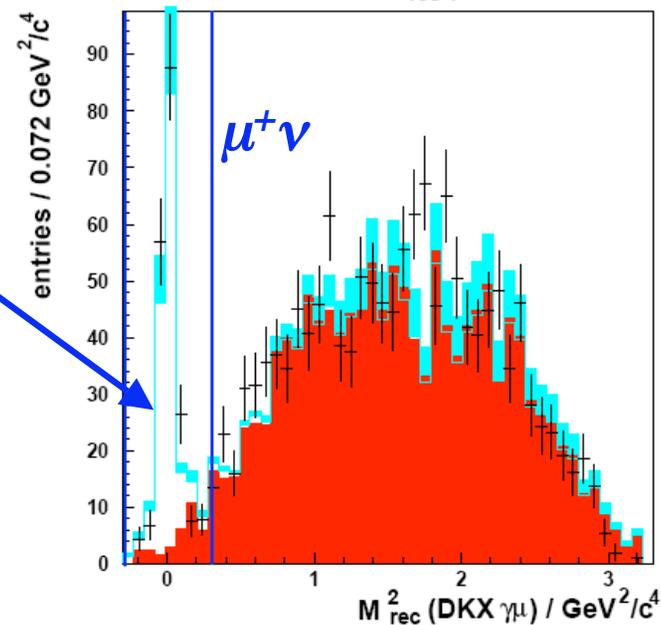
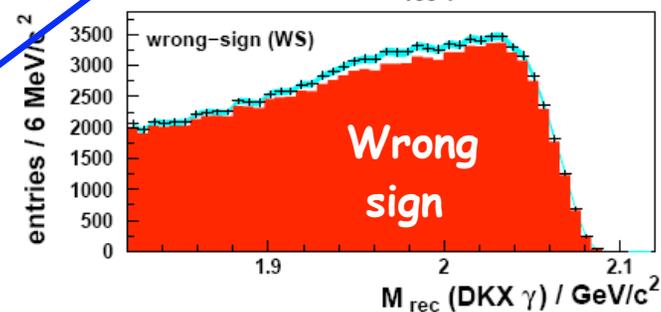
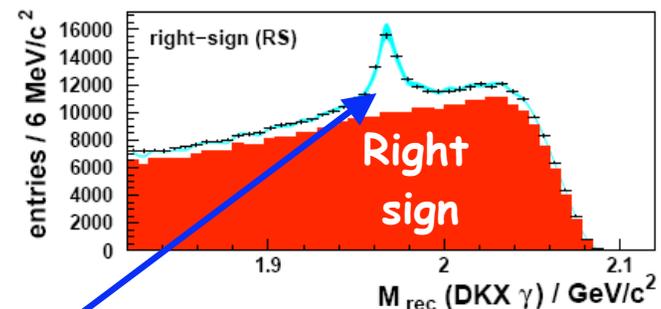
against $DKX\gamma$ counts total D_s

against $DKX\gamma\mu$ counts $D_s \rightarrow \mu^+ \nu$

$$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu) =$$

$$(0.644 \pm 0.076 \pm 0.057)\%$$

$$f_{D_s} = 275 \pm 16 \pm 12 \text{ MeV}$$



Decay Constant Summary

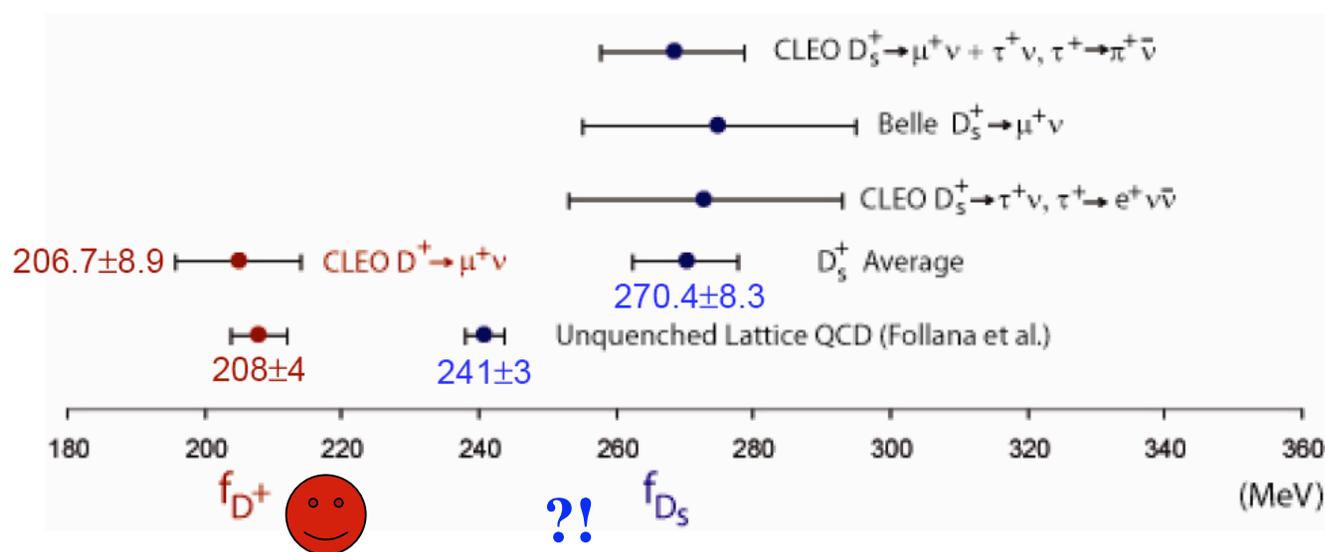
Weighted Ave. CLEO+Belle: $f_{D_s} = 270.4 \pm 7.3 \pm 3.7$ MeV
 (systematic errors are uncorrelated)

Using $f_{D^+} = (206.7 \pm 8.5 \pm 2.5)$ MeV

$f_{D_s}/f_{D^+} = 1.31 \pm 0.06 \pm 0.02$ larger than predicted

$\Gamma(D_s^+ \rightarrow \tau^+\nu) / \Gamma(D_s^+ \rightarrow \mu^+\nu) = 10.3 \pm 1.1, \quad SM = 9.72$

Consistent with lepton universality



Note: BaBar f_{D_s} PRL 98, 141801 (2007) & others depending on " $B(D_s \rightarrow \phi\pi)$ " are omitted here...

Semileptonic Decays

Concentrate on Form Factors

- o Pseudoscalar modes for Lattice QCD tests

Key: $D \rightarrow \pi l \nu$ as test of $B \rightarrow \pi l \nu$ (needed for V_{ub})

- o $D_s \rightarrow K e \nu$: newest precision result

Omitting:

- o Many other branching ratios

esp. $D \rightarrow \rho/\omega/\eta/K_1 e \nu$ (CLEO)

- o Non-Parametric FF analysis (CLEO)

- o Untagged $D \rightarrow K l \nu$ (BaBar)

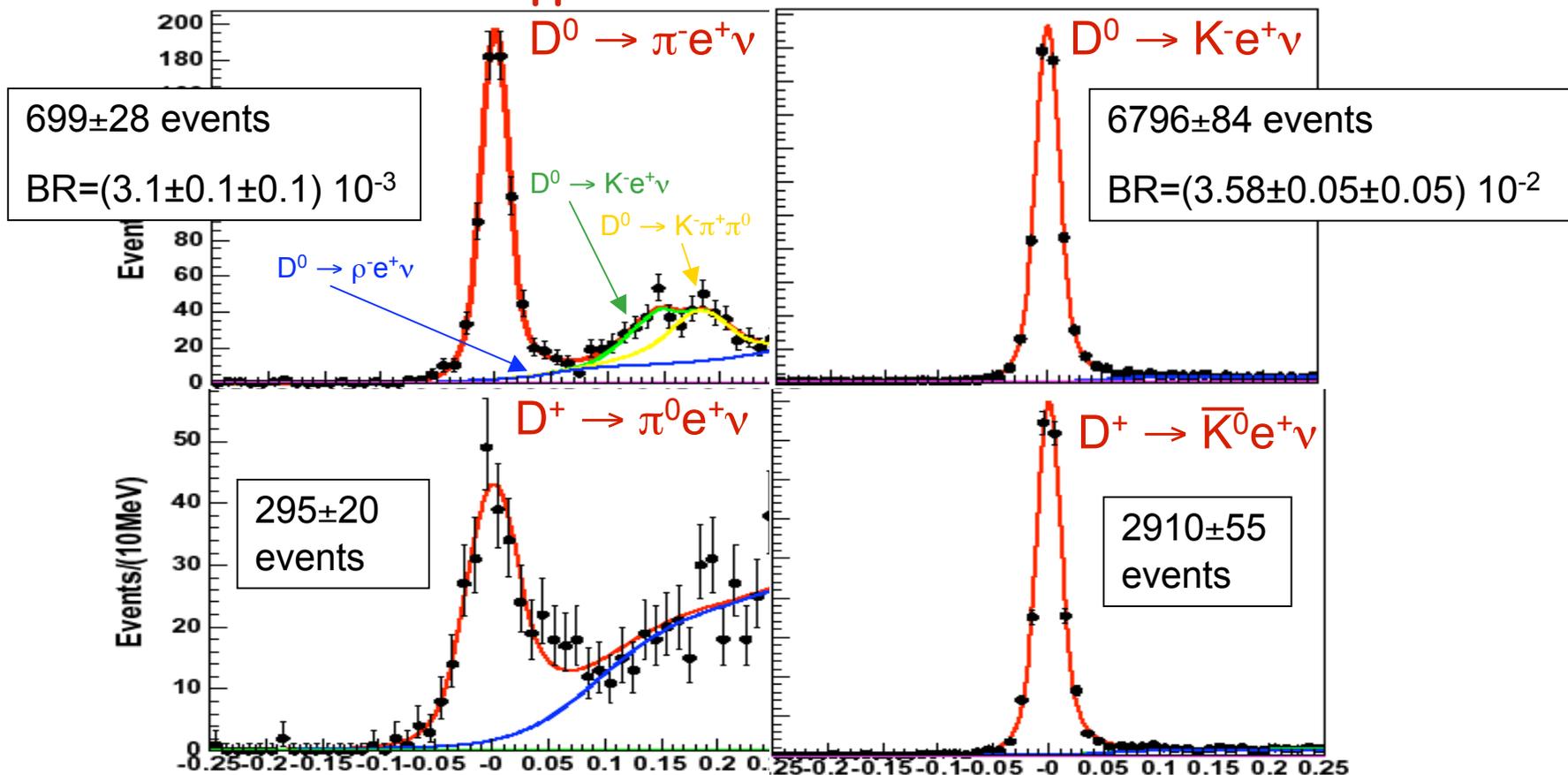


$D^{0+} \rightarrow \pi e \nu, K e \nu$ (tagged)

Preliminary
281 pb⁻¹

Cabibbo suppressed

Cabibbo favored



$$U_{\text{miss}} = E_{\text{mis}} - |p_{\text{mis}}| \quad (\text{GeV})$$

Excellent background suppression

Small K - π feed-across due to threshold kinematics

Past results: K - π signals overlapped completely!



$D^0 \rightarrow \pi l \nu, K l \nu$

PRL 97, 061804
(2006) 282 fb⁻¹

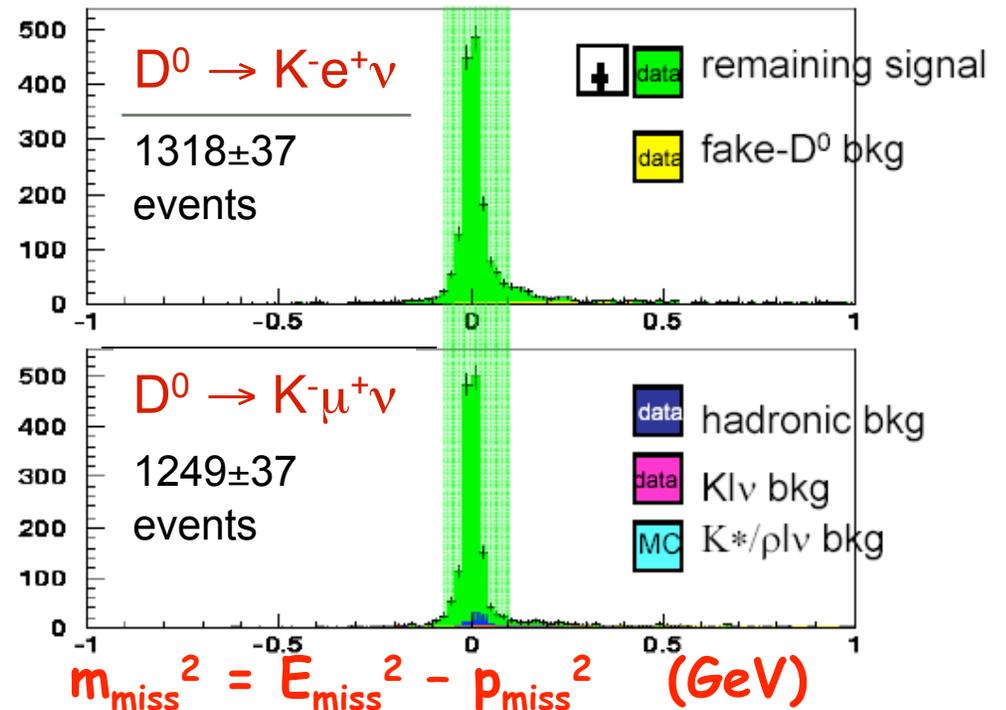
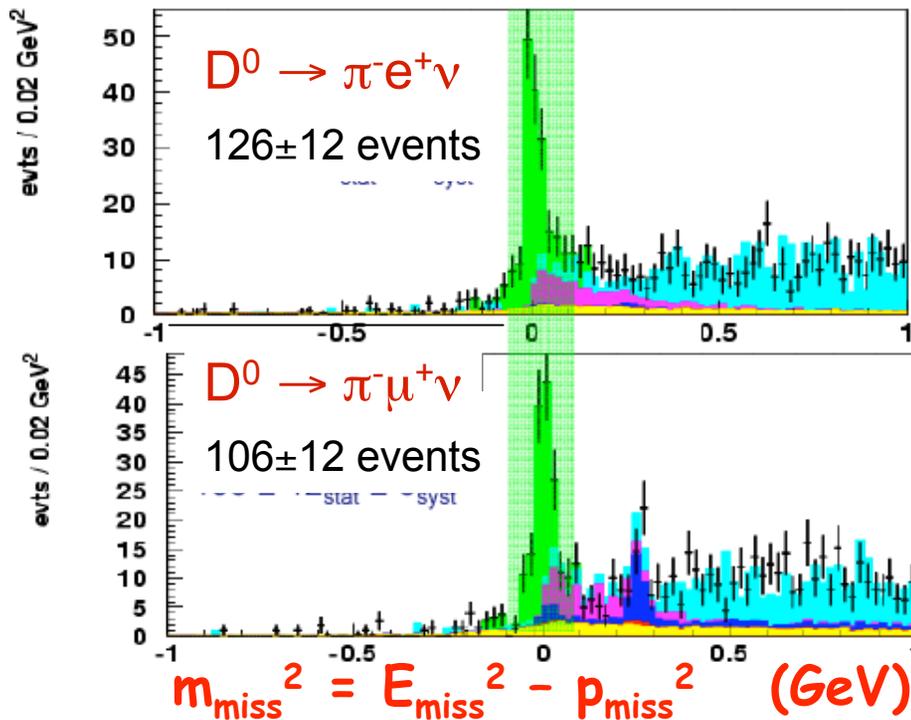
Use "Continuum tagging" again: $e^+e^- \rightarrow D^{(*)}_{\text{tag}} D^{*\text{signal}} X$.

Reconstruct all particles (except for neutrino)

Tagging provides absolute normalization $\sim 56,000$ tagged D^0

Cabibbo suppressed

Cabibbo favored



Impressive results in difficult production environment

Both e and μ measured, but only D^0

vs. CLEO-c: 1000x lumi, but ~ 3 x less signal events & ~ 10 x worse signal/noise

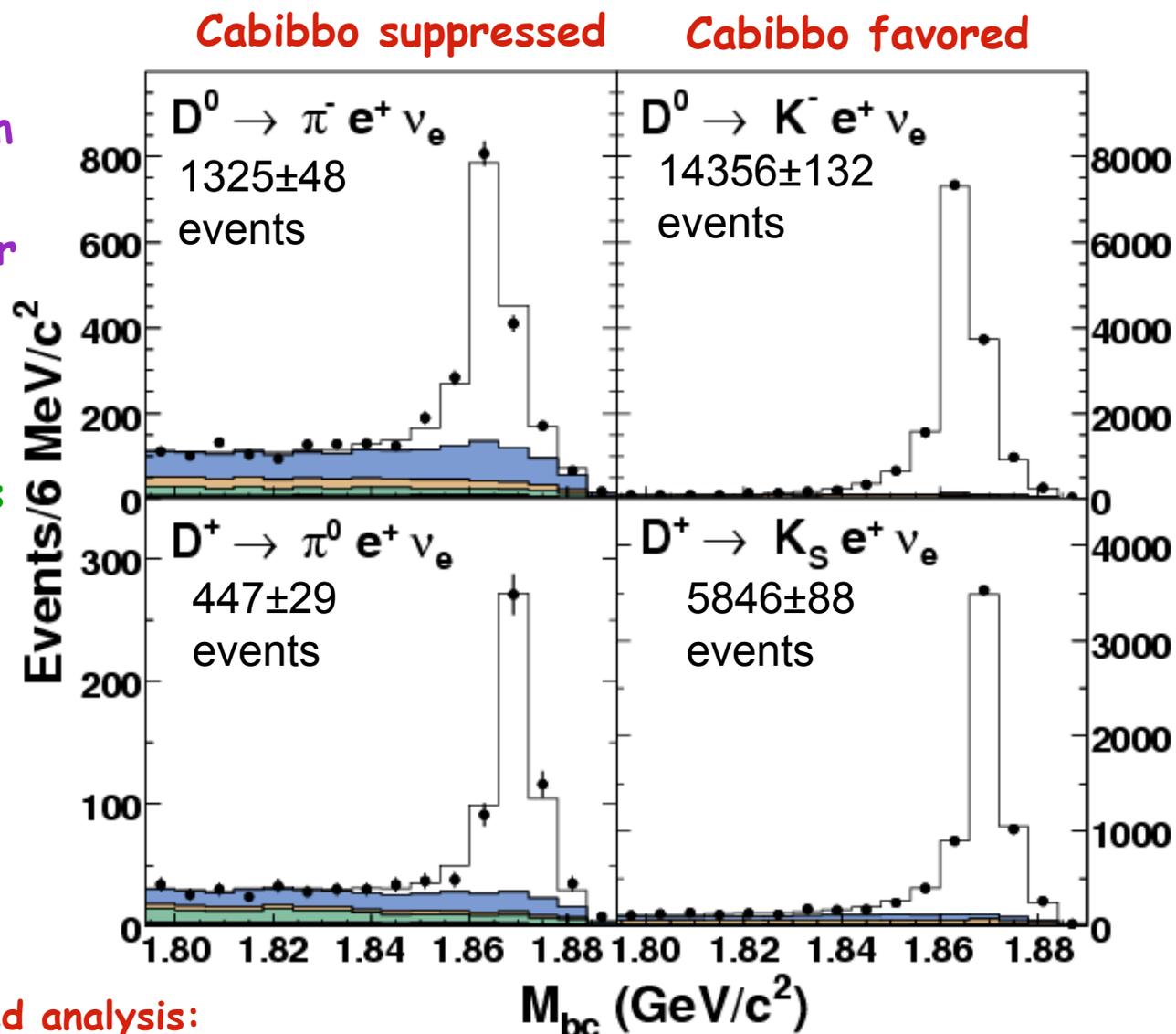


$D^{0+} \rightarrow \pi e \nu, K e \nu$ (untagged)

arXiv:0712.1012
arXiv:0712.0998
(to appear PRL/D)
281 pb⁻¹

Use global 4-momentum
balance
Infer neutrino 4-vector
w/o explicit tag

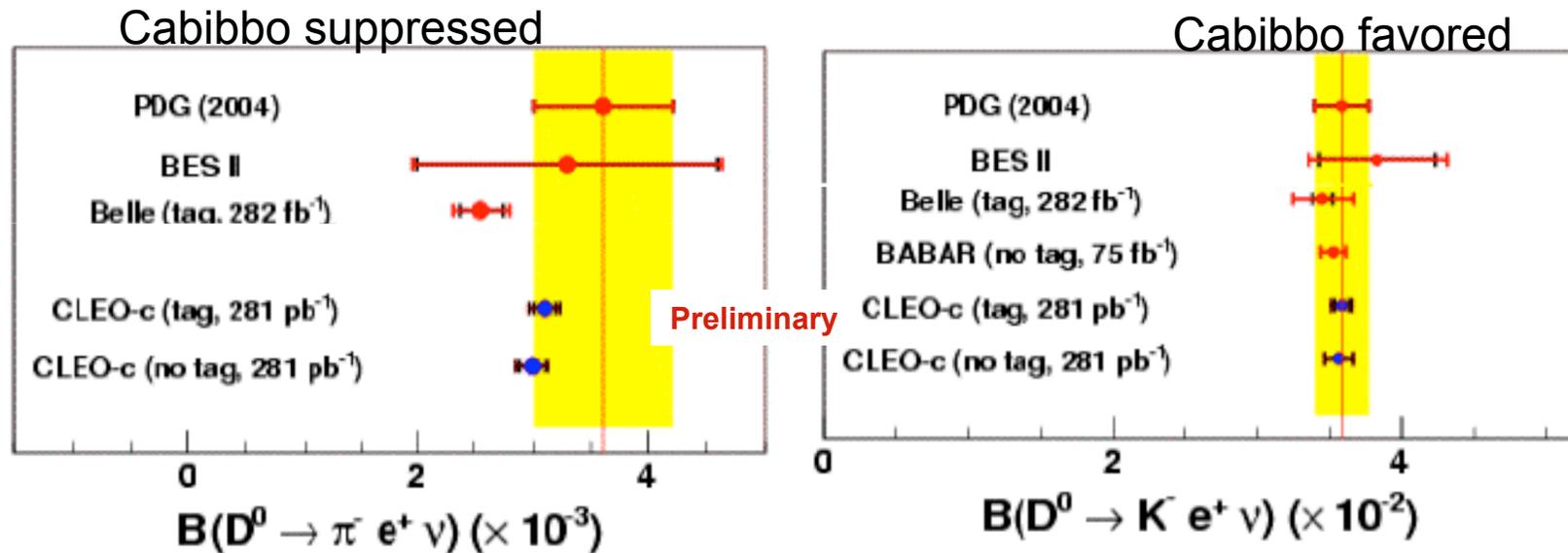
Can then use familiar
beam-constrained mass



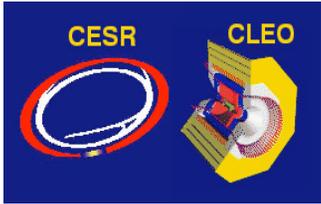
Compared to the tagged analysis:

- Factor ~2 increase in the signal statistics.

Branching Ratios

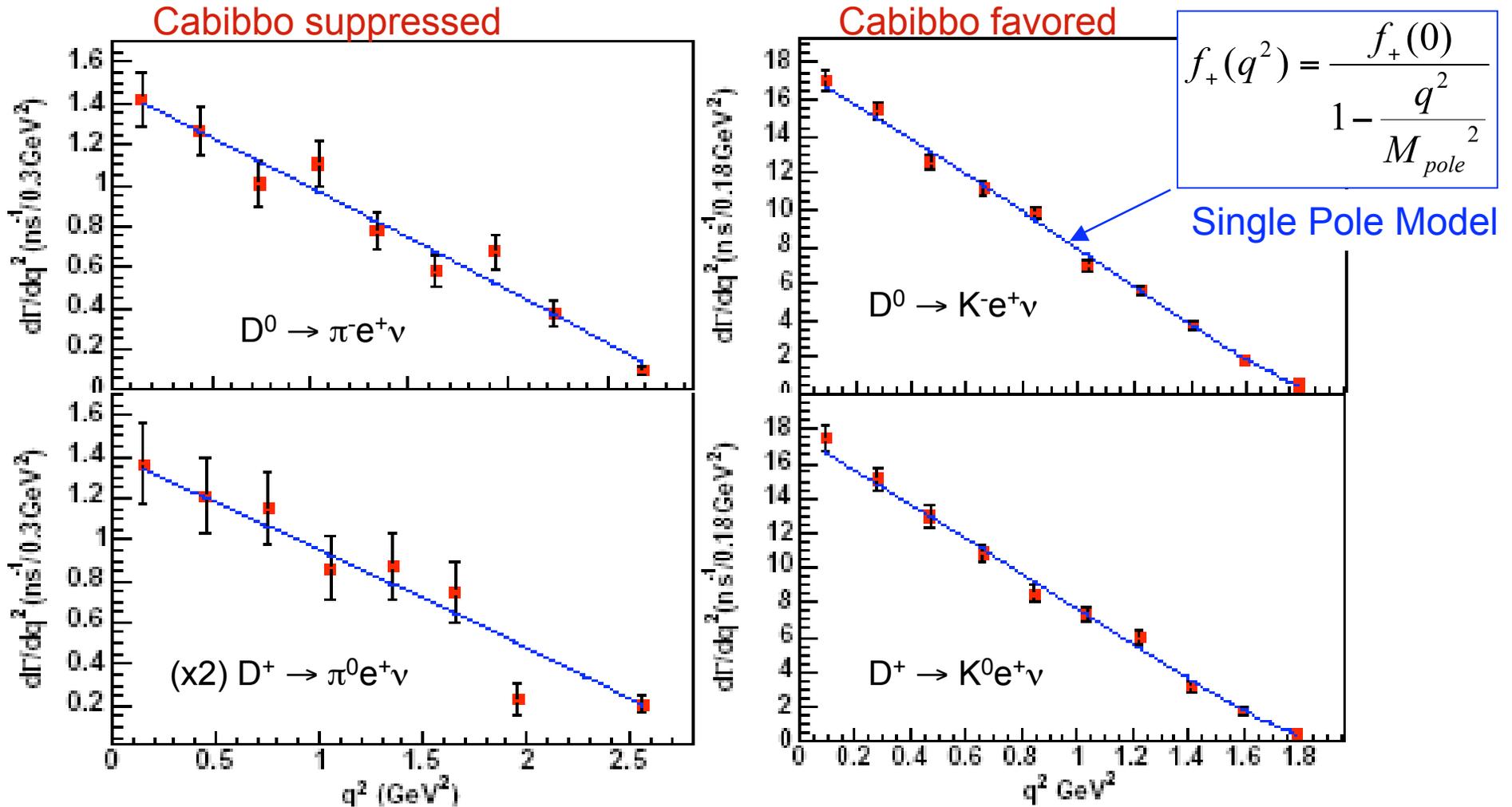


Significant improvement in precision by recent
BaBar/Belle/CLEO-c measurements
(CLEO-c best, especially for $\pi e \nu$)



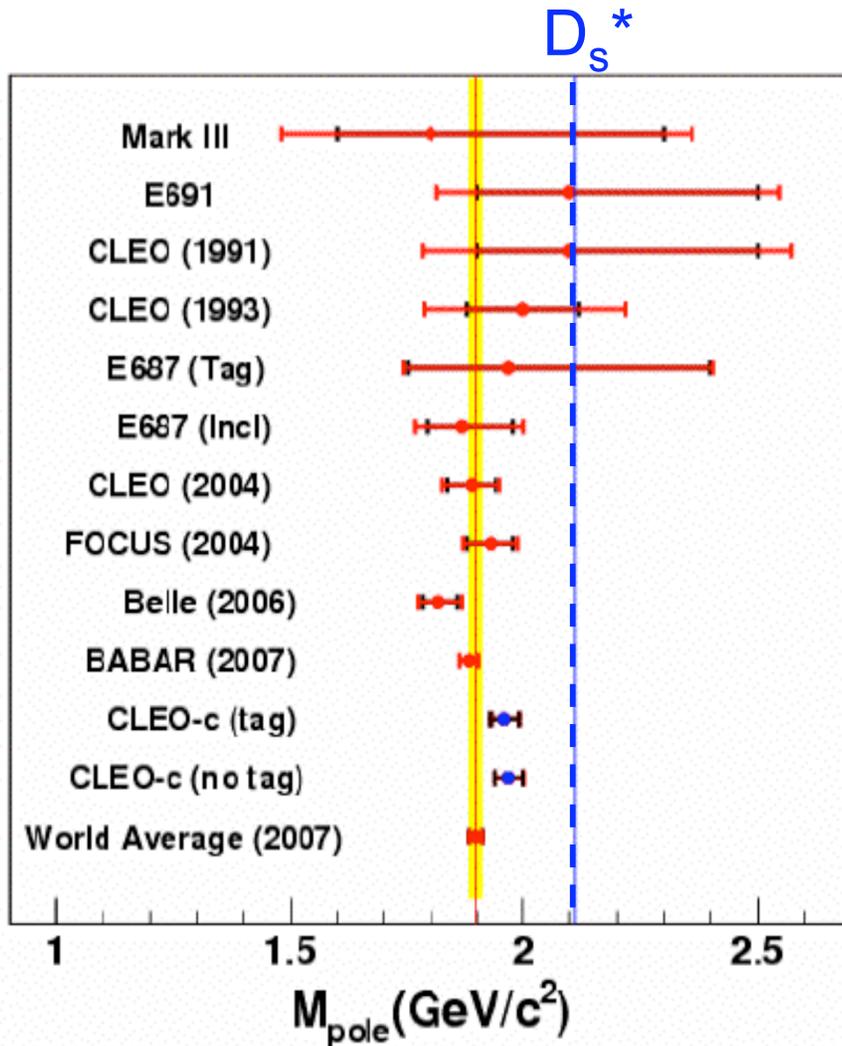
Pseudoscalar Form Factors

Preliminary
Tagged
281 pb⁻¹



Much of the visible variation is due to the phase-space factor (P^3).

$D \rightarrow K\pi$ Form Factor Pole Mass

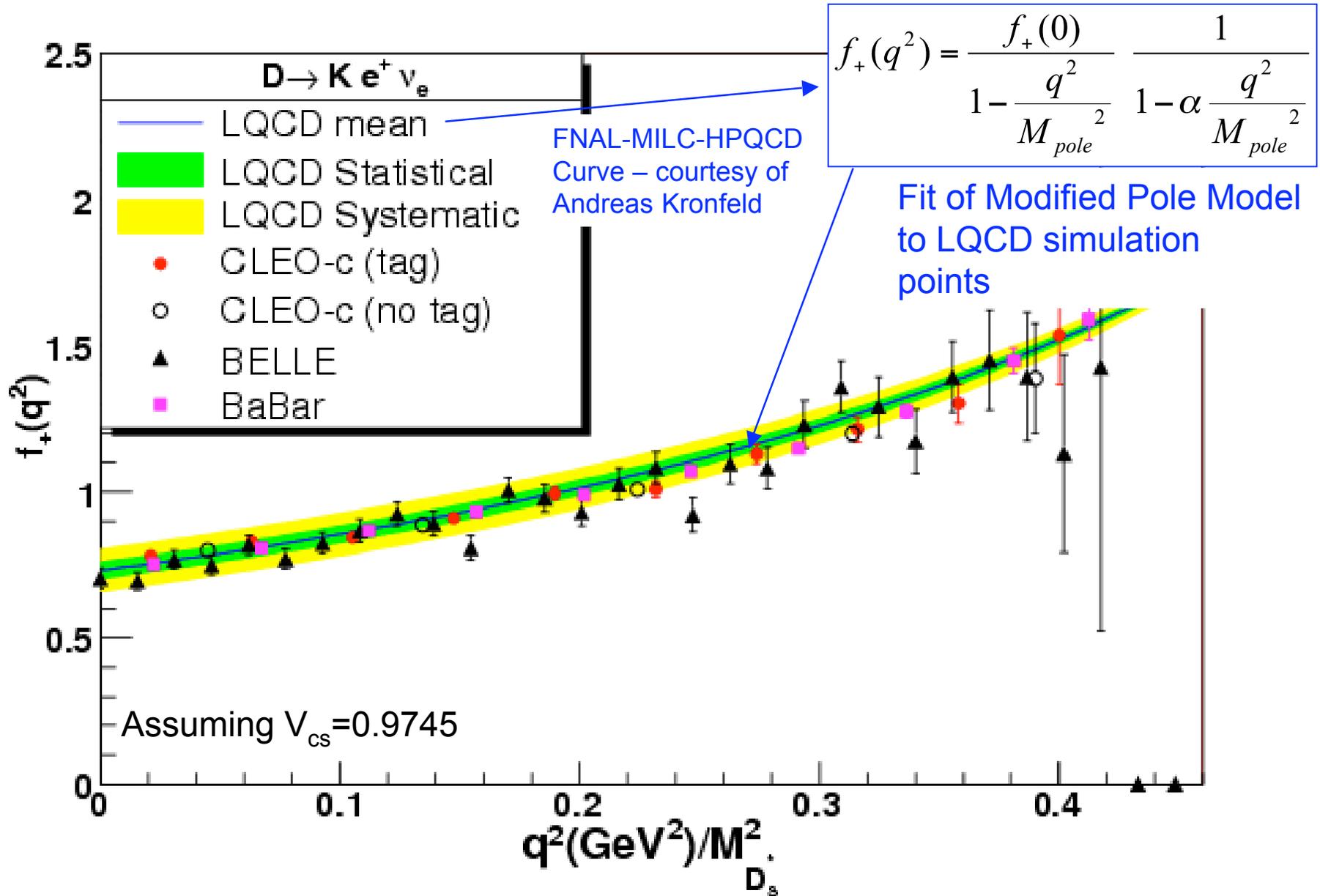


Single Pole Model describes data reasonably well,

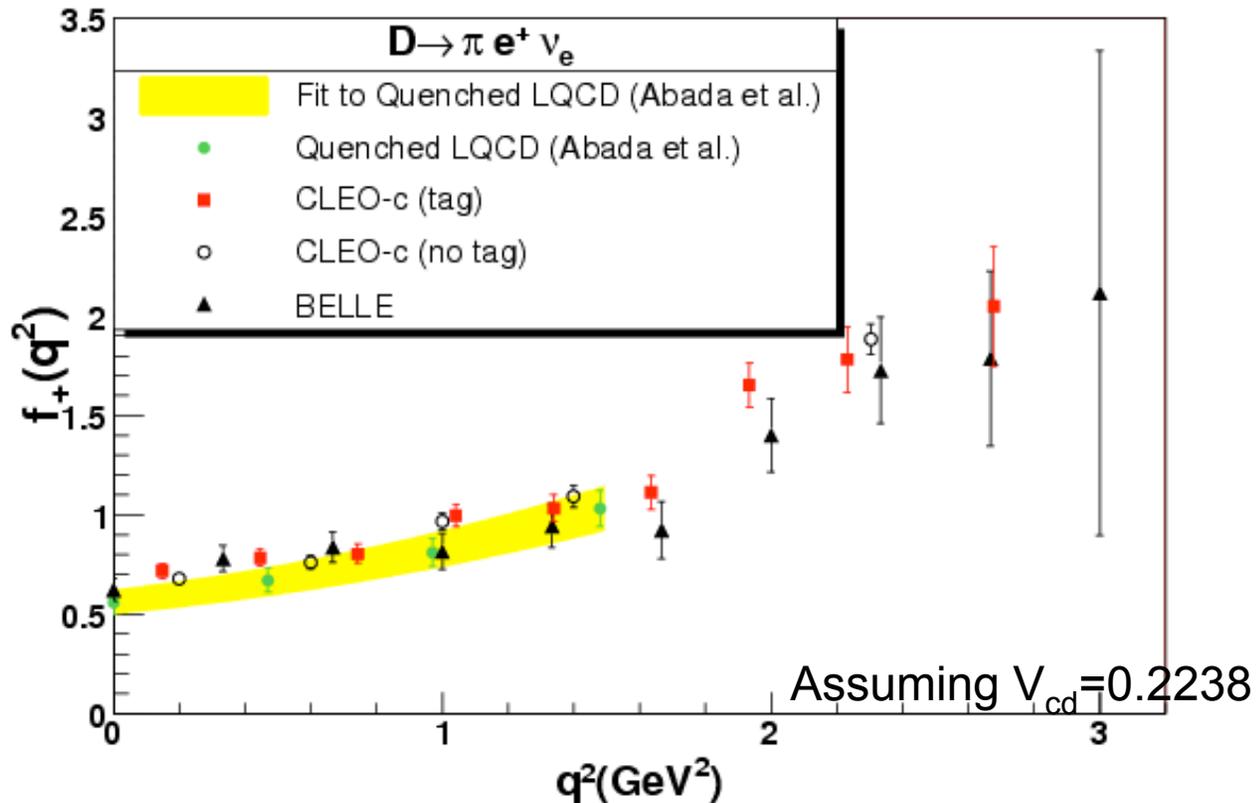
but not with spectroscopic D_s^ mass*

(from Ian Shipsey's talk at LQCD workshop, FNAL, Dec 2007
– see for more extensive discussion of form factor results)

$D \rightarrow K e^+ \nu_e$ Form Factor vs. LQCD



$D \rightarrow \pi e \nu$ Form Factor vs. LQCD



Careful re: comparisons on next page:

If parametrization wrong, comparisons can be misleading!

Much recent effort on systematic series expansions... but no time today

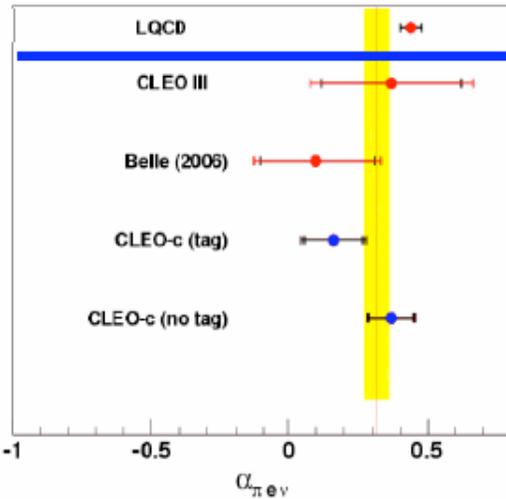
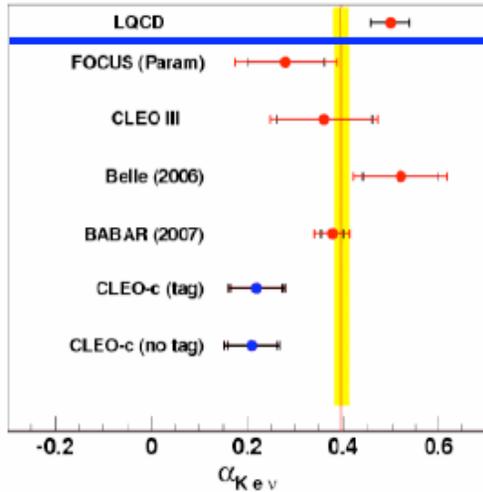
A recent paper: T. Becher & R. Hill PLB 633, 61 (2006)

(previous work: Boyd, Grinstein, Lebed, Savage, Arnesen, Rothstein, Stewart...)

CLEO untagged paper uses these expansions along with older pole forms

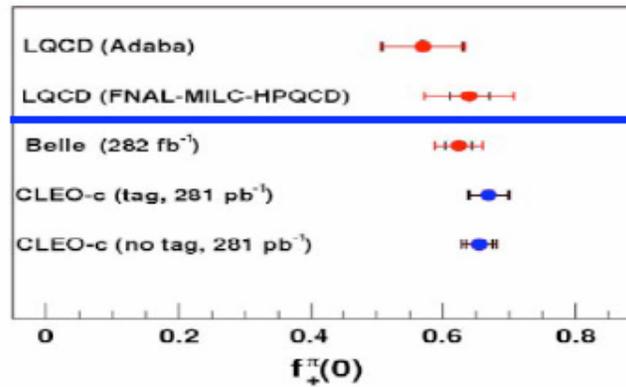
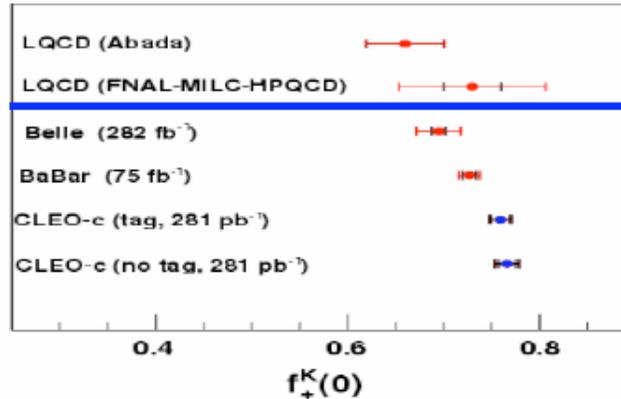
More Tests of LQCD

Slope



Normalization

(assuming $|V_{cs (cd)}| = |V_{ud (us)}|$)



$D \rightarrow K e \nu$

Normalization errors

| Channel | Experiments | theory |
|---------------------------|-------------|--------|
| $D \rightarrow K e \nu$ | 2% | 10% |
| $D \rightarrow \pi e \nu$ | 4% | 10% |

$D \rightarrow \pi e \nu$

Theoretical errors larger than experimental



$D_s \rightarrow K^+K^-e\nu$ FFs

Preliminary
FPCP2008
214 fb⁻¹

Excellent angular fits:

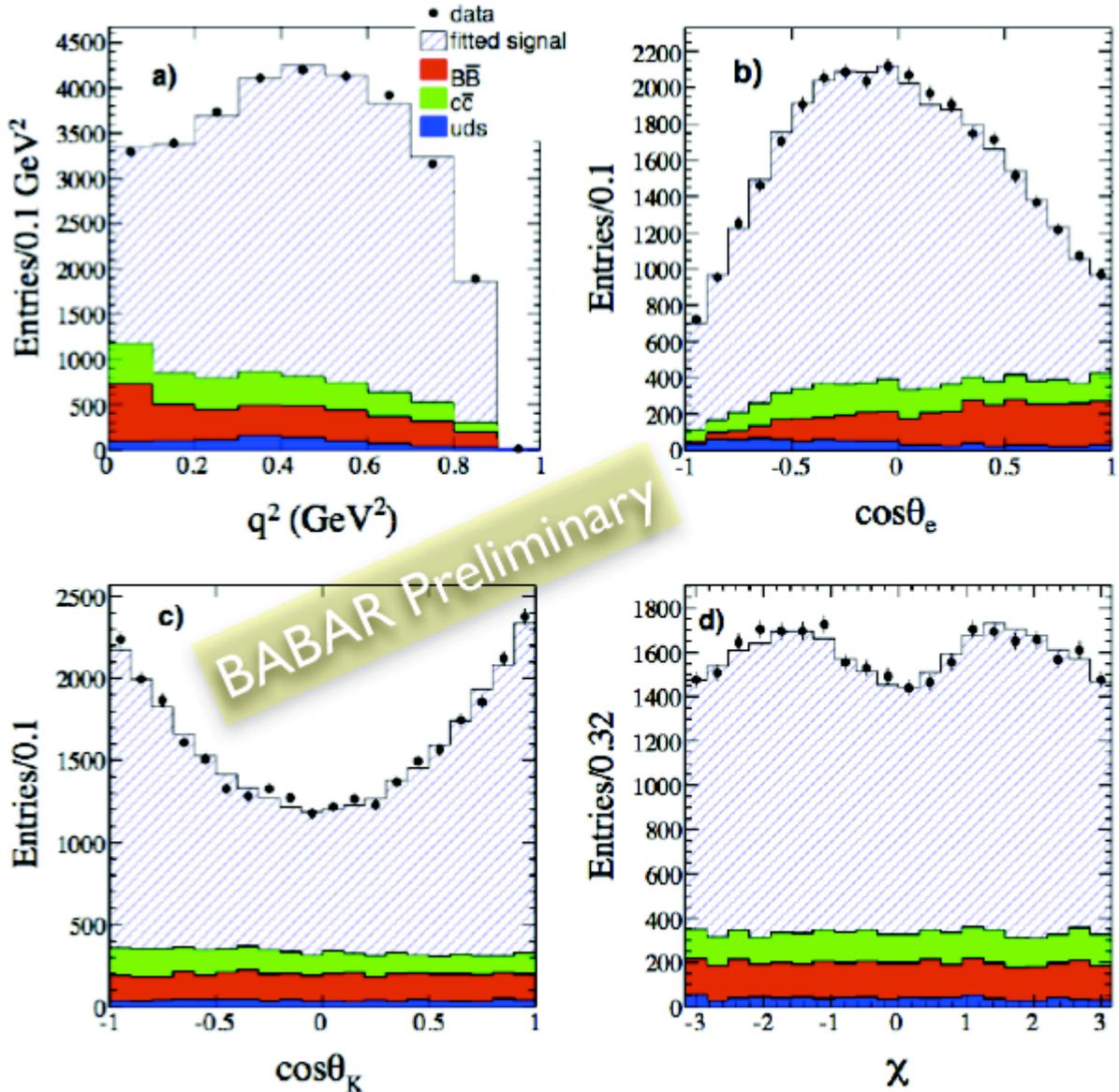
Untagged Analysis

Detailed form factor analysis
25K events
(more complicated
w/ a vector meson)

$$D_s \rightarrow \phi e \nu$$

$$D_s \rightarrow f_0 e \nu$$

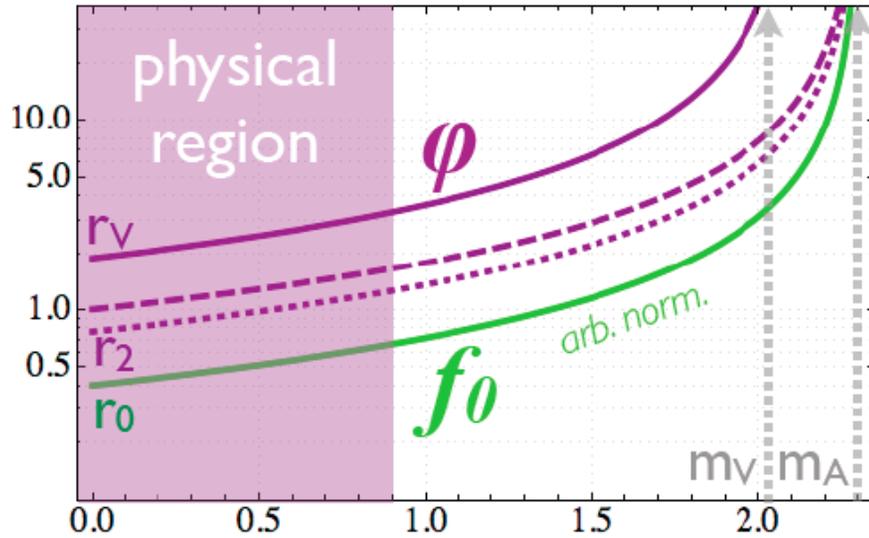
(first evidence)





$D_s \rightarrow K^+K^-e\nu$ FFs

Preliminary
FPCP2008
214 fb⁻¹



3 form-factors for ϕ
(fix $r_1 = 1.0$)

1 form-factor for f_0

FIT:

Float ratios to r_1 at $q^2=0$
 M_V fixed; M_A floats

$N_{\text{sig}} = 25,152 \pm 177 \pm 367$
 $r_V = 1.868 \pm 0.061 \pm 0.079$
 $r_2 = 0.763 \pm 0.072 \pm 0.062$
 $r_0 = 15.3 \pm 2.6 \pm 1.0$
 $m_A = 2.30^{+0.24}_{-0.18} \pm 0.21$ GeV



Agreement with
Lattice, except r_V
(need better model?)

$r_V = 1.35 \pm 0.08$
 $r_2 = 0.98 \pm 0.09$



Lattice: UKQCD
Hep-lat/0109035

+ $BF(D_s \rightarrow KK\pi)$, $BF(\phi \rightarrow KK)$, D_s lifetime, V_{cs} :
 $A_1(q^2 = 0) = 0.605 \pm 0.012 \pm 0.018 \pm 0.018$



$A_1(q^2=0) = 0.63 \pm 0.02$

Precision Hadronic Branching Fractions

Systematics:

tracking, PID efficiency

always present

BUT... some nice techniques to measure w/ tagging

Background issues:

better with threshold tagging...

Similar considerations for semileptonic, leptonic

but statistics still dominate there

*(interested in Cabibbo-suppressed semileptonic,
or rare fully leptonic modes...)*

Topics:

Hadronic modes and Golden-Mode BFs: D^0 , D^+ & D_s

Quantum correlations & $K\pi$ Phase

Omitted

o In Backup slides: Interference $D \rightarrow K_{L/S} \pi$

o MANY other decay modes (Cabibbo-suppressed, ...)

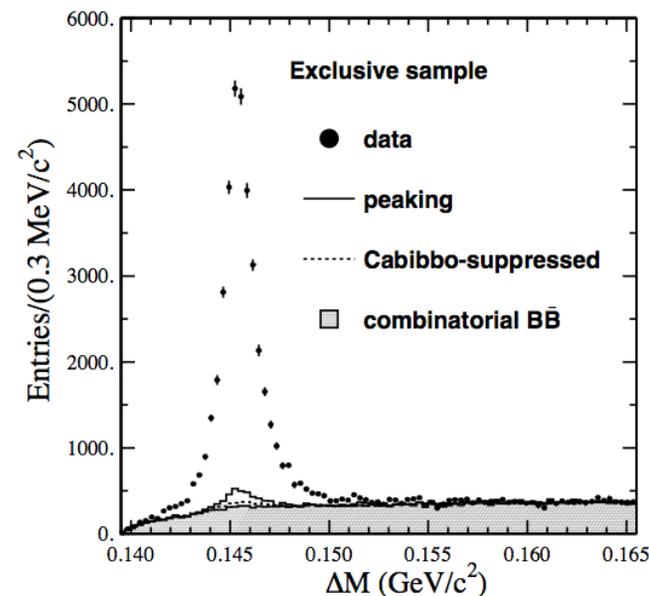
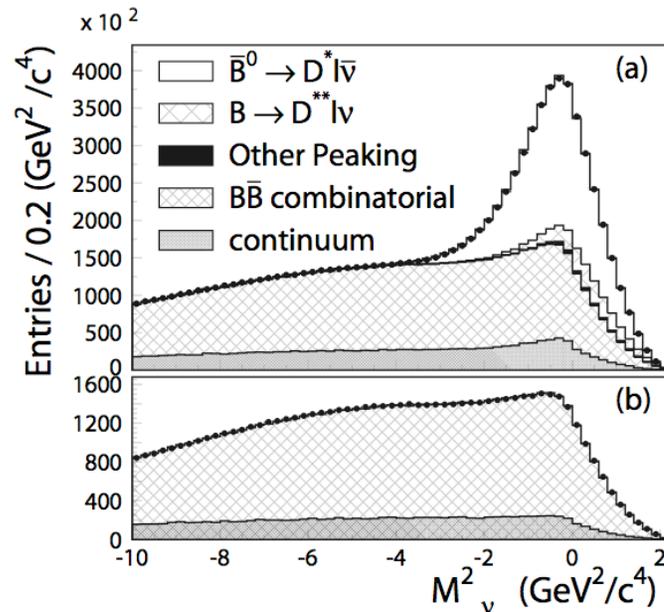


PRL 100, 051802
(2008) 232 fb⁻¹

Partial reconstruction of $B^0 \rightarrow D^{+} (X) l^- \nu_l$*

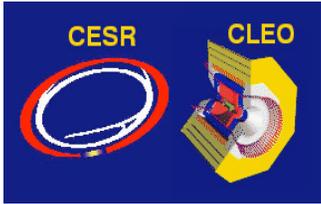
Slow pion used to estimate D^ momentum*

Full recon of $D^0 \Rightarrow K^- \pi^+$ within inclusive sample



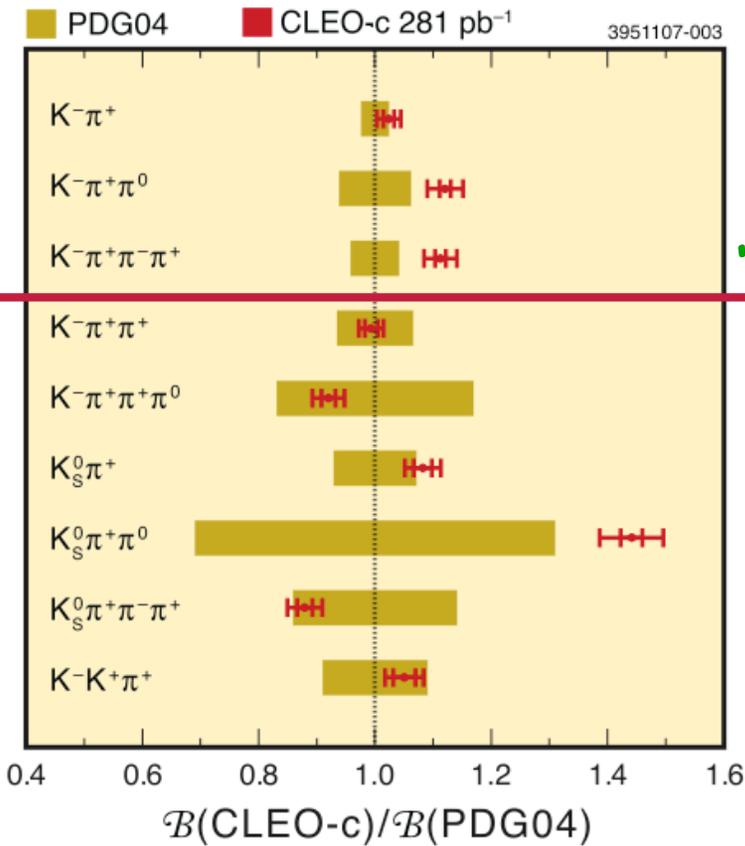
$$BF = (4.007 \pm 0.037 \pm 0.072) \%$$

Systematics: 1.8% = 1.5% exclusive effic. ⊕ 1.0% inclusive



D^0 & D^+ Comparisons

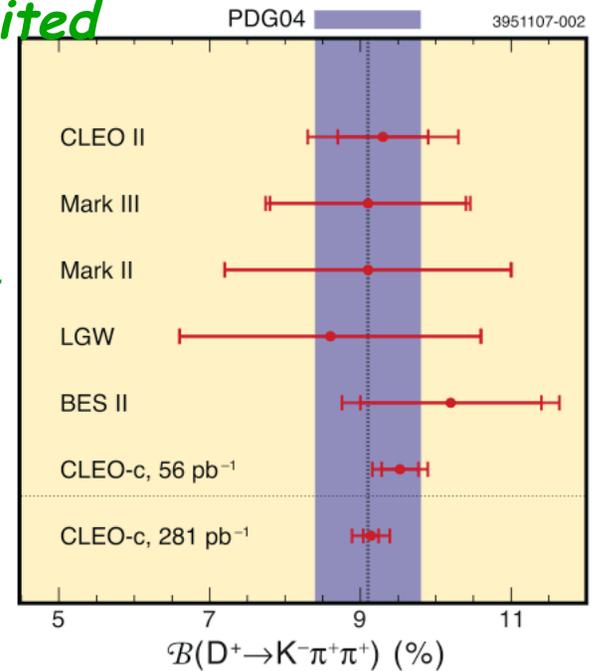
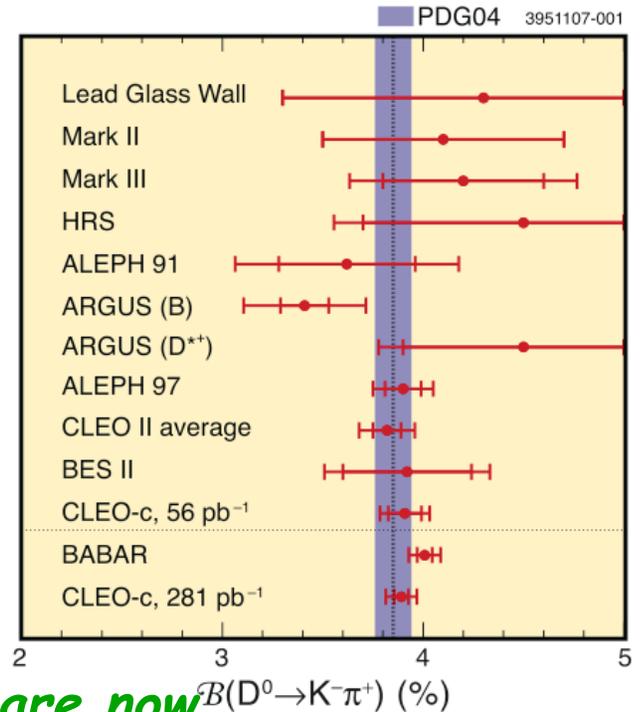
NOTE: method cancels
 #DD pairs algebraically;
 & tag eff. almost cancels



D^0 → $K^-\pi^+$

"Golden Modes" are now systematics limited

D^+ → $K^-\pi^+\pi^+$



PRD 76, 112001
 (2007) 281 pb⁻¹

Use PDG04 since PDG06 included 56 pb⁻¹ CLEO-c



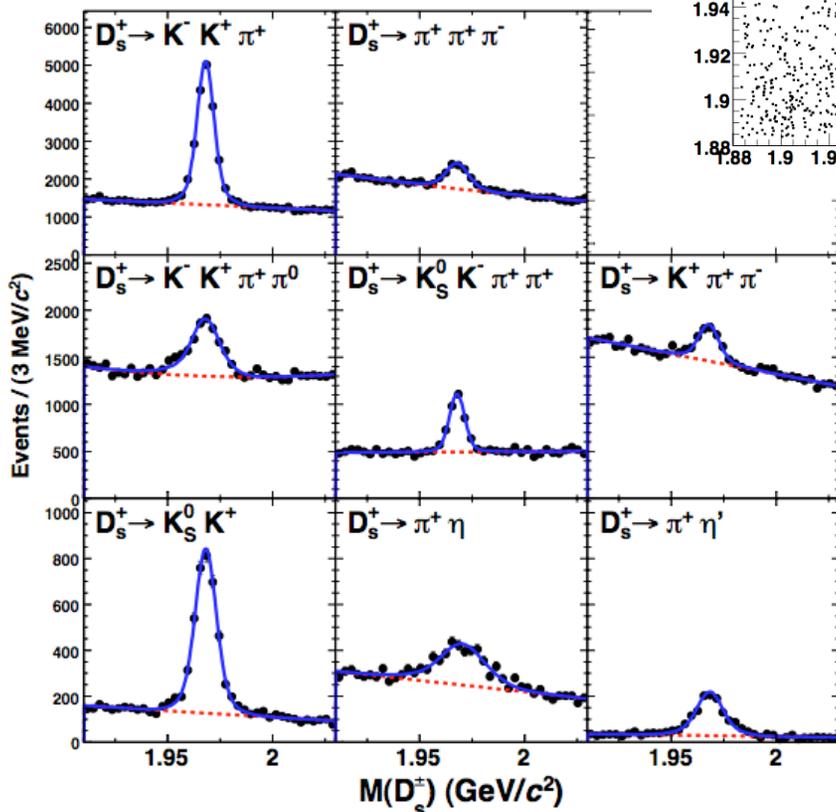
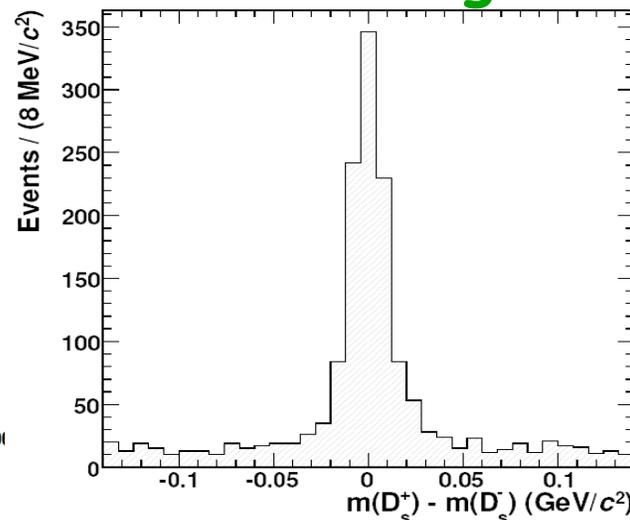
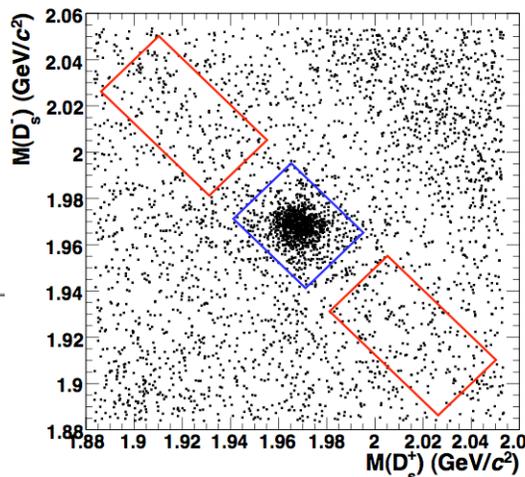
D_s Branching Ratios

PRL 100, 161804
(2008) 298 pb⁻¹

Data @ $E_{cm} = 4170$ MeV
~1 nb of $D_s^* D_s$

Double tags

Double tags



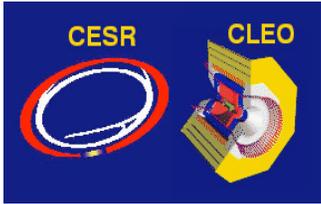
Single tags

Projected $M(D_s^+) - M(D_s^-)$

~1000 double tags

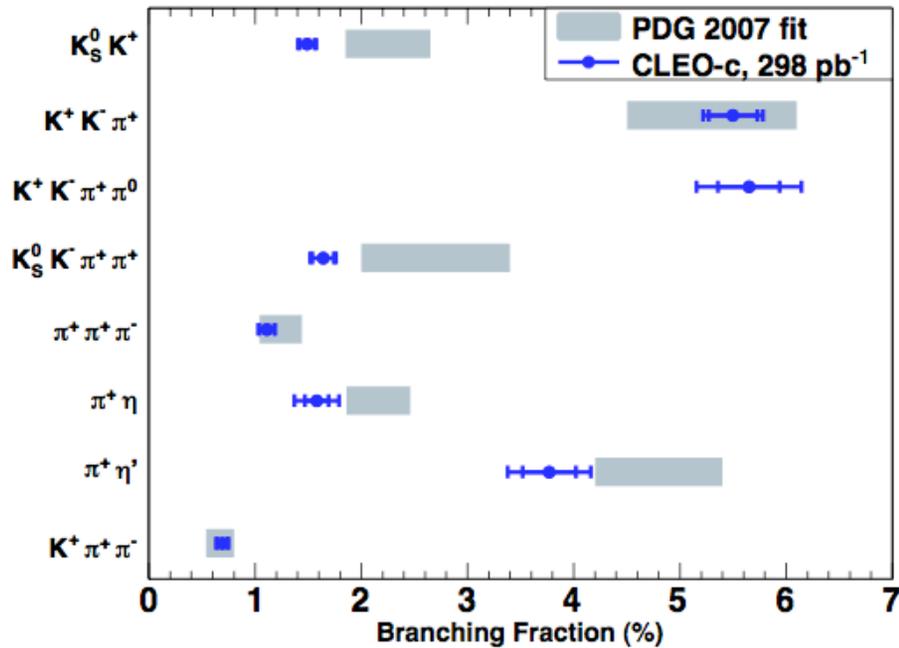
Sets scale of stat. error: ~3.5%

(~1/2 of total dataset)



D_s Branching Ratios

PRL 100, 161804
(2008) 298 pb⁻¹

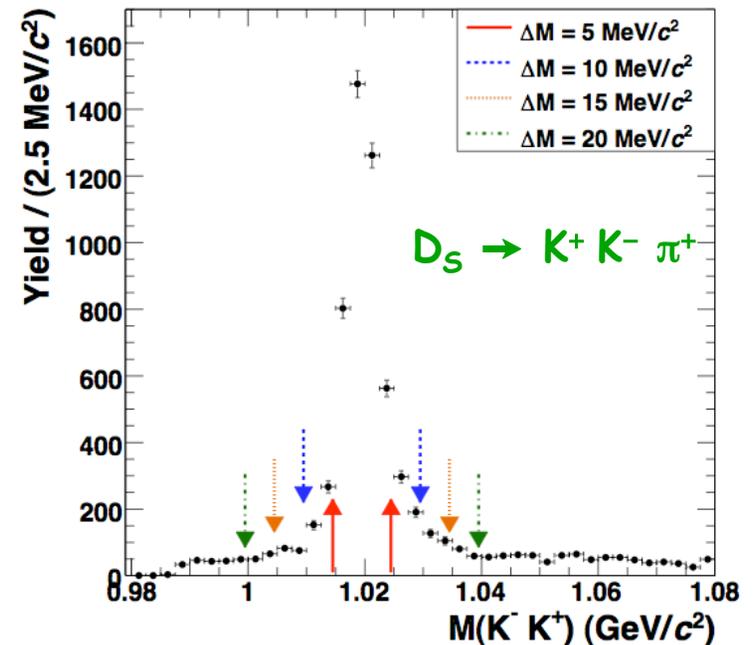


NEW key normalizing mode:
 $B(D_s \rightarrow K^+ K^- \pi^+)$
 $= (5.50 \pm 0.23 \pm 0.16) \%$

$\phi \pi^+$ "Branching fraction" ill-defined

Also quote $B(B \rightarrow K^+ K^- \pi^+)$
 with various $M(K^+ K^-)$ windows:
 $B_{\Delta M}$ for mass within $\pm \Delta M$ of ϕ

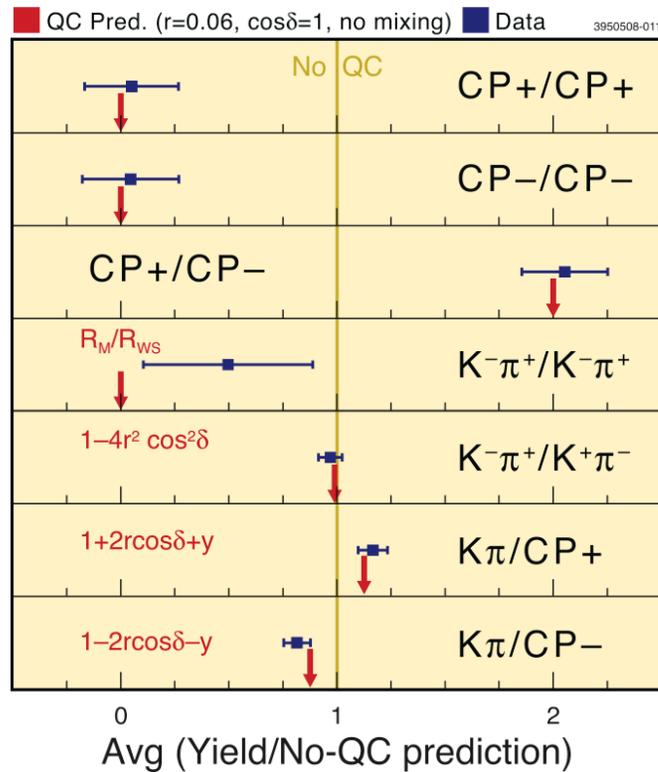
| Value | This result \mathcal{B} (%) |
|--------------------|-------------------------------|
| \mathcal{B}_5 | $1.69 \pm 0.08 \pm 0.06$ |
| \mathcal{B}_{10} | $1.99 \pm 0.10 \pm 0.05$ |
| \mathcal{B}_{15} | $2.14 \pm 0.10 \pm 0.05$ |
| \mathcal{B}_{20} | $2.24 \pm 0.11 \pm 0.06$ |



Quantum Coherence & $K\pi$ phase

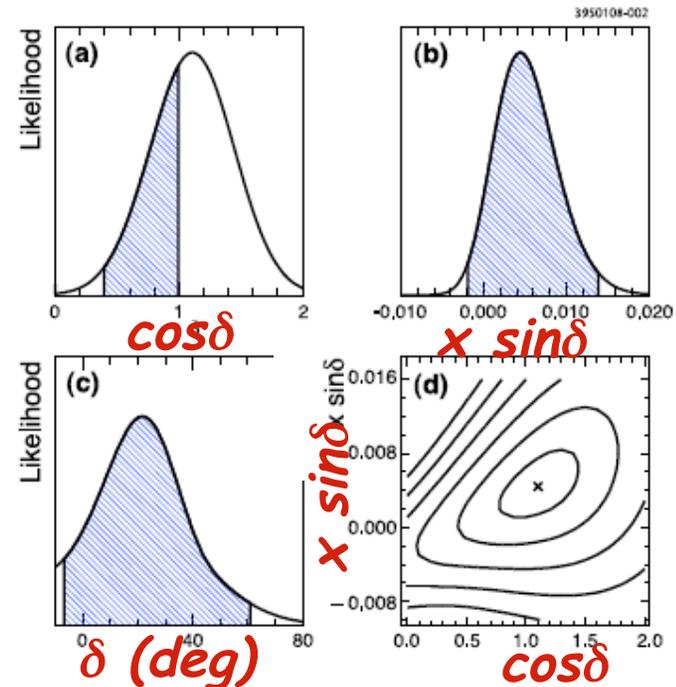
arXiv:0802.2264
 arXiv:0802.2268
 PRL/D to appear
 281 pb⁻¹

Correlated D pairs are produced
 at the $\psi(3770)$:



Allows a measurement of
 strong $K\pi$ FSI phase,
 of great interest for
 D mixing results !

Simultaneous fit to:
 hadronic & semilep modes
 + external mixing inputs:
 (x, y, x'^2, y', r^2)



$$\cos \delta = 1.10 \pm 0.35 \pm 0.07$$

$$\delta = (22^{+11}_{-12} \quad ^{+9}_{-11})^\circ$$

Not Covered...

*Mixing, Dalitz, Spectroscopy:
well-covered in other talks*

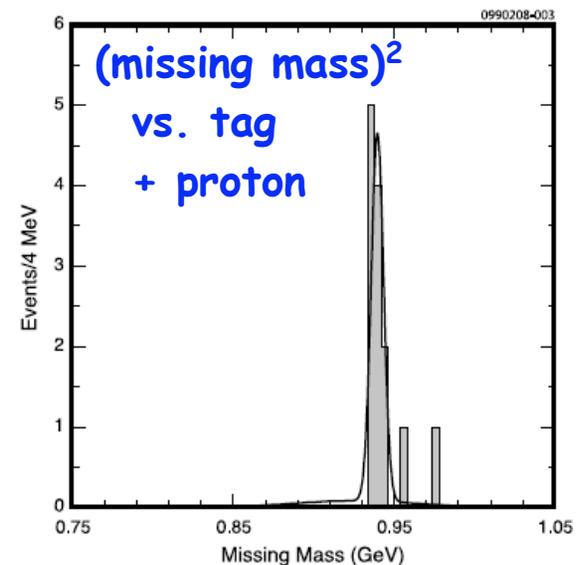
Much other work:

- o CLEO: other hadronic & semileptonic modes
(Cabibbo-suppressed, etc.)*
- o BaBar: $D \rightarrow K l \nu$ (2007, untagged)*
- o Various: CPV searches, Rare decays*
- o etc.*

One "fun" new result:

$$B(D_s \rightarrow p \bar{n}) =$$
$$(1.30 \pm 0.36 +0.12 -0.16) \times 10^{-3}$$

CLEO PRL 100, 181802 (2008)



Conclusions

Tests of Lattice QCD becoming precise

Intriguing disagreement for f_{D_s} ?

Charm threshold best for experimental precision

Outlook

Lattice QCD marches onwards with CPU, techniques, ...

Much existing data left to mine at BaBar, Belle, CLEO

Very soon we will have data at BESIII & LHC-b, ...

Super-B, ... ???

Charm is alive & well

Acknowledgments

Thanks to CLEO collaborators I've borrowed from:

P. Onyisi, M. Shepherd, T. Skwarnicki, S. Stone, W. Sun, ...

& to my Charming BaBar & Belle colleagues:

(S. Prell, Y. Sakai, P. Chang)

Thanks for convenient web pages with results!

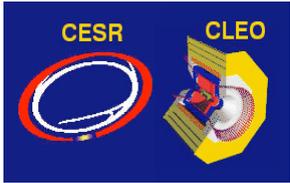
& to my new BESIII collaborators:

Thanks for providing me a future of continuing charm physics...

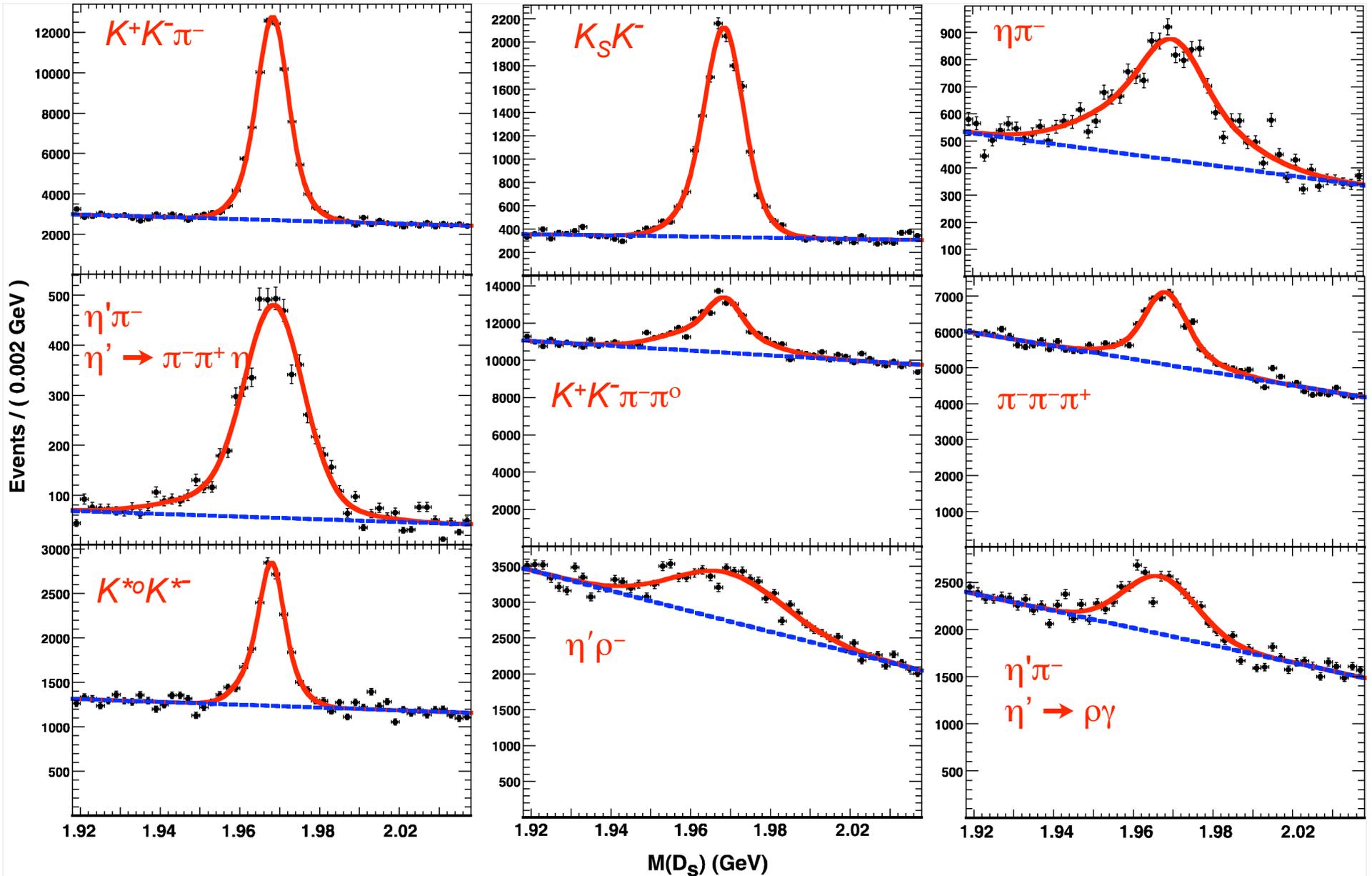
& finally to the HQL08 organizers:

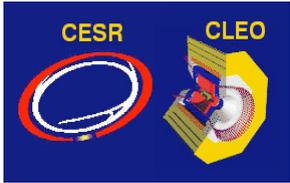
Thanks for the opportunity to speak, and the great conference

BACKUP SLIDES

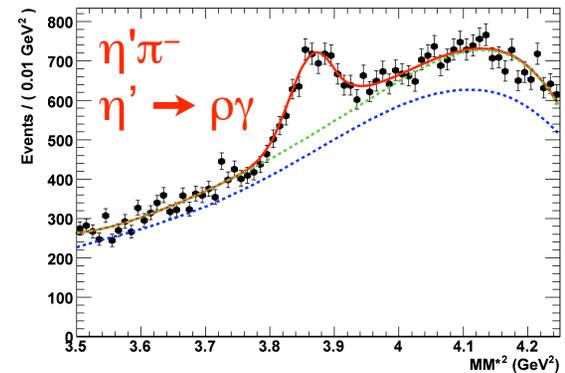
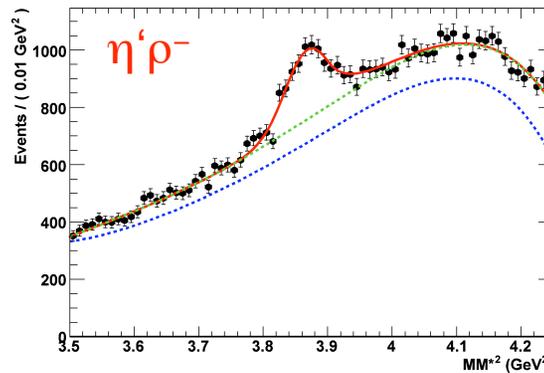
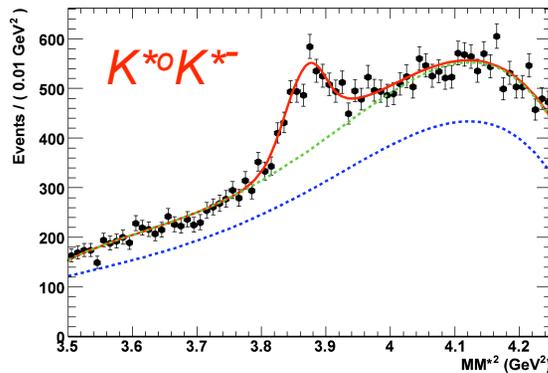
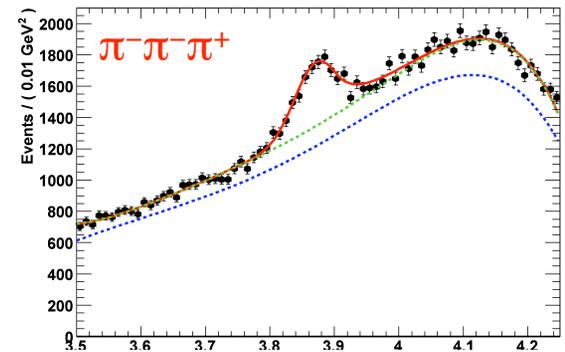
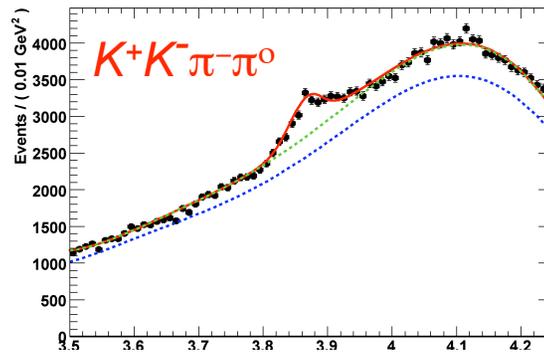
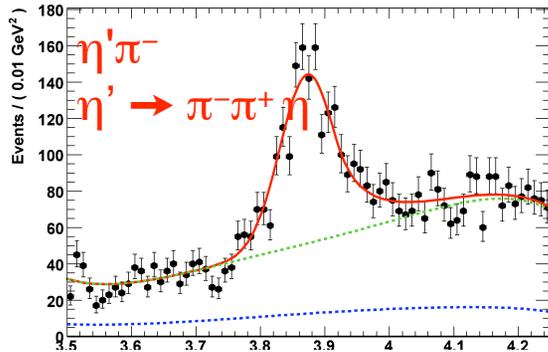
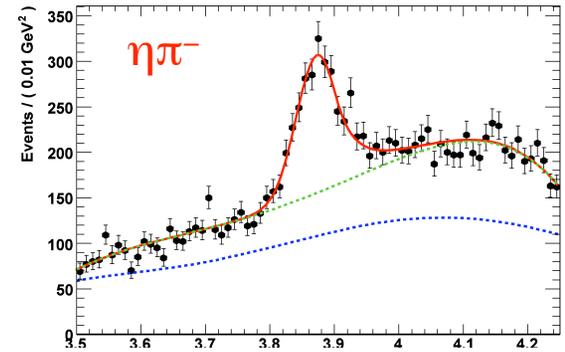
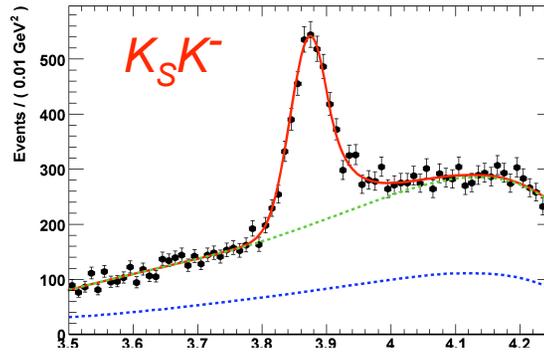
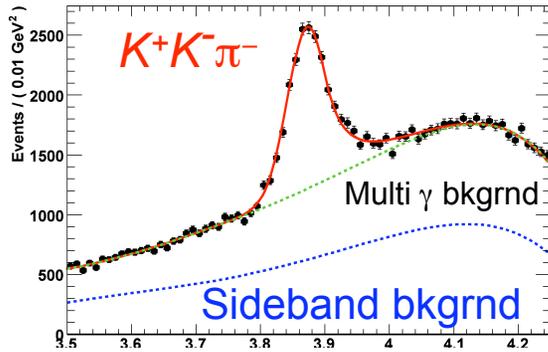


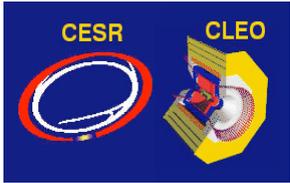
f_{D_s} : D_s Mass Peaks



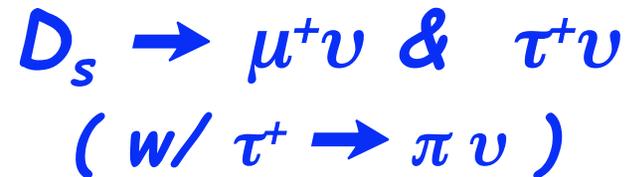


$f_{D_s}: D_s \gamma$ (Missing Mass) ²



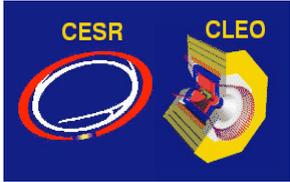


Systematics on BF



| Source of Error | % |
|--------------------------------------|------------|
| Finding the μ^+ track | 0.7 |
| Min. ionization of μ^+ in EM cal | 1.0 |
| Particle identification of μ^+ | 1.0 |
| MM ² width | 0.2 |
| Extra showers in event > 250 MeV | 0.4 |
| Background | 0.7 |
| Number of single tag D^+ | 0.6 |
| Total | 2.2 |

| Source of Error | % |
|------------------------------------|------------|
| Finding the μ^+ track | 0.7 |
| Particle identification of μ^+ | 1.0 |
| MM ² width | 0.2 |
| Extra showers with > 300 MeV | 0.4 |
| Background | 0.5 |
| Number of single tag D_s^- | 3.0 |
| Total | 3.3 |



D^0, D^+ Branching Fractions

Single Tags: $N_j = N_{DD} \mathcal{B}_j \varepsilon_j$

Double Tags: $N_{ij} = N_{DD} \mathcal{B}_i \mathcal{B}_j \varepsilon_{ij}$

$$\mathcal{B}_i = N_{ij} \varepsilon_j / N_j \varepsilon_{ij}$$

$$N_{DD} = N_i N_j \varepsilon_{ij} / N_{ij} \varepsilon_i \varepsilon_j$$

Key points:

\mathcal{B} independent of N_{DD} (usual Achilles' heel)

$\varepsilon_j / \varepsilon_{ij} \sim \varepsilon_i$: \sim independent of tag j

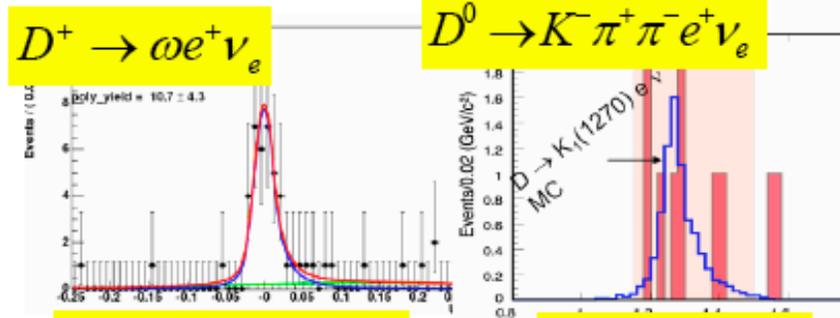
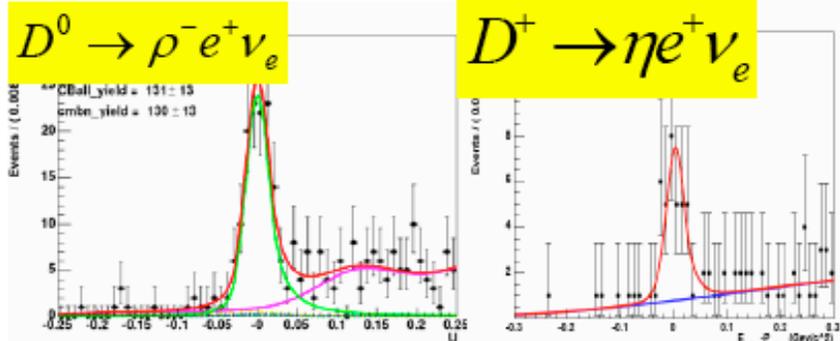
Systematics:

-- *Study efficiencies with tag data*



CLEO-c semileptonic tagging analysis technique: big impact

1st Observations:



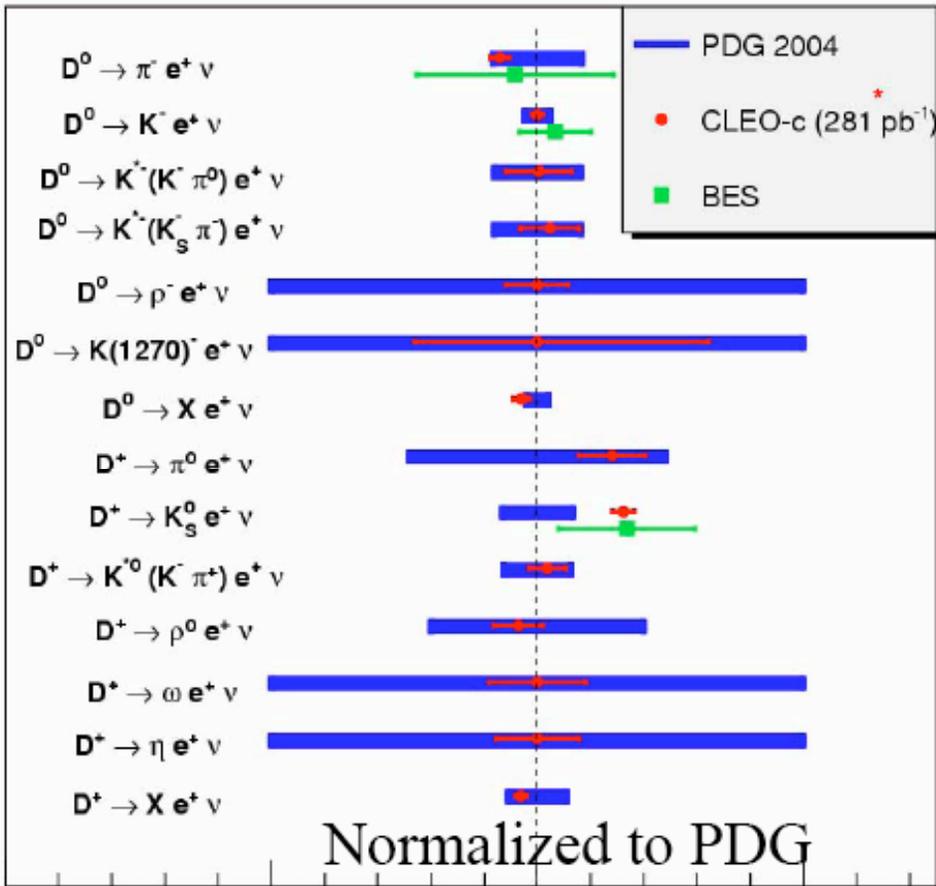
$D^+ / D^0 \rightarrow X e^+ \nu_e$

$D \rightarrow K^* e^+ \nu_e$
form factors

$D \rightarrow K / \pi e^+ \nu_e$
BFs 56/pb

References:
PRL 95, 181801 (2005);
PRL 95, 181802 (2005)
PRL. 99, 191801 (2007)

Precision Measurements:



$D \rightarrow K / \pi e^+ \nu$ branching fractions are for 56/pb
CLEO's measurements most precise for ALL modes; 4 modes observed for the first time



$D \rightarrow K l \nu$

PRD 76, 052005
(2007) 75 fb⁻¹

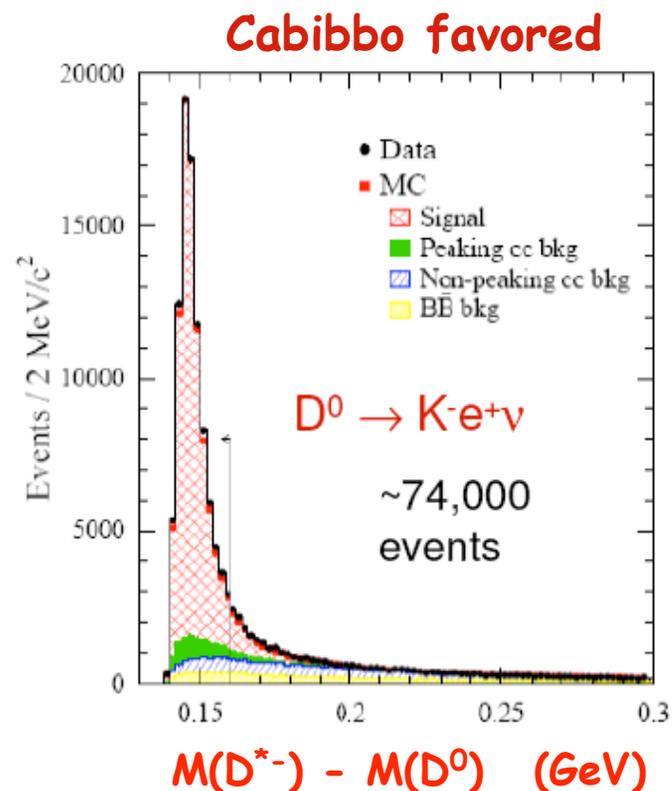
Neutrino "reconstruction" technique

Tagged with $D^{*-} \rightarrow D^0 p \pi^-$

Very large signal statistics.

Compared to CLEO-c results:

- Factor ~300 more luminosity
- Factor ~5 more signal events
- Normalization to $BR(D^0 \rightarrow K^- \pi^+)$ [determined by CLEO-c]
- Poor q^2 resolution (unfolding needed for form factor measurements)
- Much worse signal/noise (method not suitable for Cabibbo suppressed decays)



Interference in $K_L \pi$, $K_S \pi$

D Decay diagrams source both K^0 and $K^0\text{bar}$

⇒ These interfere in physical K_L , K_S final states: K_S, K_L asymmetry

$$R(D) = [B(D \Rightarrow K_S \pi) - B(D \Rightarrow K_L \pi)] / [B(D \Rightarrow K_S \pi) + B(D \Rightarrow K_L \pi)]$$

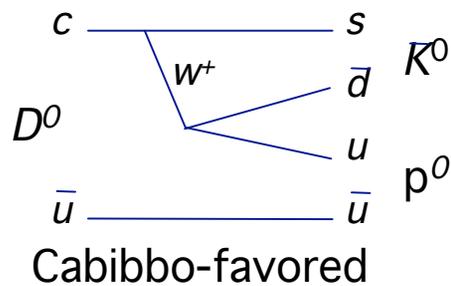
Bigi & Yamamoto [PLB 349, 363 (1995)]

D^0 : expect BF asymmetry of:

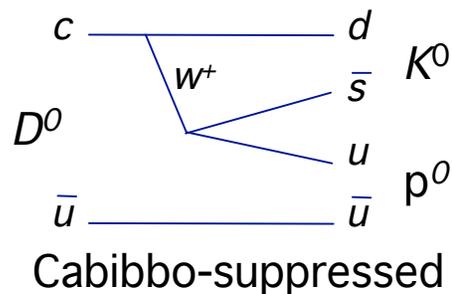
$$R(D^0) = 2 \tan^2 \theta_c \sim 10\%$$

D^+ : more diagrams to consider...

$R(D^+)$ see next page...



$$\bar{K}^0 = \frac{1}{\sqrt{2}} (K_S^0 - K_L^0)$$

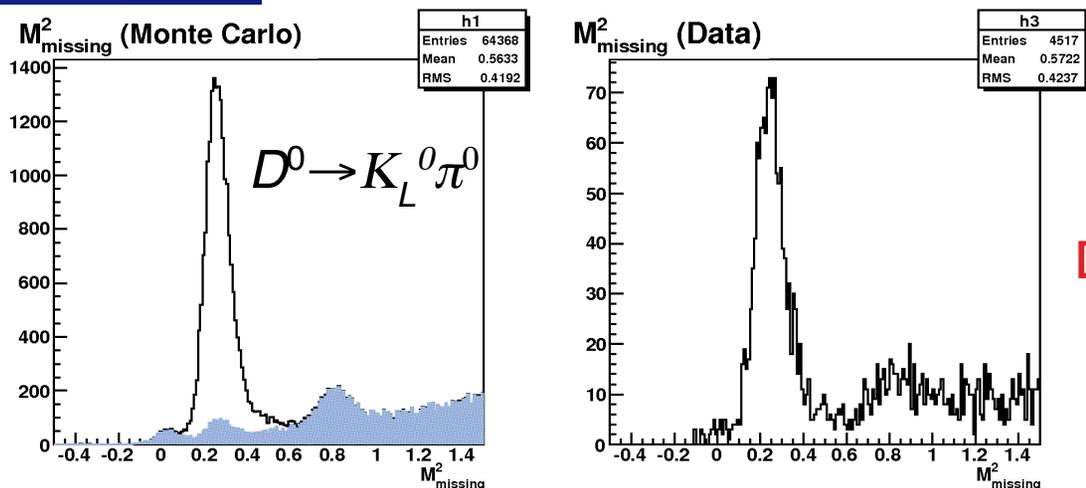


$$K^0 = \frac{1}{\sqrt{2}} (K_S^0 + K_L^0)$$



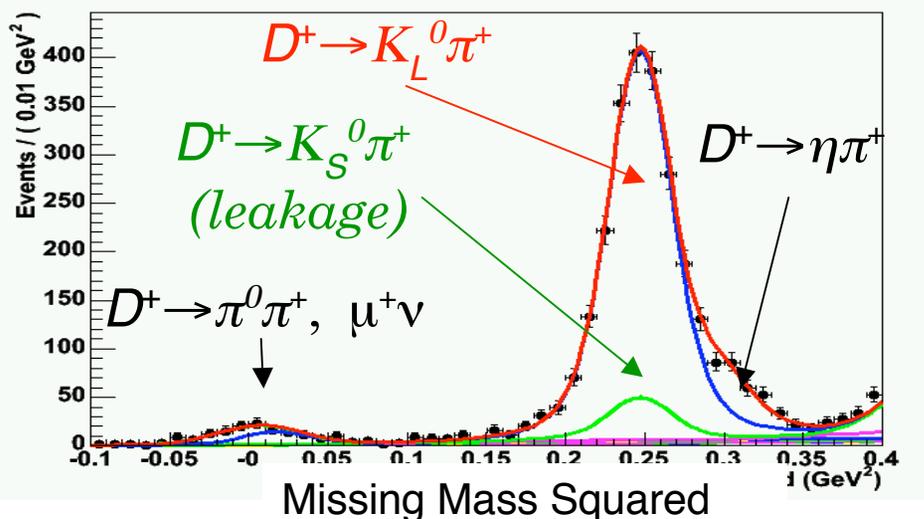
Interference in $K_L \pi$, $K_S \pi$

PRL 100, 091801
(2008) 281 pb⁻¹



Missing Mass Squared

D^0 : $R_D = 0.108 \pm 0.025 \pm 0.024$
(consistent with $2 \tan^2 \theta_C$)



Missing Mass Squared

D^+ : $R_D = 0.022 \pm 0.016 \pm 0.018$

Dao-Neng Gao predicts:
 $R(D^+) = 0.035$ to 0.044
(arXiv:hep-ph/0610389v2)

J. Rosner, CHARM2007:
 $R(D^+) = 0.067 \pm 0.007$