



# *Heuristic Study of the Effect of Chromatic Nonlinearities on BBU Instability Thresholds*

*Initial investigation with the toy lattice used in Hoffstaetter and Bazarov,  
PRST-AB 7, 054401 (2004)*

$$X_i^{(N+1)} = R_{ij} X_j^{(N)} + M_{ijk} X_j^{(N)} X_k^{(N)} \quad i, j, k=1-6$$

*Introduce nonzero  $M_{116}$   $M_{226}$   $M_{126}$  to see how particle energy  
offsets affect the instability threshold calculation*

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*Cornell Laboratory for Accelerator-Based Sciences and Education*

*ERL@CESR Meeting*

*29 March 2012*





# Dependence on Energy and Magnitudes of Nonlinear Transfer Elements

$$M_{116} = M_{226} = M_{126}$$

-10k

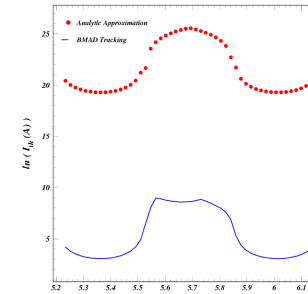
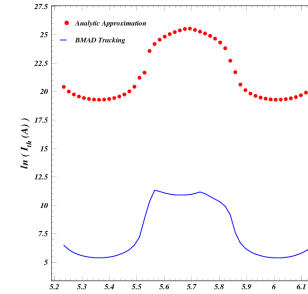
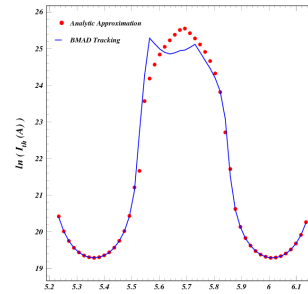
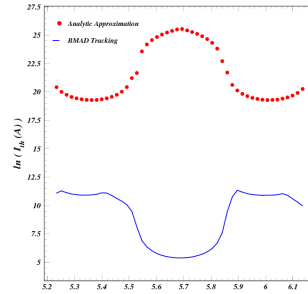
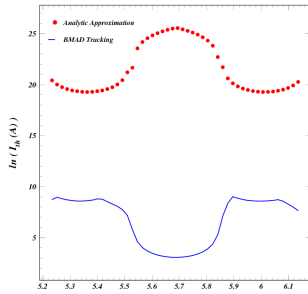
-1k

0

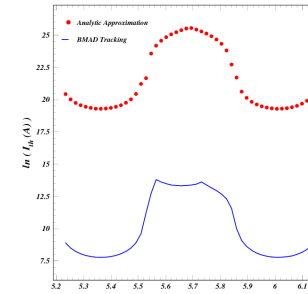
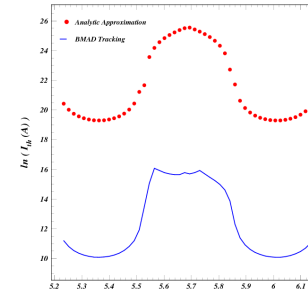
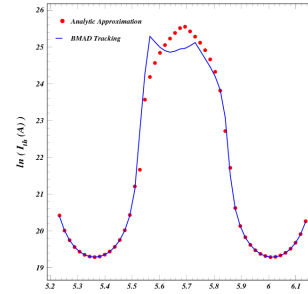
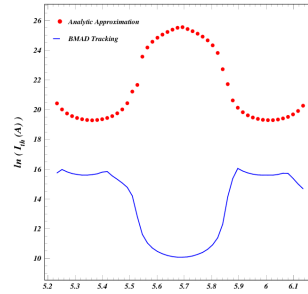
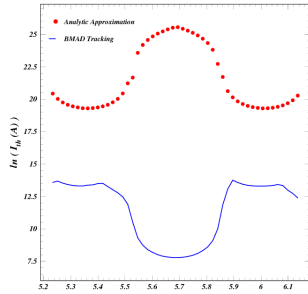
1k

10k

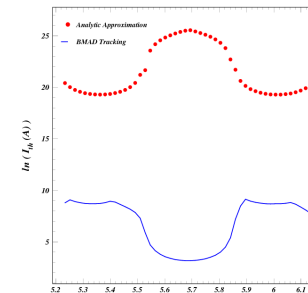
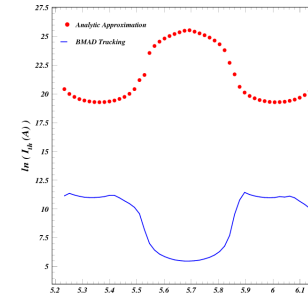
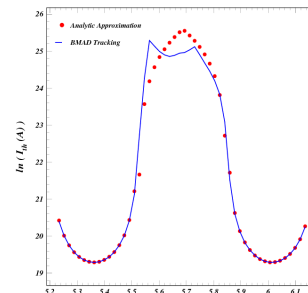
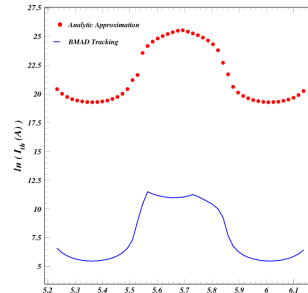
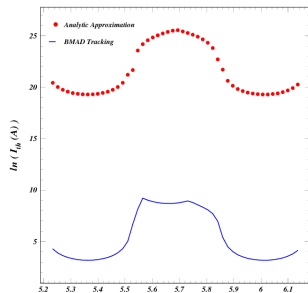
$\Delta E/E = -1e-3$



$\Delta E/E = 0$



$\Delta E/E = 1e-3$



Ratio of Return Time to Bunch Spacing