

# Symmetries in two-Higgs-doublet models

**João P. Silva**

**ISEL & CFTP**

# Why I got interested

- There is no reason why there should be only one Higgs doublet

**==> this is an experimental question**

- Take n Higgs. Even in the Higgs potential alone

$$V_H = Y_{ab}(\Phi_a^\dagger \Phi_b) + \frac{1}{2}Z_{ab,cd}(\Phi_a^\dagger \Phi_b)(\Phi_c^\dagger \Phi_d),$$

there are

$$n^2 + \frac{n^2(n^2+1)}{2} = \frac{n^2(n^2+3)}{2} \quad (2, 14, 54, \dots)$$

parameters.

# Why I got interested

- **Cut the number of parameters through symmetries. What are the range of possibilities?**
- **What is the role of basis transformations?**
- **What about CP?**

## Collaborations with

- **Pedro Ferreira**
- **Luís Lavoura**
- **Howard Haber**
- **Markos Maniatis**
- **Otto Nachtmann**

## and discussions with

- **Igor Ivanov**
- **Celso Nishi**
- ...

# Main ideas

- **What are Generalized CP (GCP) symmetries?**
- **GCP in the scalar potential**
- **Extend GCP to the quark sector**  
**=> only one single implementation is possible**  
**=> unique model**
- **Unique model displays a new type of spontaneous CPV**
- **Model is under stress!**

# The scalar sector of the THDM

$$\begin{aligned} V_H = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[ m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{H.c.} \right] \\ & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \left[ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 (\Phi_1^\dagger \Phi_1) (\Phi_1^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2) (\Phi_1^\dagger \Phi_2) + \text{H.c.} \right], \end{aligned}$$

**14 parameters**

$$V_H = Y_{ab} (\Phi_a^\dagger \Phi_b) + \frac{1}{2} Z_{ab,cd} (\Phi_a^\dagger \Phi_b) (\Phi_c^\dagger \Phi_d),$$

$$\begin{aligned} Y_{ab} &= Y_{ba}^*, \\ Z_{ab,cd} &\equiv Z_{cd,ab} = Z_{ba,dc}^*. \end{aligned}$$

# Basis transformations

$$\Phi_a \rightarrow \Phi'_a = U_{ab} \Phi_b,$$

$$v_a \rightarrow v'_a = U_{ab} v_b.$$

$$Y_{ab} \rightarrow Y'_{ab} = U_{a\alpha} Y_{\alpha\beta} U_{b\beta}^* = (U Y U^\dagger)_{ab},$$
$$Z_{ab,cd} \rightarrow Z'_{ab,cd} = U_{a\alpha} U_{c\gamma} Z_{\alpha\beta,\gamma\delta} U_{b\beta}^* U_{d\delta}^*,$$

**(14 – 3) = 11 parameters**

# Higgs-family (HF) symmetries

$$\Phi_a \rightarrow \Phi_a^S = S_{ab} \Phi_b,$$

$$Y_{ab} = S_{a\alpha} Y_{\alpha\beta} S_{b\beta}^*,$$

$$Z_{ab,cd} = S_{a\alpha} S_{c\gamma} Z_{\alpha\beta,\gamma\delta} S_{b\beta}^* S_{d\delta}^*.$$

**Example:**

$$Z_2 : \quad \Phi_1 \rightarrow \Phi_1, \quad \Phi_2 \rightarrow -\Phi_2,$$

$$\begin{aligned} V_H = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[ m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{H.c.} \right] \\ & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \left[ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 (\Phi_1^\dagger \Phi_1) (\Phi_1^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2) (\Phi_1^\dagger \Phi_2) + \text{H.c.} \right], \end{aligned}$$



# Higgs-family (HF) symmetries and basis transformations

$$\begin{aligned}\Phi_1 &= \frac{1}{\sqrt{2}} (\Phi'_1 + \Phi'_2), & \Rightarrow & \frac{1}{\sqrt{2}} (\Phi'_1 + \Phi'_2) \rightarrow \frac{1}{\sqrt{2}} (\Phi'_1 + \Phi'_2), \\ \Phi_2 &= \frac{1}{\sqrt{2}} (\Phi'_1 - \Phi'_2). & & \frac{1}{\sqrt{2}} (\Phi'_1 - \Phi'_2) \rightarrow -\frac{1}{\sqrt{2}} (\Phi'_1 - \Phi'_2),\end{aligned}$$

$$\Pi_2 : \quad \Phi'_1 \leftrightarrow \Phi'_2,$$

$$\begin{aligned}V_H &= m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[ m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{H.c.} \right] \\ &+ \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ &+ \left[ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \underbrace{\lambda_6 (\Phi_1^\dagger \Phi_1) (\Phi_1^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2) (\Phi_1^\dagger \Phi_2)}_{\lambda_6 = \lambda_7^*} + \text{H.c.} \right],\end{aligned}$$

Real ↗  
↘ Real

# Higgs-family (HF) symmetries and basis transformations

symmetry	$m_{11}^2$	$m_{22}^2$	$m_{12}^2$	$\lambda_1$	$\lambda_2$	$\lambda_3$	$\lambda_4$	$\lambda_5$	$\lambda_6$	$\lambda_7$
$Z_2$			0						0	0
$\Pi_2$		$m_{11}^2$	real		$\lambda_1$			real		$\lambda_6^*$

- **These two models are the same but viewed in two different basis**
- **Obviously, they make the same physical predictions; we say that they are in the same class**

# Higgs-family (HF) symmetries and basis transformations

The symmetry

$$\Phi_a \rightarrow \Phi_a^S = S_{ab}\Phi_b,$$

Under the basis change

$$\Phi'_a = U_{a\alpha}\Phi_\alpha$$

Transforms into

$$S' = USU^\dagger$$

$\Rightarrow$

$$S' = \begin{pmatrix} e^{-i\theta_1} & 0 \\ 0 & e^{i\theta_1} \end{pmatrix}$$

# The usual CP transformation

$$\Phi_a(t, \vec{x}) \rightarrow \Phi_a^{\text{CP}}(t, \vec{x}) = \Phi_a^*(t, -\vec{x}),$$

$$\begin{aligned} (\Phi_1)^{\text{CP}} &= (\Phi_1)^*, \\ (\Phi_2)^{\text{CP}} &= (\Phi_2)^*. \end{aligned}$$

# CP and basis transformations: General CP Transformations (GCP)

$$\begin{aligned}\Phi_1 &= \frac{1}{\sqrt{2}} \Phi'_1 + \frac{1}{\sqrt{2}} e^{i\pi/4} \Phi'_2, \\ \Phi_2 &= -\frac{1}{\sqrt{2}} e^{-i\pi/4} \Phi'_1 + \frac{1}{\sqrt{2}} \Phi'_2.\end{aligned}$$

$$\begin{aligned}\frac{1}{\sqrt{2}} (\Phi'_1)^{\text{CP}} + \frac{1}{\sqrt{2}} e^{i\pi/4} (\Phi'_2)^{\text{CP}} &= \frac{1}{\sqrt{2}} (\Phi'_1)^* + \frac{1}{\sqrt{2}} e^{-i\pi/4} (\Phi'_2)^* \\ -\frac{1}{\sqrt{2}} e^{-i\pi/4} (\Phi'_1)^{\text{CP}} + \frac{1}{\sqrt{2}} (\Phi'_2)^{\text{CP}} &= -\frac{1}{\sqrt{2}} e^{i\pi/4} (\Phi'_1)^* + \frac{1}{\sqrt{2}} (\Phi'_2)^*,\end{aligned}$$

$$\begin{aligned}(\Phi'_1)^{\text{CP}} &= \frac{1+i}{2} (\Phi'_1)^* - \frac{i}{\sqrt{2}} (\Phi'_2)^*, \\ (\Phi'_2)^{\text{CP}} &= -\frac{i}{\sqrt{2}} (\Phi'_1)^* + \frac{1-i}{2} (\Phi'_2)^*.\end{aligned}$$

Lee & Wick, PR 148, 1385 (1966)

**This is NOT the usual type of CP transformation**

# CP and basis transformations: General CP Transformations (GCP)

We **MUST** consider **GCP** transformations

$$\Phi_a \rightarrow \Phi_a^{\text{GCP}} = X_{a\alpha} \Phi_\alpha^*$$

Under the basis change

$$\Phi'_a = U_{a\alpha} \Phi_\alpha$$

The **GCP** transformation is changed according to:

$$X' = UXU^T.$$

$$\Rightarrow X' = UXU^T = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \quad \boxed{0 \leq \theta \leq \pi/2}$$

Ecker, Grimus & Neufeld JPA 20, L807 (1987)

# How many classes of symmetry-constrained potentials are there?

Invariance under some

$$\Phi_a \rightarrow S_{ab}\Phi_b,$$

and/or invariance under some

$$\Phi_a \rightarrow X_{ab}\Phi_b^*,$$

# The 6 types of THDM scalar potentials

symmetry	$m_{11}^2$	$m_{22}^2$	$m_{12}^2$	$\lambda_1$	$\lambda_2$	$\lambda_3$	$\lambda_4$	$\lambda_5$	$\lambda_6$	$\lambda_7$	$n_{\text{parameters}}$
$Z_2$			0						0	0	7
$U(1)$			0					0	0	0	6
$U(2)$		$m_{11}^2$	0	$\lambda_1$			$\lambda_1 - \lambda_3$	0	0	0	3
CP1			real					real	real	real	9
CP2		$m_{11}^2$	0	$\lambda_1$						$-\lambda_6$	5
CP3		$m_{11}^2$	0	$\lambda_1$			$\lambda_1 - \lambda_3 - \lambda_4$ (real)		0	0	4

Ivanov, PRD 77, 015017 (2008)

Ferreira, Haber & JPS, PRD 79, 116004 (2009)

$$CP1 : \quad X = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix},$$

$$CP2 : \quad X = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix},$$

$$CP3 : \quad X = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

$$Z_2 : \quad S = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix},$$

$$U(1) : \quad S = \begin{pmatrix} e^{i\alpha} & 0 \\ 0 & e^{-i\alpha} \end{pmatrix}_{\alpha \neq \pi/2}$$



# Extending GCP into the Yukawa terms

## Yukawa Lagrangian

$$-\mathcal{L}_Y = \bar{q}_L(\Gamma_1\Phi_1 + \Gamma_2\Phi_2)n_R + \bar{q}_L(\Delta_1\tilde{\Phi}_1 + \Delta_2\tilde{\Phi}_2)p_R + \text{H.c.},$$

## GCP transformations for fermions

$$\begin{aligned}q_L &\rightarrow X_\alpha\gamma^0 C q_L^*, \\n_R &\rightarrow X_\beta\gamma^0 C n_R^*, \\p_R &\rightarrow X_\gamma\gamma^0 C p_R^*,\end{aligned}$$

Use  $X' = UXU^T$  and Ecker, Grimus, Neufeld to write:

$$X_\alpha = \begin{bmatrix} c_\alpha & s_\alpha & 0 \\ -s_\alpha & c_\alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad \text{Block structure}$$

where  $0 \leq \alpha \leq \pi/2$ , and similarly for  $X_\beta$  and  $X_\gamma$ .

# Extending GCP into the Yukawa terms

Forcing this GCP onto the Yukawa Lagrangian gives:

$$\begin{aligned}X_\alpha \Gamma_1^* - (c_\theta \Gamma_1 - s_\theta \Gamma_2) X_\beta &= 0, \\X_\alpha \Gamma_2^* - (s_\theta \Gamma_1 + c_\theta \Gamma_2) X_\beta &= 0.\end{aligned}$$

\* This gives us

2 equations/matrices X 9 entries X 2 complex  
= 36 equations in 36 unknowns

\* Block structure means that we can separate problem into  $m_n$ ,  $m_3$ ,  $3_n$ , and  $3_3$  blocks ( $m, n=1, 2$ ).

# Extending GCP into the Yukawa terms

Simplest block is 33:

$$\begin{aligned}
 X_\alpha \Gamma_1^* - (c_\theta \Gamma_1 - s_\theta \Gamma_2) X_\beta &= 0, \\
 X_\alpha \Gamma_2^* - (s_\theta \Gamma_1 + c_\theta \Gamma_2) X_\beta &= 0.
 \end{aligned}$$

$$\begin{aligned}
 (\Gamma_1)_{33}^* - c_\theta (\Gamma_1)_{33} + s_\theta (\Gamma_2)_{33} &= 0, \\
 (\Gamma_2)_{33}^* - s_\theta (\Gamma_1)_{33} - c_\theta (\Gamma_2)_{33} &= 0.
 \end{aligned}$$

$$\begin{aligned}
 \begin{bmatrix} 1 - c_\theta & s_\theta \\ -s_\theta & 1 - c_\theta \end{bmatrix} \begin{bmatrix} \text{Re}(\Gamma_1)_{33} \\ \text{Re}(\Gamma_2)_{33} \end{bmatrix} &= 0, & \det &= 2(1 - c_\theta), \\
 \begin{bmatrix} 1 + c_\theta & -s_\theta \\ s_\theta & 1 + c_\theta \end{bmatrix} \begin{bmatrix} \text{Im}(\Gamma_1)_{33} \\ \text{Im}(\Gamma_2)_{33} \end{bmatrix} &= 0, & \det &= 2(1 + c_\theta) \neq 0
 \end{aligned}$$

# Extending GCP into the Yukawa terms

## Conclusions:

CP2:  $\theta = \pi/2$

$\Gamma_a$ matrix element	component	condition for vanishing determinant
33	Im	impossible
	Re	$\theta = 0$
13, 23	Im	$\alpha = \theta = \pi/2$
	Re	$\alpha = \theta$
31, 32	Im	$\beta = \theta = \pi/2$
	Re	$\beta = \theta$
11, 12, 21, 22	Im	$\theta = \pi - \alpha - \beta$
	Re	$\theta = \alpha + \beta$ or $\theta = \alpha - \beta$ or $\theta = \beta - \alpha$

$$\Gamma_{1_{33}} = \Gamma_{2_{33}} = 0$$

Block vanishes if  
 $\alpha \neq \theta = \pi/2$

Block vanishes if  
 $\beta \neq \theta = \pi/2$

Block vanishes if  
 $\alpha = \beta = \theta = \pi/2$

**==> All  $\theta = \pi/2$  cases imply vanishing determinant**

**==> one zero down-type quark mass (& up-type & charged lepton)**

**==> We cannot extend CP2 to the quark sector**

# The single surviving model

\* Perform a similar analysis for CP3 ( $0 < \theta < \pi/2$ )

==> There is one single way to extend CP3 to the quark sector consistent with non-vanishing quark masses!!

==> One must have  $\alpha = \beta = \theta = \pi/3$  and

$$\Gamma_1 \rightarrow \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{12} & -a_{11} & a_{23} \\ a_{31} & a_{32} & 0 \end{bmatrix},$$

$$\Gamma_2 \rightarrow \begin{bmatrix} a_{12} & -a_{11} & -a_{23} \\ -a_{11} & -a_{12} & a_{13} \\ -a_{32} & a_{31} & 0 \end{bmatrix},$$

6 real parameters

# Fit to experiment

- The model is CP conserving.  
**==> There is also no exact CP3 model**  
CPV is accommodated by breaking CP3 softly (later...)
- With the CPV vacuum phase there are in principle 15 parameters
  - 6 real parameters from down Yukawa
  - 6 real parameters from up Yukawa
  - 2 vevs
  - 1 vacuum phase
- Fit to 11 observables
  - 3 + 3 quark masses
  - 3 + 1 CKM parameters
  - $v^2$

# Fit to experiment

$$\begin{aligned}
 a_{11} &= 4.6927 \times 10^{-6}, & a_{12} &= -5.9799 \times 10^{-4}, \\
 a_{13} &= -2.32 \times 10^{-2}, & a_{23} &= -6.6 \times 10^{-3}, \\
 a_{31} &= -8.815 \times 10^{-5}, & a_{32} &= 5.1193 \times 10^{-6},
 \end{aligned}$$

$$v_1 = 173.944, \quad v_2 \cos \delta = -0.8467 \quad v_2 \sin \delta = -0.9565$$

$$\begin{aligned}
 b_{11} &= 7.3 \times 10^{-3}, & b_{12} &= 7.6445 \times 10^{-5}, \\
 b_{13} &= 9.578 \times 10^{-1}, & b_{23} &= 2.325 \times 10^{-1}, \\
 b_{31} &= 1.3446 \times 10^{-4}, & b_{32} &= 5.9491 \times 10^{-4},
 \end{aligned}$$



$$\begin{aligned}
 m_d &= 0.00298, & m_s &= 0.10511, & m_b &= 4.19701, \\
 m_u &= 0.00200, & m_c &= 1.27439, & m_t &= 171.451,
 \end{aligned}$$

$$|V| = \begin{bmatrix} 0.97430 & 0.22521 & 0.00339 \\ 0.22516 & 0.97348 & 0.04039 \\ 0.00579 & 0.04011 & 0.99918 \end{bmatrix}.$$

$$0.00874^{+0.00026}_{-0.00037}$$

PDG (2008)

**==> Good agreement with PDG**  
**Except  $V_{td}$**

# What about FCNC?

- **The model does have FCNC**
- **Maybe suppressed by making scalar masses large enough and/or couplings small enough**
  - **15 parameters for 11 observables**
- **Otherwise, redo the analysis leading to CKM extraction**



# CP Violation in the 6 types of THDM scalar potentials

symmetry	exact		softly-broken	
	explicit CPV	spontaneous CPV	explicit CPV	spontaneous CPV
$Z_2$	–	–	Yes	Yes
$U(1)$	–	–	–	–
$U(2)$	–	–	–	–
CP1	–	Yes	Yes	Yes
CP2	–	–	Yes	Yes
CP3	–	–	–	–

TDLee, PRD 8, 1226 (1973)

Branco & Rebelo, PLB 160, 117 (1985)

Ferreira, Maniatis, Nachtmann & JPS, JHEP08 (2010) 125

# The lagrangian does not have explicit CPV

$$\begin{aligned} V_H = & m^2 \left[ \Phi_1^\dagger \Phi_1 + \Phi_2^\dagger \Phi_2 \right] \\ & + \frac{1}{2} \lambda_1 \left[ (\Phi_1^\dagger \Phi_1)^2 + (\Phi_2^\dagger \Phi_2)^2 \right] + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \frac{1}{2} (\lambda_1 - \lambda_3 - \lambda_4) \left[ (\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2 \right] \\ & + \Delta m^2 \left[ \Phi_1^\dagger \Phi_1 - \Phi_2^\dagger \Phi_2 \right] - m_{12}^2 \left[ \Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1 \right], \end{aligned} \quad \left. \vphantom{V_H} \right\} \text{CP3}$$

→ soft-breaking of CP3

- $m_{12}^2$  (hence,  $V_H$ ) kept real by imposing also CP1
- all Yukawa couplings real

**==> Lagrangian preserves CP**

**==> This is not SM-like CPV**

# The scalar sector of the model does not have spontaneous CPV

## Proofs:

- **Bilinears**

Ferreira, Maniatis, Nachtmann & JPS, JHEP08 (2010) 125

- **Calculate the basis invariant signals of CPV after SEwkSB –  $J_1$ ,  $J_2$ , and  $J_3$  – of**

Lavoura & JPS, PRD 50, 4619 (1994)

Botella & JPS, PRD 51, 3870 (1995)

- **Go to the Higgs basis and count independent phases**

Ferreira & JPS, arXiv:1001.0574, EPJC (in print)

# The Higgs basis

Do

$$\Phi_a = U_{ab} H_b \quad U^\dagger = \frac{1}{v} \begin{bmatrix} v_1 & v_2 e^{-i\delta} \\ v_2 & -v_1 e^{-i\delta} \end{bmatrix}$$

As a result

$$H_1 = \begin{bmatrix} G^+ \\ (v + H^0 + iG^0)/\sqrt{2} \end{bmatrix}, \quad H_2 = \begin{bmatrix} H^+ \\ (R + iI)/\sqrt{2} \end{bmatrix}$$

**arbitrary phase**  
**vevless**

# The Higgs basis

==>

$$\begin{aligned} V_H = & \bar{m}_{11}^2 H_1^\dagger H_1 + \bar{m}_{22}^2 H_2^\dagger H_2 - \left[ \bar{m}_{12}^2 H_1^\dagger H_2 + \text{H.c.} \right] + \frac{1}{2} \bar{\lambda}_1 (H_1^\dagger H_1)^2 + \frac{1}{2} \bar{\lambda}_2 (H_2^\dagger H_2)^2 \\ & + \bar{\lambda}_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \bar{\lambda}_4 (H_1^\dagger H_2)(H_2^\dagger H_1) + \left[ \frac{1}{2} \bar{\lambda}_5 (H_1^\dagger H_2)^2 + \bar{\lambda}_6 (H_1^\dagger H_1)(H_1^\dagger H_2) \right. \\ & \left. + \bar{\lambda}_7 (H_2^\dagger H_2)(H_1^\dagger H_2) + \text{H.c.} \right]. \end{aligned}$$

**Stationarity conditions ==>**  $2\bar{m}_{12}^2 = \bar{\lambda}_6 v^2$

**Arbitrary phase of  $H_2$**

**==> Signals of CPV are:**  $\text{Im}(\bar{\lambda}_6 \bar{\lambda}_7^*), \text{Im}(\bar{\lambda}_5^* \bar{\lambda}_6^2),$  and  $\text{Im}(\bar{\lambda}_5^* \bar{\lambda}_7^2)$

**Lavoura & JPS, PRD 50, 4619 (1994)**

# The scalar sector of the model does not have spontaneous CPV

Transforming the coefficients of the scalar potential into the Higgs basis, we get

$$-\bar{\lambda}_7 = \bar{\lambda}_6 = \frac{2}{v^4} v_1 v_2 (\lambda_1 - \lambda_3 - \lambda_4) \sin \delta \boldsymbol{\eta}$$

$$\bar{\lambda}_5 = -\frac{1}{v^4} (\lambda_1 - \lambda_3 - \lambda_4) \boldsymbol{\eta}^2$$

$$\boldsymbol{\eta} = -i \left( v_1^2 e^{i\delta} + v_2^2 e^{-i\delta} \right).$$

**==> The scalar sector is CP conserving, even after spontaneous electroweak symmetry breaking**

**==> This is not the usual type of spontaneous CPV**

# The model does have CPV

**Define**

$$\begin{aligned}\sqrt{2} \Gamma_d &= v_1 \Gamma_1 + v_2 e^{i\delta} \Gamma_2, & H_d &= \Gamma_d (\Gamma_d)^\dagger, \\ \sqrt{2} \Delta_u &= v_1 \Delta_1 + v_2 e^{-i\delta} \Delta_2. & H_u &= \Delta_u (\Delta_u)^\dagger.\end{aligned}$$

**Basis invariant source of CPV in W interactions is**

$$\begin{aligned}J &= \text{Tr}[H_u, H_d]^3 = 6i(m_t^2 - m_c^2)(m_t^2 - m_u^2)(m_c^2 - m_u^2) \\ &\times (m_b^2 - m_s^2)(m_b^2 - m_d^2)(m_s^2 - m_d^2) \text{Im}(V_{us}V_{cb}V_{ub}^*V_{cs}^*).\end{aligned}$$

$\propto \sin(\delta)$  Bernabéu, Branco & Gronau, PL 169B, 243 (1986)

**==> The model does have a weird spontaneous CPV**

**\* scalar sector does the deed**

spontaneously break electroweak symmetry

**\* quark sector pays the price**

violates CP

# Open questions

- Are there FCNC?

- Yes.
- FCNC couplings depend on only  $15-11=4$  new parameters
- masses of scalars depend on only 2 (3) more

11  
↑

0  
↑

Lavoura

**==> FCNC are very constrained**



# Open questions

- **After Lavoura**
  - Fitting [quark masses] allows for large scalar masses
  - BUT, fitting [quark masses + CKM] forces one small scalar mass
- **This problem goes away if you take a complex soft-CP3 breaking term**
  - Good fits to four of
    - KK mixing
    - $\epsilon_K$
    - BB mixing
    - BsBs mixing
    - $\sin(2\beta)$

# Open questions

- **Are there other models with this new type of spontaneous CPV?**
  - we have built 3HDM like this
  - **BUT**
    - they are THDM-like (third vev vanishes)
    - general 3HDM do not seem to exhibit this new type of CPV

# Conclusions

- **It is important to consider Generalized CP transformations/symmetries**
- **The CP2 symmetry cannot be extended to the Yukawa sector in a way consistent with non-zero quark masses**
- **The exact CP3 symmetry cannot be extended to the Yukawa sector in a way consistent with non-zero quark masses and CPV**

# Conclusions

- There is one single softly-broken CP3-symmetric model which can be extended to the Yukawa sector in a way consistent with non-zero quark masses and CPV
- The model is very constrained and may be in trouble (in progress...)
  - If it survives de assault, fine
  - If it does not, we will have proved that there is no possible extension of GCP into the Yukawa sector

# Conclusions

- In any case:

**There is a new type of spontaneous CPV.**

**Search is on for other models of this type.**

**END**