



# *Beam-breakup Calculations for the 1- vs 2-Turn Document*

*-- Draft of Complete Text and Figures ---*

*-- Status update since ERL@CESR talk of 23 July 2009 --*

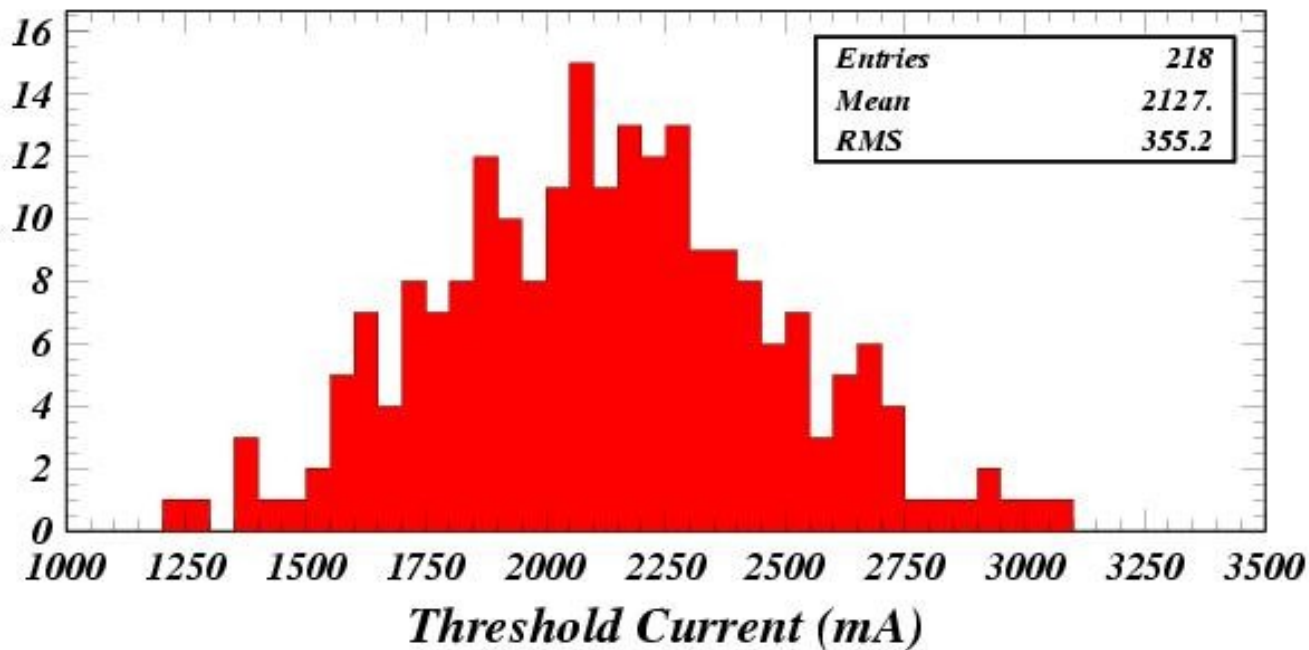
*Jim Crittenden, Georg Hoffstaetter, Matthias Liepe and Chris Mayes*

*ERL @ CESR Meeting  
22 October 2009*





# *Bmad Validation with Polarized HOMs in the 2007 PRSTAB Coupled Optics*



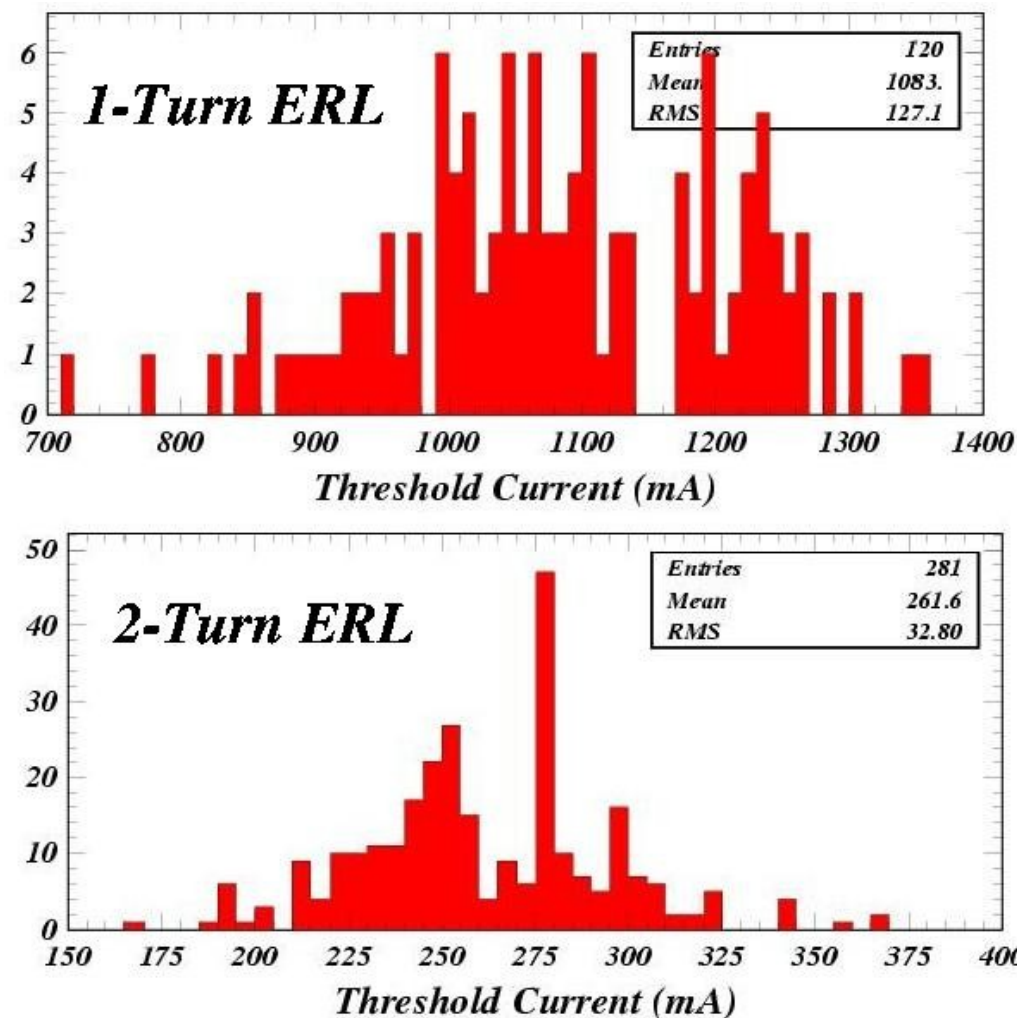
*Modelled BBU instability thresholds for the case of a single higher-order mode excited in a single cavity of the fully coupled single-turn ERL optics in Ref. ERL-06-01 with polarized HOMs with 60 MHz frequency splitting and 10 MHz HOM frequency spread.*

*The resulting average and RMS values of 2127 mA and 355 mA compare well with the values 2076 mA and 341 mA obtained in Ref. ERL-06-01.*



# *Bmad BBU 1 vs 2 Turn Comparison*

## *Updated HOMS (c.f. Matthias), Unpolarized*



*Modelled BBU instability thresholds for the case of the five updated HOMs excited in each cavity of the full 1-turn Cornell ERL optics (upper plot) compared to the threshold currents calculated for the same case in the 2-turn ERL (c.f. Chris, lower plot).*

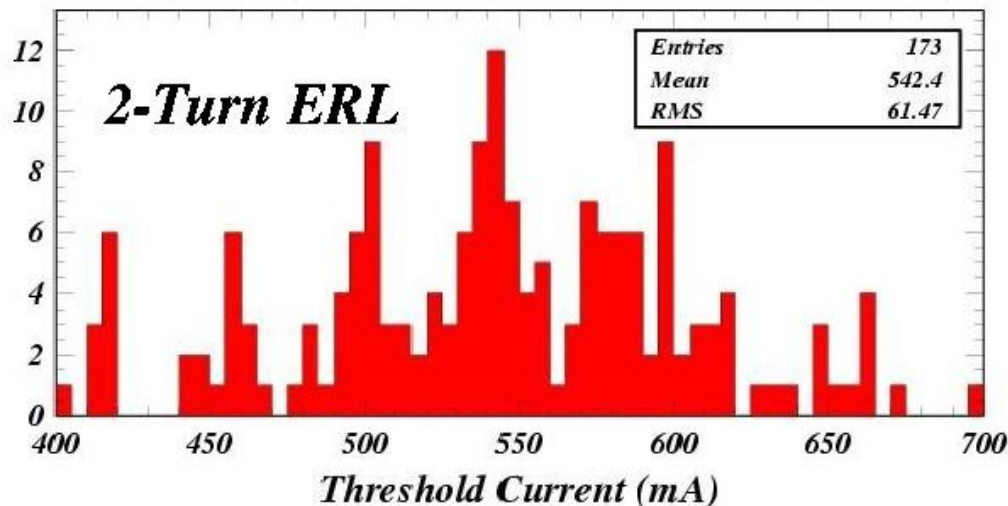
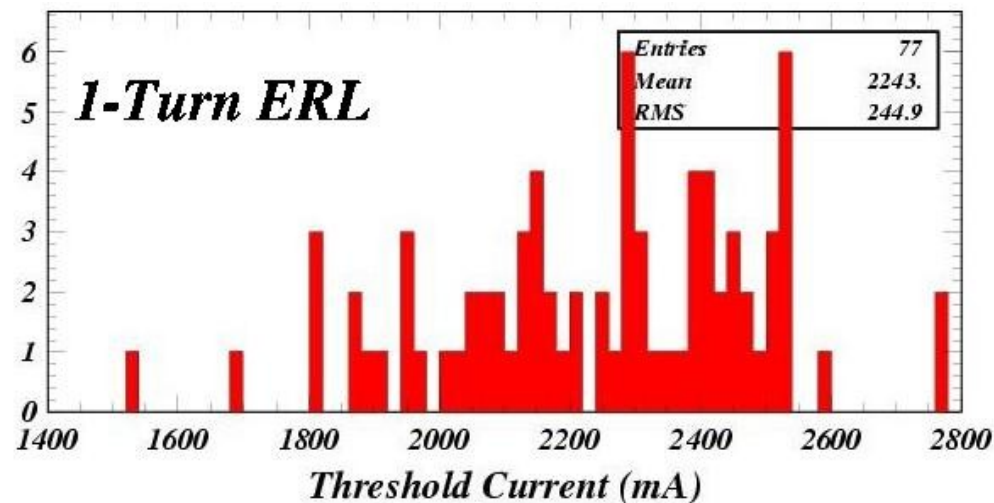
*The average 1-turn instability threshold is 1082 mA with an RMS spread of 127 mA. The corresponding values for the 2-turn optics are about a factor of four lower, in rough agreement with the estimate of  $N(2N-1) = 6$  given in PRSTAB 10 (2007).*

*The worst case found for the 2-turn optics is 160 mA, marginally above the 100 mA design current of the Cornell X-ray ERL.*



# *Bmad BBU 1 vs 2 Turn Comparison*

## *Updated HOMS, Polarized with Coupled Optics*



*Modelled BBU instability thresholds for the case of polarized HOMs with 50 MHz HOM frequency splitting excited in each cavity of the full 1-turn Cornell ERL optics (upper plot) compared to the threshold currents calculated for the same case in the 2-turn ERL (lower plot).*

*The improvement is about a factor of two for each of the optics, showing that this means of BBU instability mitigation is as effective in the 2-turn optics as in the 1-turn optics.*