

# **Electron cloud instability measurement at CesarTA**

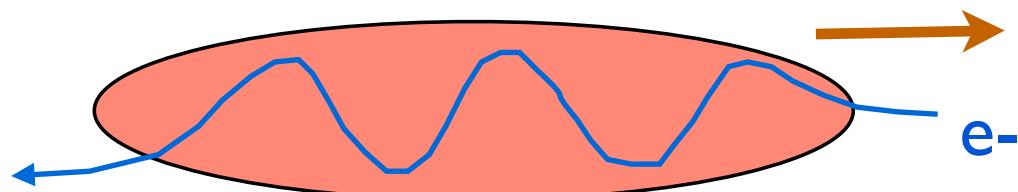
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CesarTA meeting  
5 August 2009

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- Strong head-tail instability
- Incoherent emittance growth
- Coupled bunch instability

# Coherent strong head-tail instability

- Coherent motion between inner bunch and electron cloud.
- Electrons oscillate electric force inner bunch along z,  
$$\omega_e = \sqrt{\frac{\lambda_p r_e c^2}{\sigma_y (\sigma_x + \sigma_y)}}$$
- The instability is characterized by  $\omega_e \sigma_z / c$ , number of electron oscillation along the bunch.



# Threshold of the strong head-tail instability (Balance of growth and Landau damping)

- Stability condition for  $\omega_e \sigma_z / c > 1$

$$\omega_e = \sqrt{\frac{\lambda_p r_e c^2}{\sigma_y (\sigma_x + \sigma_y)}}$$

$$U = \frac{\sqrt{3} \lambda_p r_0 \beta}{v_s \gamma \omega_e \sigma_z / c} \frac{|Z_\perp(\omega_e)|}{Z_0} = \frac{\sqrt{3} \lambda_p r_0 \beta}{v_s \gamma \omega_e \sigma_z / c} \frac{KQ}{4\pi} \frac{\lambda_e}{\lambda_p} \frac{L}{\sigma_y (\sigma_x + \sigma_y)} = 1$$

- Since  $\rho_e = \lambda_e / 2\pi \sigma_x \sigma_y$ ,

$$\rho_{e,th} = \frac{2\gamma v_s \omega_e \sigma_z / c}{\sqrt{3} K Q r_0 \beta L}$$

Origin of Landau damping is momentum compaction

$$v_s \sigma_z = \alpha \sigma_\delta L$$

- $Q = \min(Q_{nl}, \omega_e \sigma_z / c)$   
 $Q_{nl} = 5-10?$ , depending on the nonlinear interaction.
- $K$  characterizes cloud size effect and pinching.
- $\omega_e \sigma_z / c \sim 12-20$  for damping rings.
- We use  $K = \omega_e \sigma_z / c$  and  $Q_{nl} = 7$  for analytical estimation.

# Parameters for the instability

- Threshold

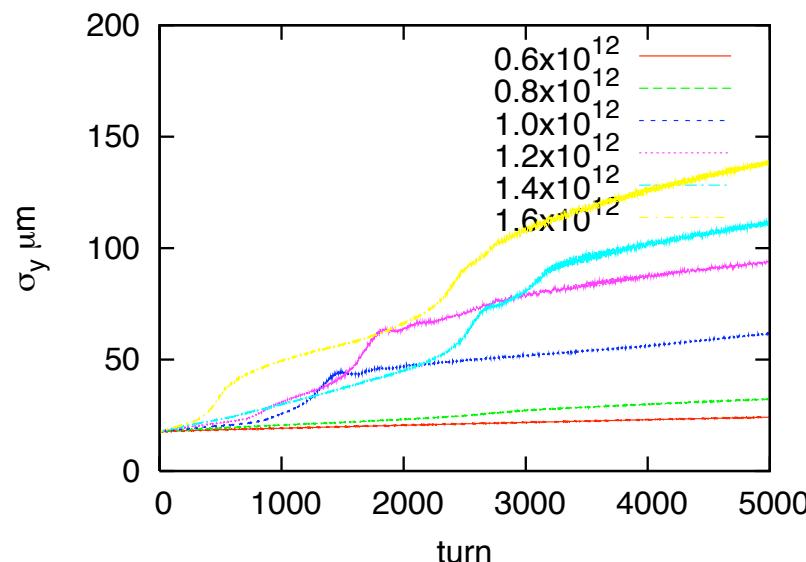
		KEKB	PEP-II	Cesr-TA/5	Cesr-TA/2	ILC-DR
Circumference	$L(\text{m})$	3,016	2,200	768	768	6,414
Energy	$E$	3.5	3.1	5.0	2.1	5.0
Bunch population	$N_+(10^{10})$	8	8	2	2	2
Beam current	$I_+(\text{A})$	1.7	3.0	-	-	0.4
Emittance	$\varepsilon_x(\text{nm})$	18	48	40	2.6	0.5
Momentum compaction	$\alpha(10^{-4})$	3.4		62.0	67.6	4.2
Bunch length	$\sigma_z(\text{mm})$	6	12	15.7	12.2	6
RMS energy spread	$\sigma_E/E(10^{-3})$	0.73		0.94	0.80	1.28
Synchrotron tune	$\nu_s$	0.025	0.025	0.0454	0.055	0.067
Damping time	$\tau_x$	40	40		56.4	26

		KEKB <sup>1</sup>	KEKB <sup>2</sup>	PEP-II	Cesr-TA/5	Cesr-TA/2	ILC-DR
Bunch population	$N_+(10^{10})$	3	8	8	2	2	2
Beam current	$I_+(\text{A})$	0.5	1.7	3.0	-	-	0.4
Bunch spacing	$\ell_{sp}(\text{ns})$	8	7	4	4	4	6
Electron frequency	$\omega_e/2\pi(\text{GHz})$	28	40	15	9.6	43	100
Phase angle	$\omega_e \sigma_z/c$	3.6	5.9	3.7	3.2	11.0	12.6
Threshold	$\rho_e (10^{12} \text{ m}^{-3})$	0.63	0.38	0.77	7.40	1.70	0.19
Tune shift at $\rho_e$	$\Delta\nu_{x+y}$	0.0078	0.0047	0.0078	0.016	0.009	0.011

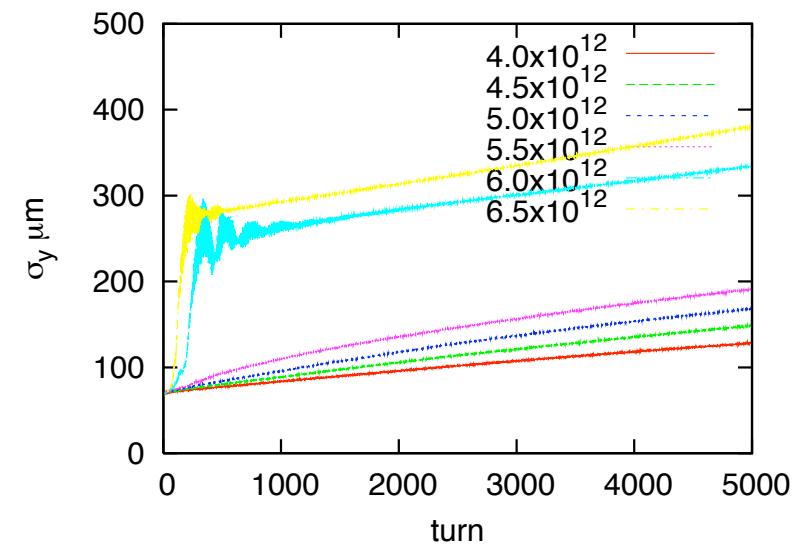
# Simulation of the strong head-tail instability

- Uniform beta model, integration step is  $L/8$ .

2 GeV



5 GeV

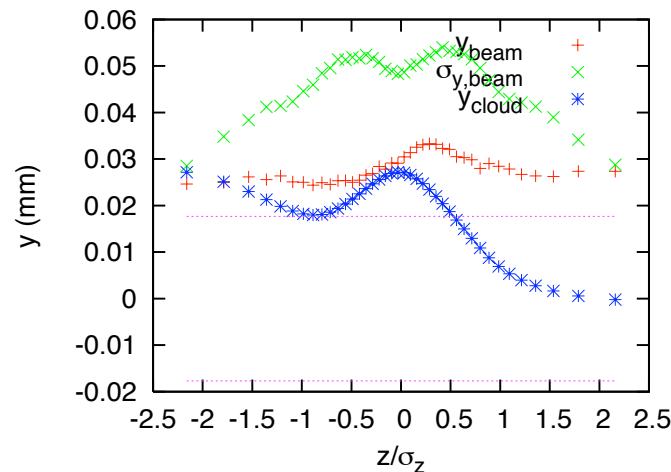


$$\rho_{\text{th}} = 1.0 \times 10^{12} \text{ cm}^{-3}$$

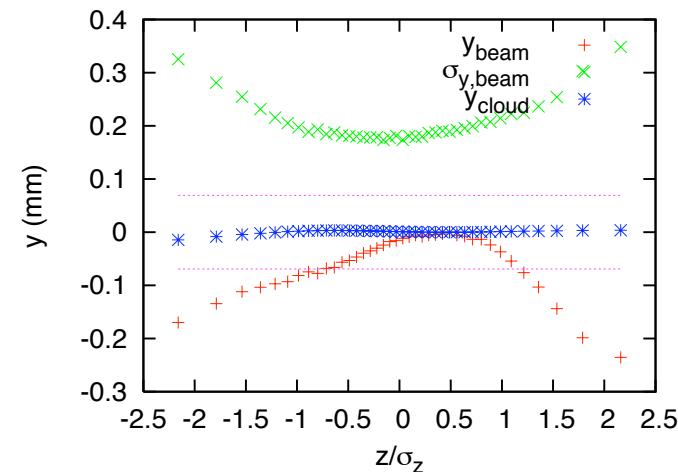
$$6 \times 10^{12} \text{ cm}^{-3}$$

# Coherent motion in the simulation

2 GeV



5 GeV



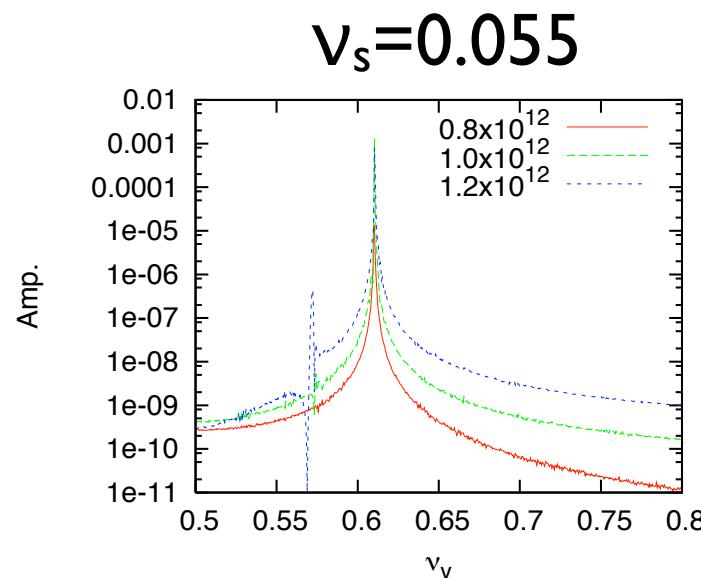
# Measurements

- Measure the beam size as a function of the beam current.
- Measure the beam size along the bunch train.
- Fourier spectra of the position monitor and beam size monitor.

# Fourier spectra in the simulation

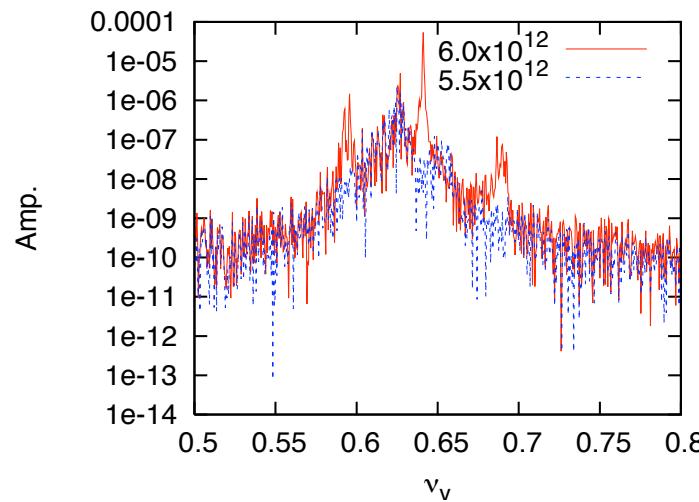
$$v_{y0}=0.6$$

2GeV



5GeV

0.0454

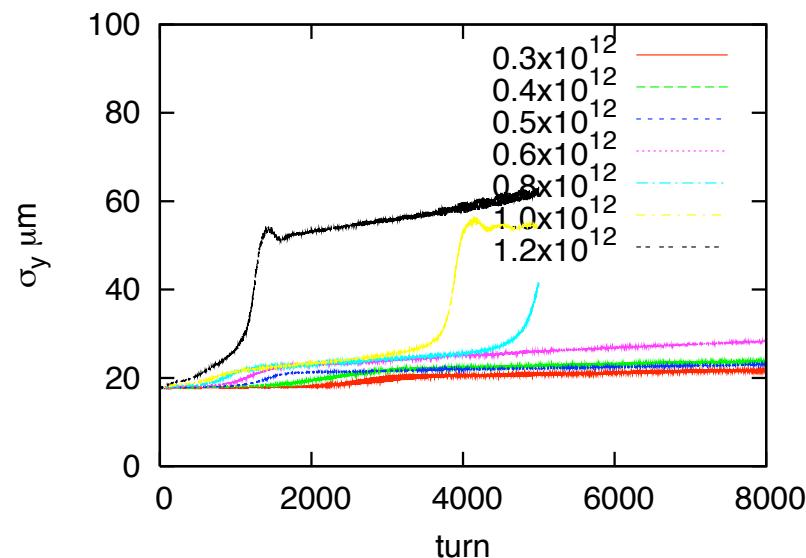


The spectra depend on choice of the cloud size, different between cloud size  $\sim \sigma_y$  or  $>> \sigma_y$ . Right solution should be given for cloud size  $>> \sigma_y$ .

# Effect of dispersion

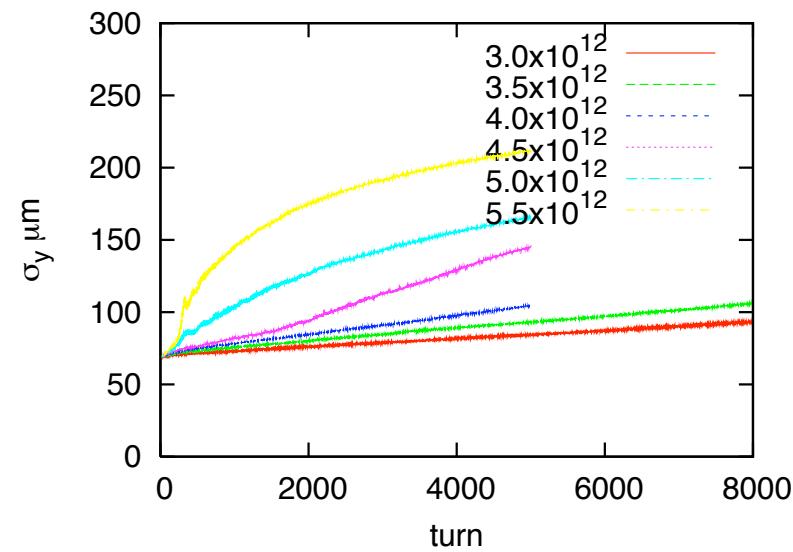
- $\eta_x = 1.5 \text{ m}$

2 GeV



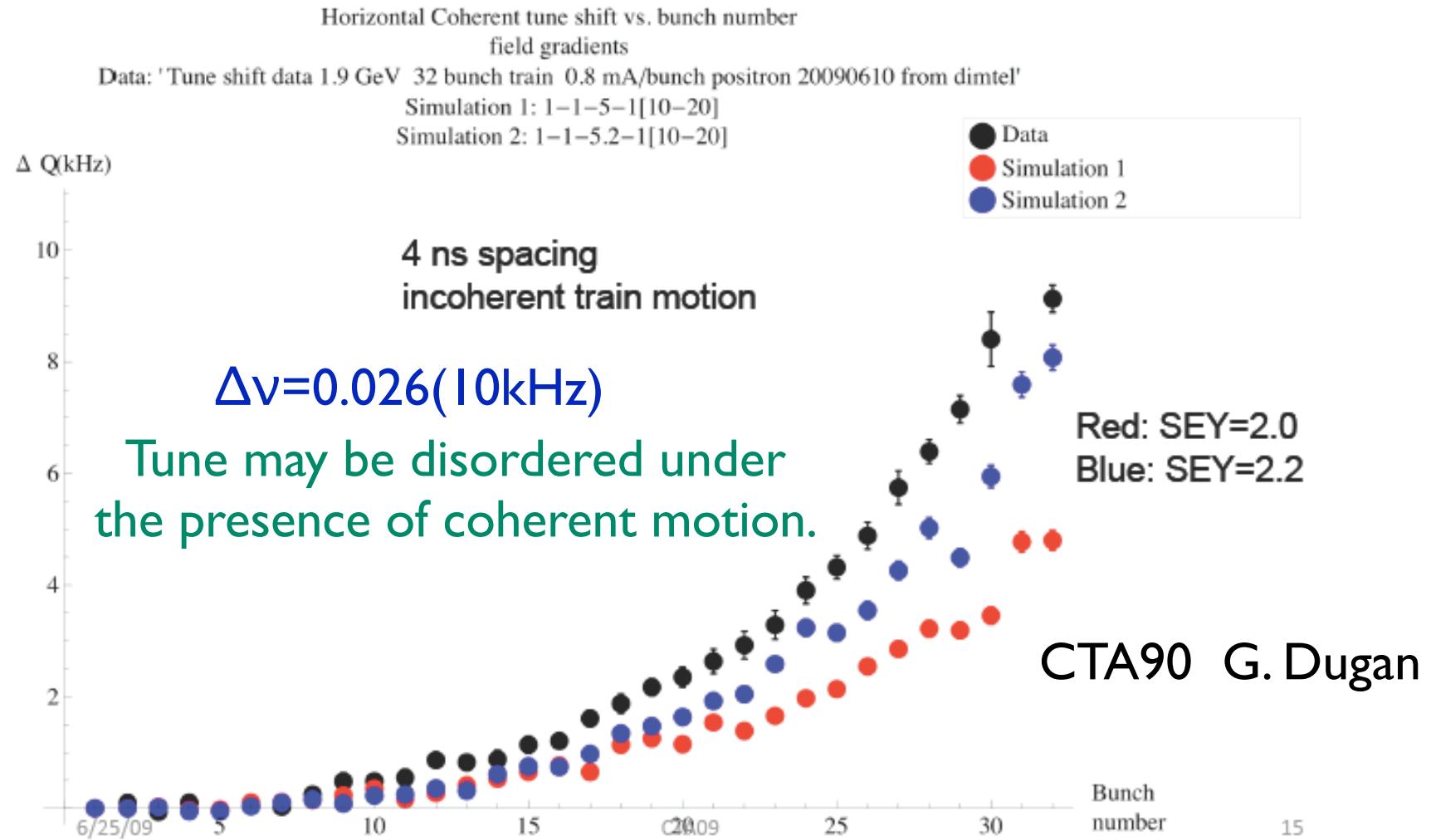
$$\rho_{th} = 0.8 \times 10^{12} \text{ cm}^{-3}$$

5 GeV



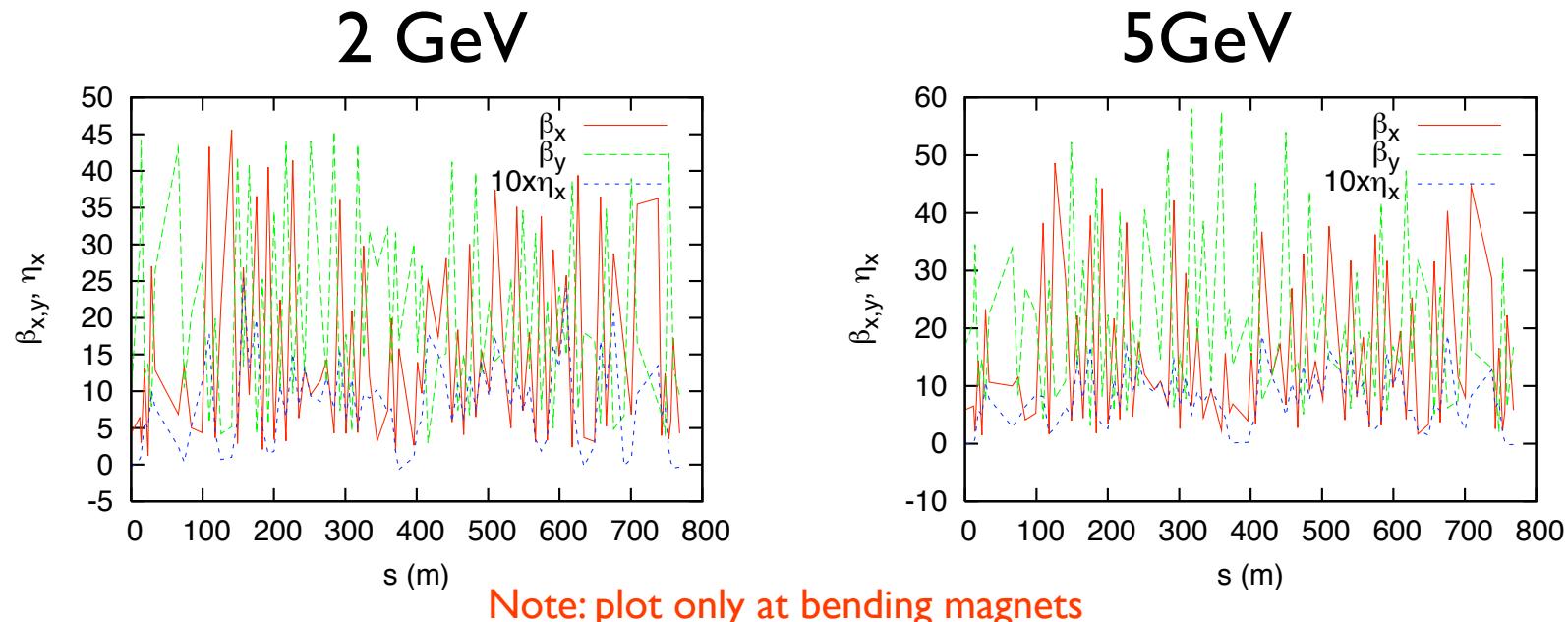
$$4.5 \times 10^{12} \text{ cm}^{-3}$$

- Not big effect



# Incoherent emittance growth

- Electron cloud is located in bending magnets.
- $\beta$ , phase and  $\eta$  are taken into account.



# Emittance growth due to nonlinear diffusion

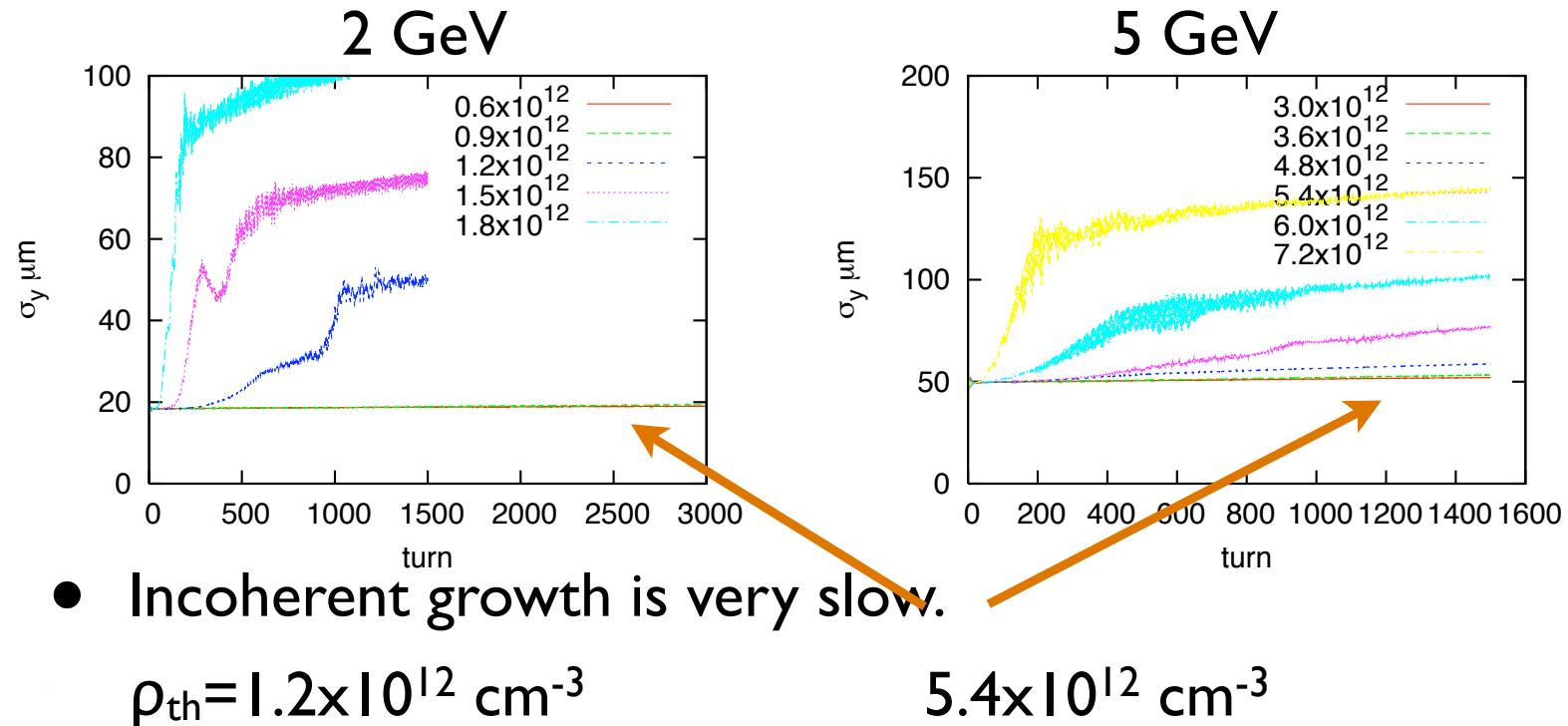
- Nonlinearity in one turn map

$$H_n \sim \oint a_n(s) x(s)^n \Big|_{x(s)=\sqrt{\beta/\beta_0} \cos \varphi(s) x_0 + \dots} ds = \oint a_n(s) \frac{\beta(s)^{n/2}}{\beta_0^{n/2}} \cos n\varphi(s) ds \times x_0^n + \dots$$

- Electron cloud density  $\sim a(s)$   $\beta$ , phase are integrated.
- Uniform  $\beta$  model cancels phase dependence, therefore no emittance growth,  $H(J)$ .
- $\beta$  and phase variations are essential for the emittance growth.

# Simulation of the Incoherent emittance growth

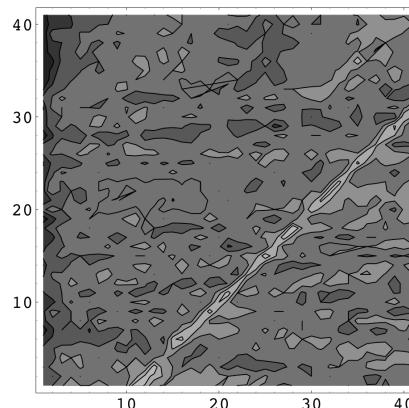
- Bending magnet section 475/768 m
- The electron density  $\rho$  is the averaged one,  $\rho_{\text{bend}} \times 475/768$



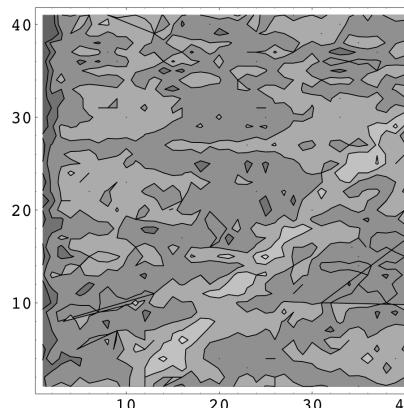
When electrons distribute also in drift space, the incoherent growth may be slower.

# Measurement of the incoherent emittance growth

- The same beam size measurement as is done for coherent strong head-tail.
  - ★ Beam size measurement as a function of the beam current.
  - ★ Measure the beam size along the bunch train.
  - ★ Fourier spectra (check no coherent signal).
- Beam size measurement in tune space,  $\nu_x - \nu_y$ .



single bunch

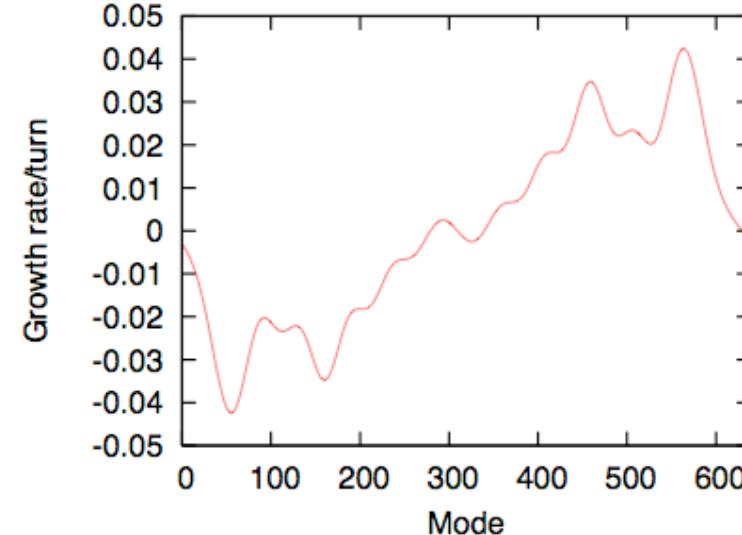
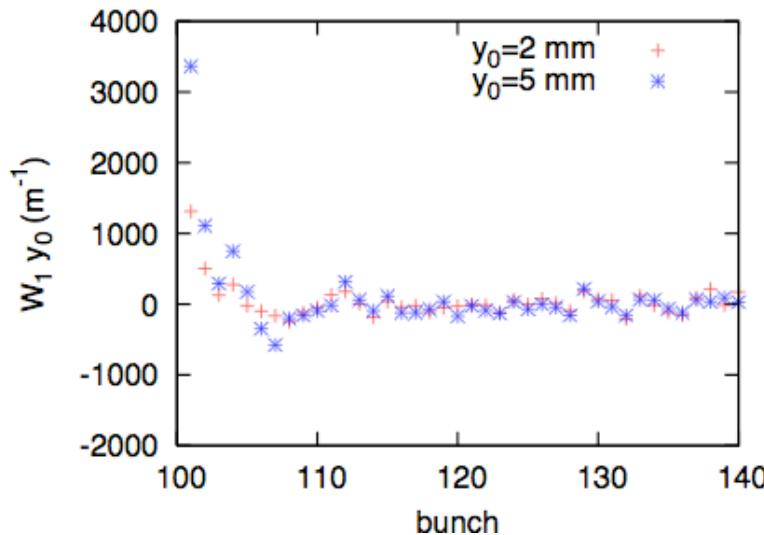


2.7mA x 10 bunches, 14ns

No signal in the  
measurement on June  
27-29, 2008.  
5.3 GeV chess mode

## Measurement of electron cloud induced Coupled bunch instability

- $N_p = 1 \times 10^{10}$ , 4 ns spacing uniformly for example. Number of bunch is 640. It is possible to do 14 ns, 90 bunches.
- The analysis is easy for uniform filling, but is possible for partial filling.
- Cut off the feed back power and measure the positions of all bunches turn by turn.
- Growth time  $\sim 25$  turn, 64  $\mu$ sec for this condition.



This spectrum is given for free electron motion. If bending magnet is dominant, different spectrum is obtained.