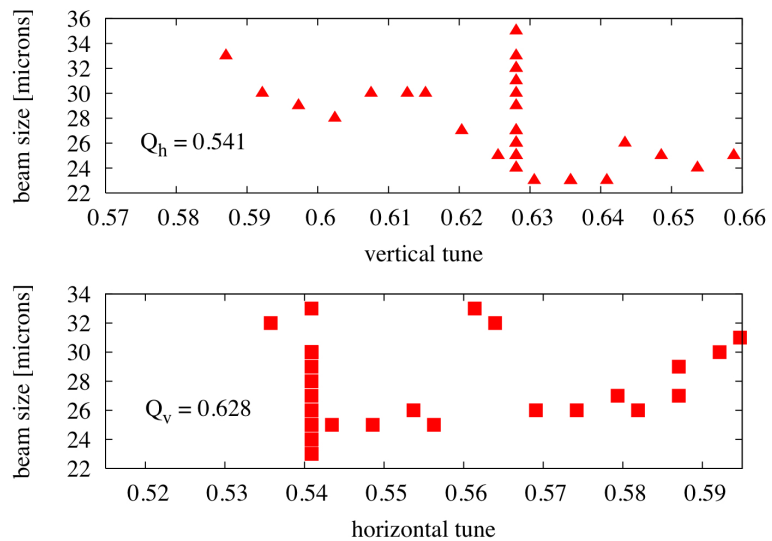
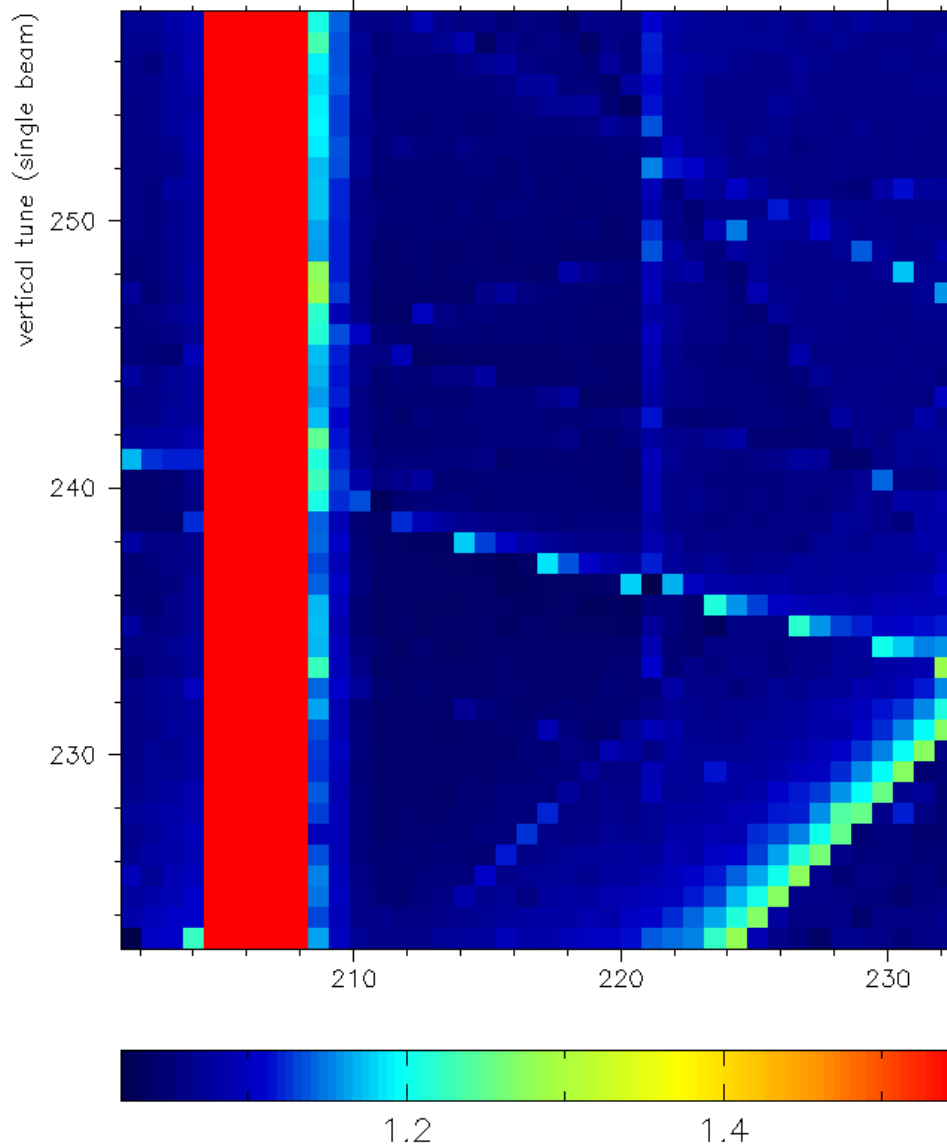


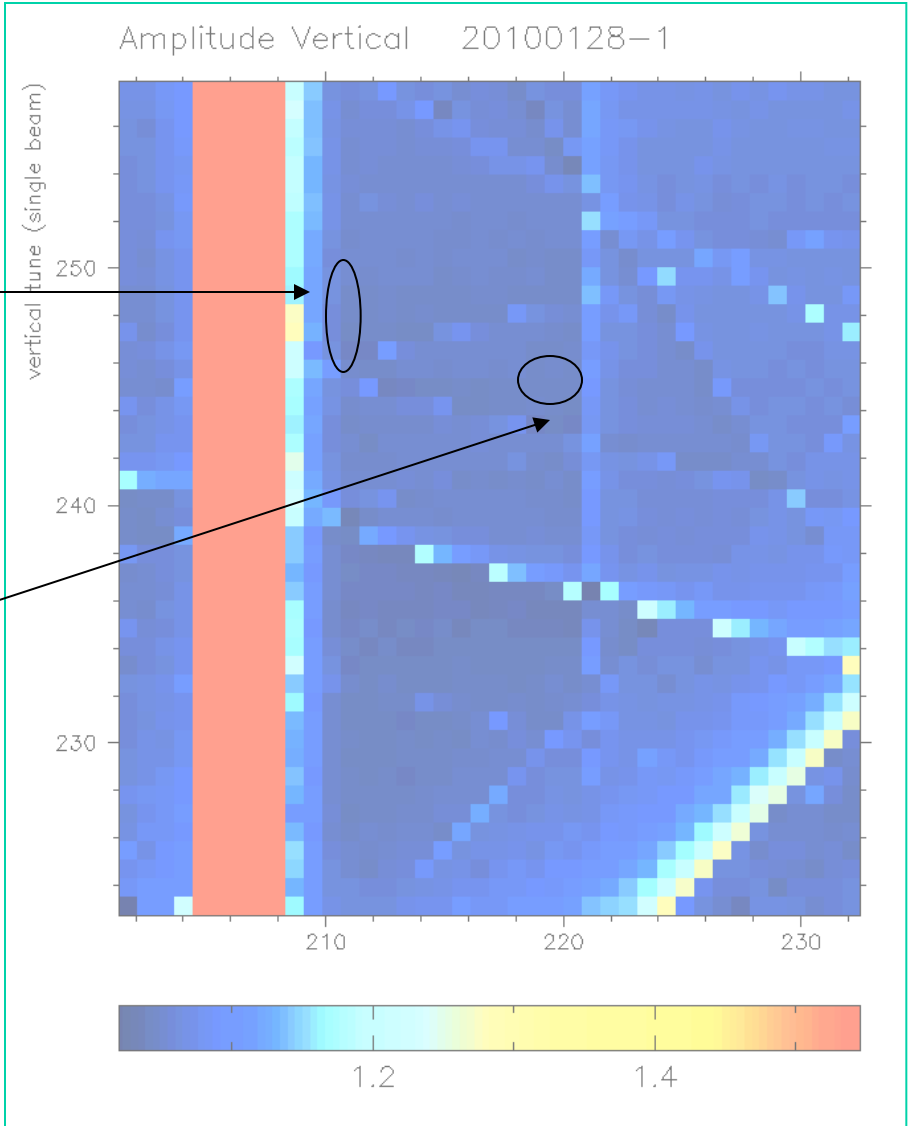
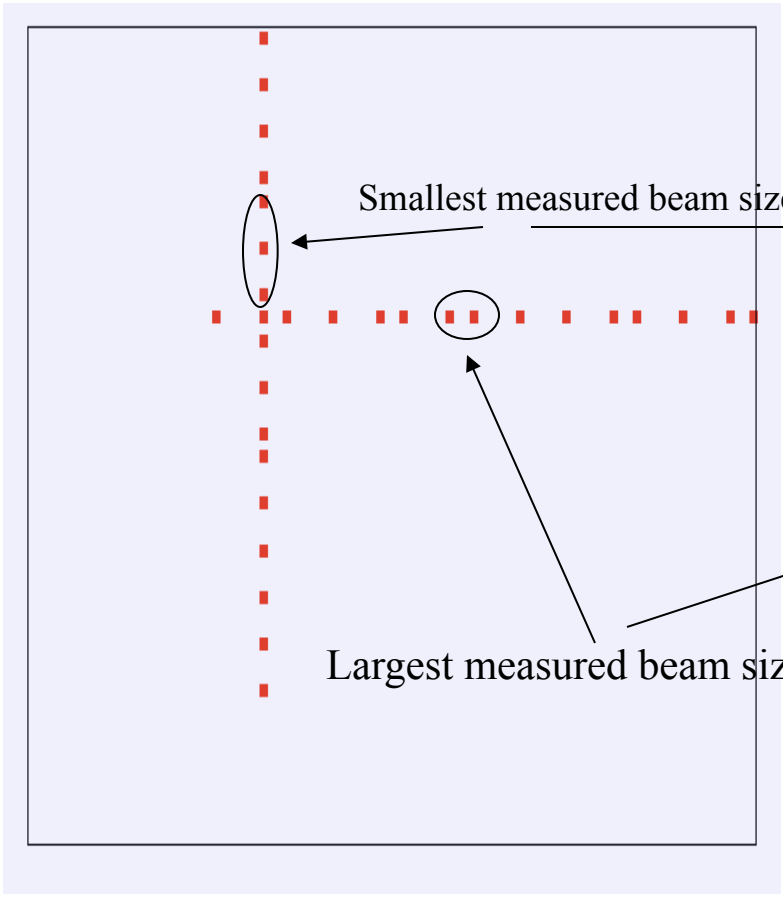
Tune scan of vertical beam size



X-ray beam size monitor
Gives turn by turn beam size

Amplitude Vertical 20100128-1





$$\sigma_{min} = 23\mu m$$

$$\epsilon_v = 32\mu m$$

Cta_2085mev_20090516

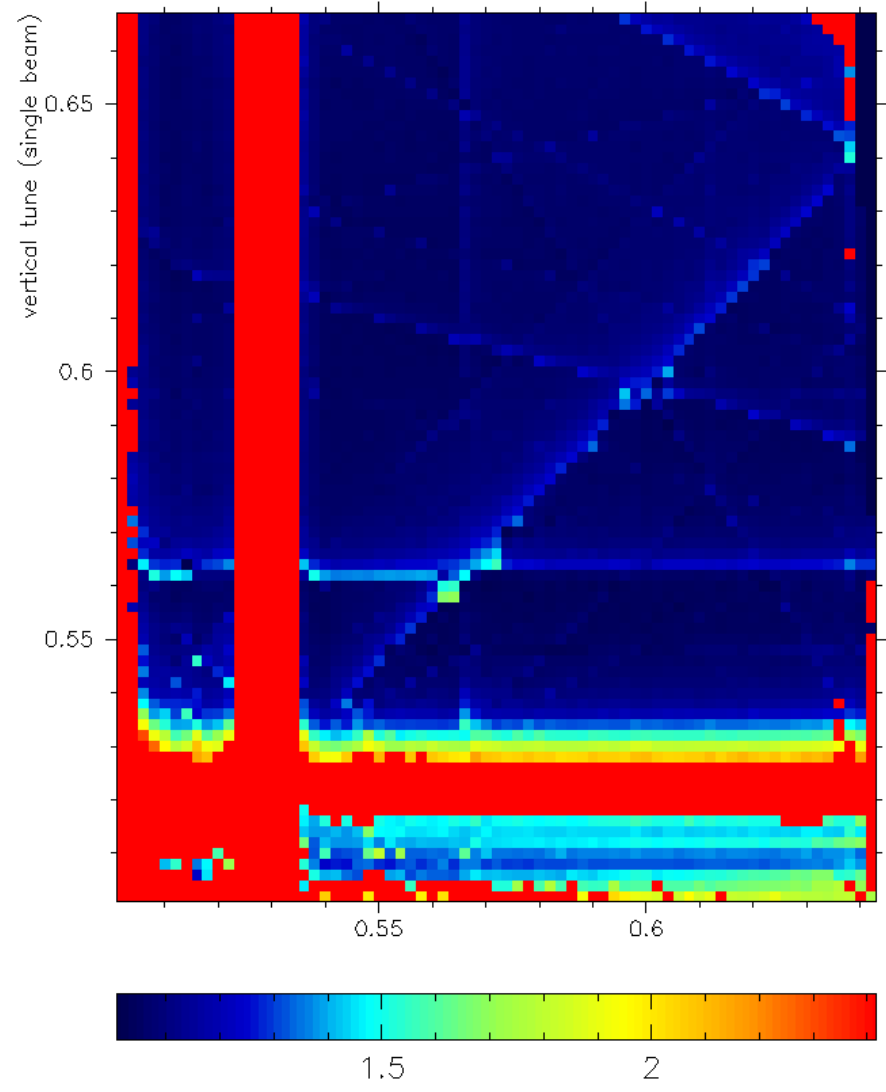
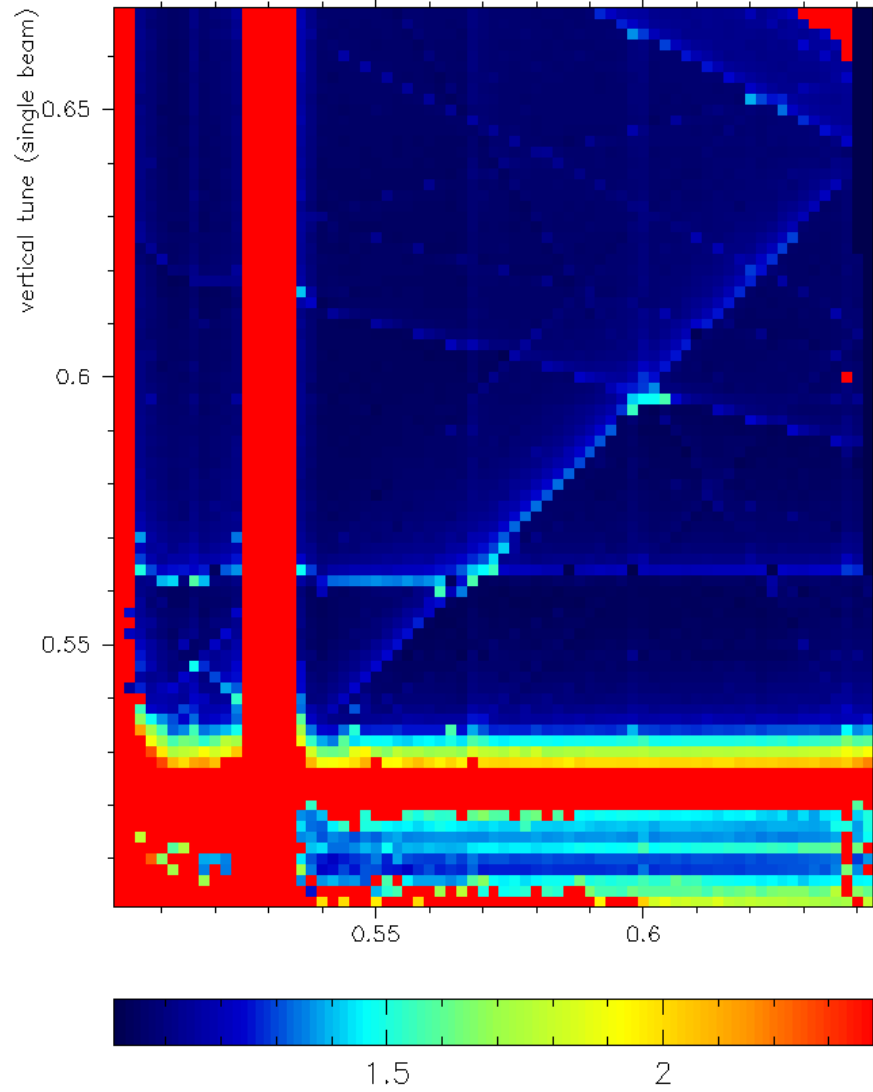
$Q_z=0.066=25.7\text{kHz}$

nominal

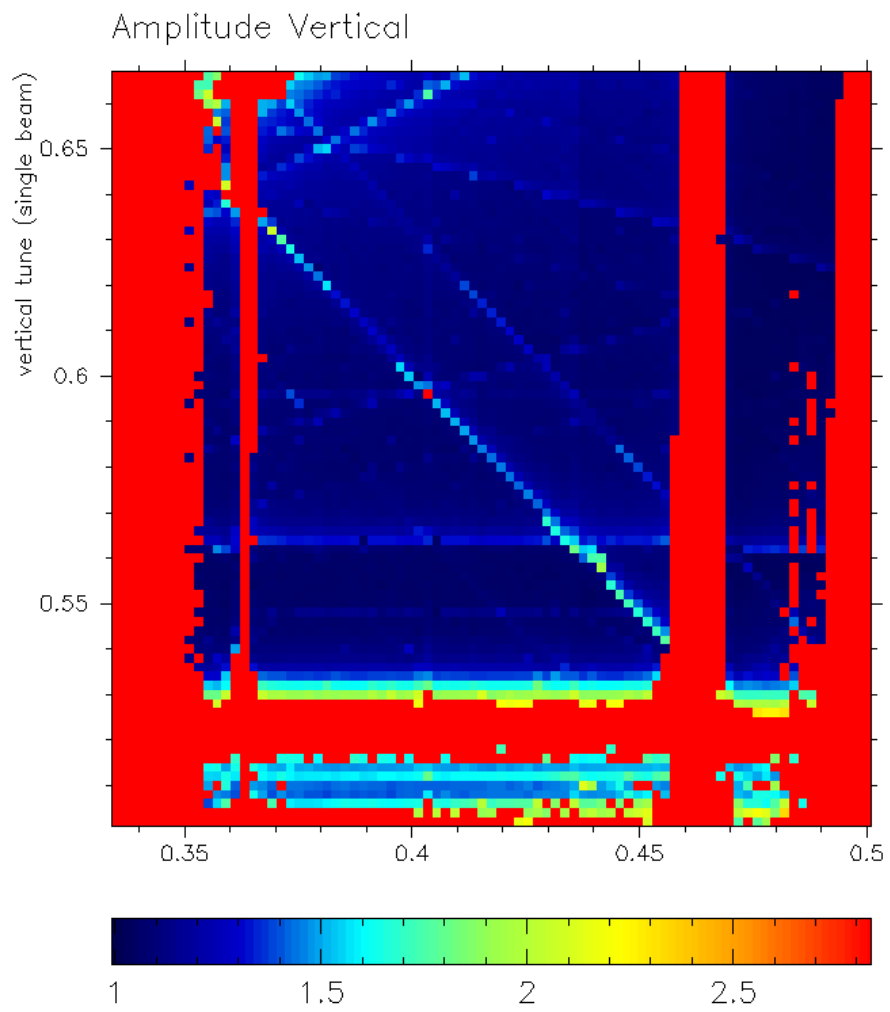
Zero dispersion in RF

Amplitude Vertical

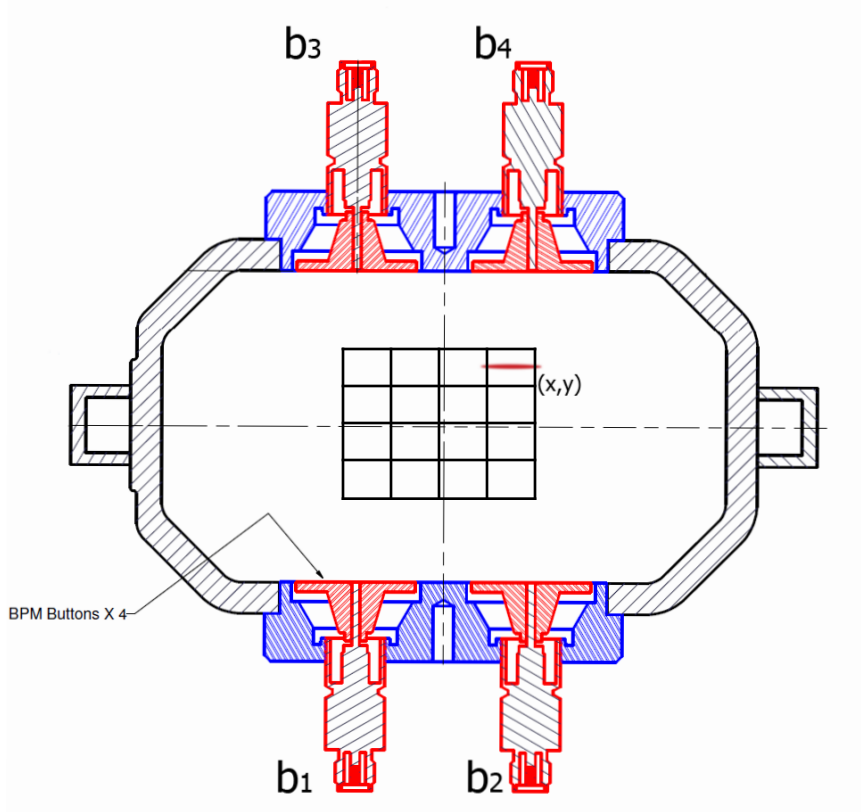
Amplitude Vertical



$$Q_h < 0.5$$



Gain mapping



Signal at each button depends on bunch current (k) and position (x,y)

$$B_1 = kf(x, y)$$

$$B_1 \approx k \left(f(0, 0) + \frac{\partial f}{\partial x}x + \frac{\partial f}{\partial y}y + \frac{1}{2} \frac{\partial^2 f}{\partial x^2}x^2 + \frac{1}{2} \frac{\partial^2 f}{\partial y^2}y^2 + \frac{\partial^2 f}{\partial x \partial y}xy + \dots \right)$$

$$B_1 \approx k(c_0 + c_1x + c_2y + c_3x^2 + c_4y^2 + c_5xy)$$

Signals on the four buttons are related by symmetry

$$B_2 = kf(-x, y)$$

$$B_3 = kf(x, -y)$$

$$B_4 = kf(-x, -y)$$

Combining sums and differences we find the following relationship, good to second order

$$B_1 - B_2 - B_3 + B_4 = \frac{1}{k} \left(\frac{c_5}{c_1 c_2} \right) (B_1 - B_2 + B_3 - B_4)(B_1 + B_2 - B_3 - B_4)$$

$$B(+ - - +) = \frac{c}{k} B(+ - + -) B(+ + - -)$$

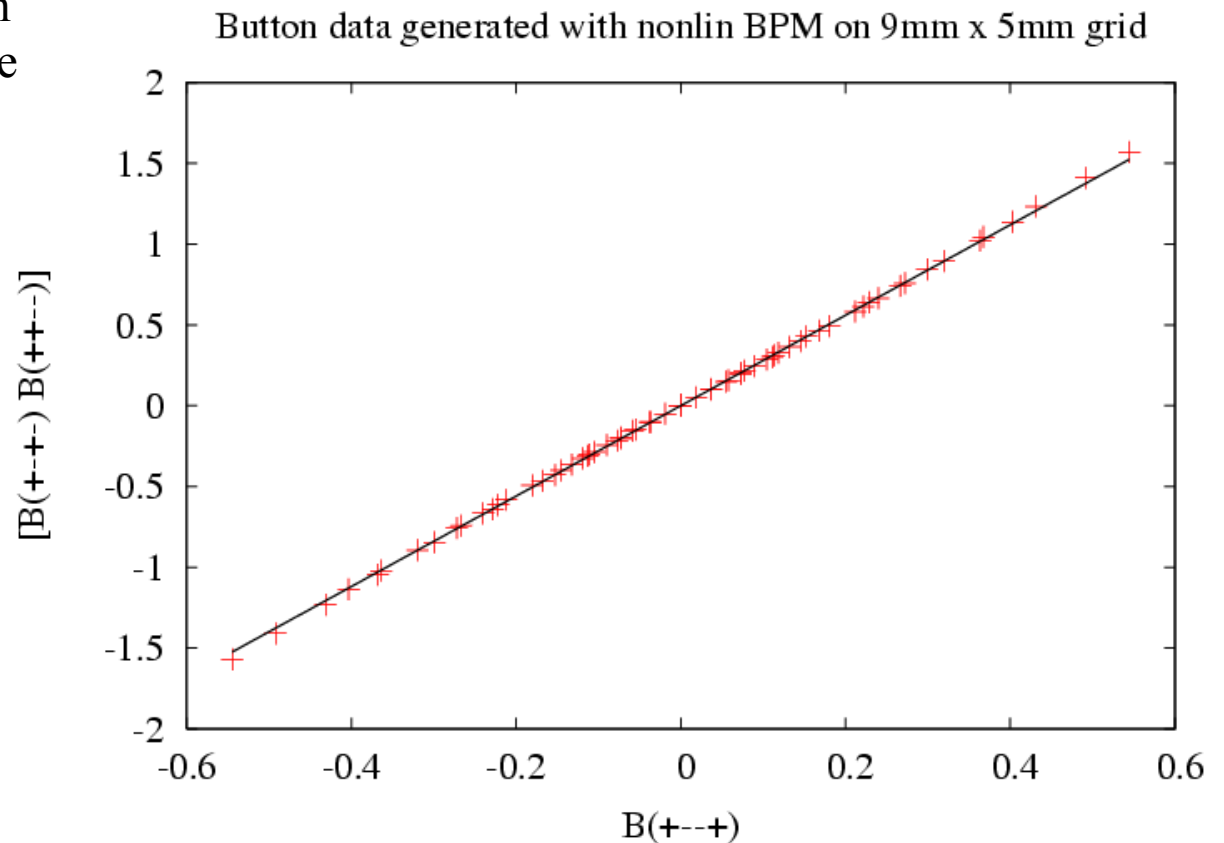
Simulation

$$B(+ - - +) = \frac{c}{k} B(+ - + -) B(+ + - -)$$

Using a map that reproduces the “exact” dependence of the button signals on the bunch positions we generate B_1, B_2, B_3, B_4 for each of 45 points on a 9mm x 5mm grid

In first order $c=0$, and therefore $B(+ - - +) = 0$. Evidently the first order approximation is not very good enough this range.

The small deviations from the straight line at large amplitudes is a measure of the higher than second order contributions.

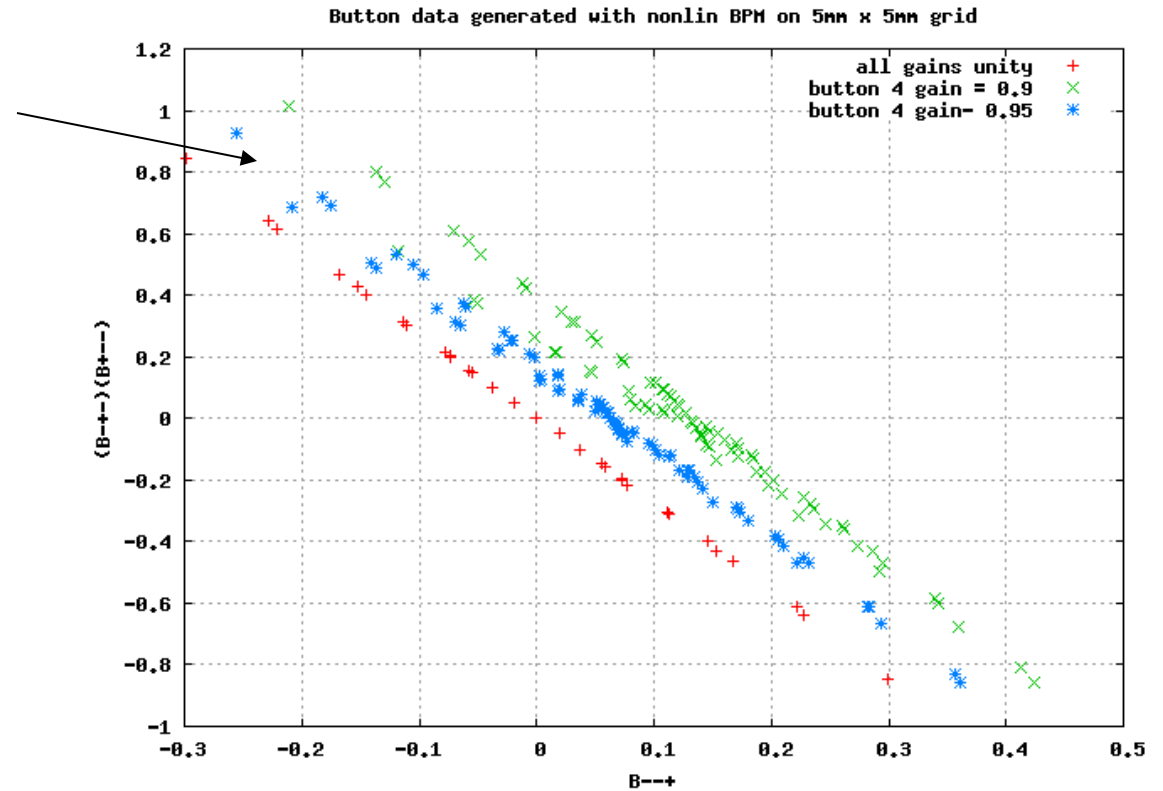


Simulation with gain errors

$$B(+ - - +) = \frac{c}{k} B(+ - + -) B(+ + - -)$$

Introduce gain errors

Zero offset, nonlinearity, and multi-valued relationship in is a measure of gain errors.



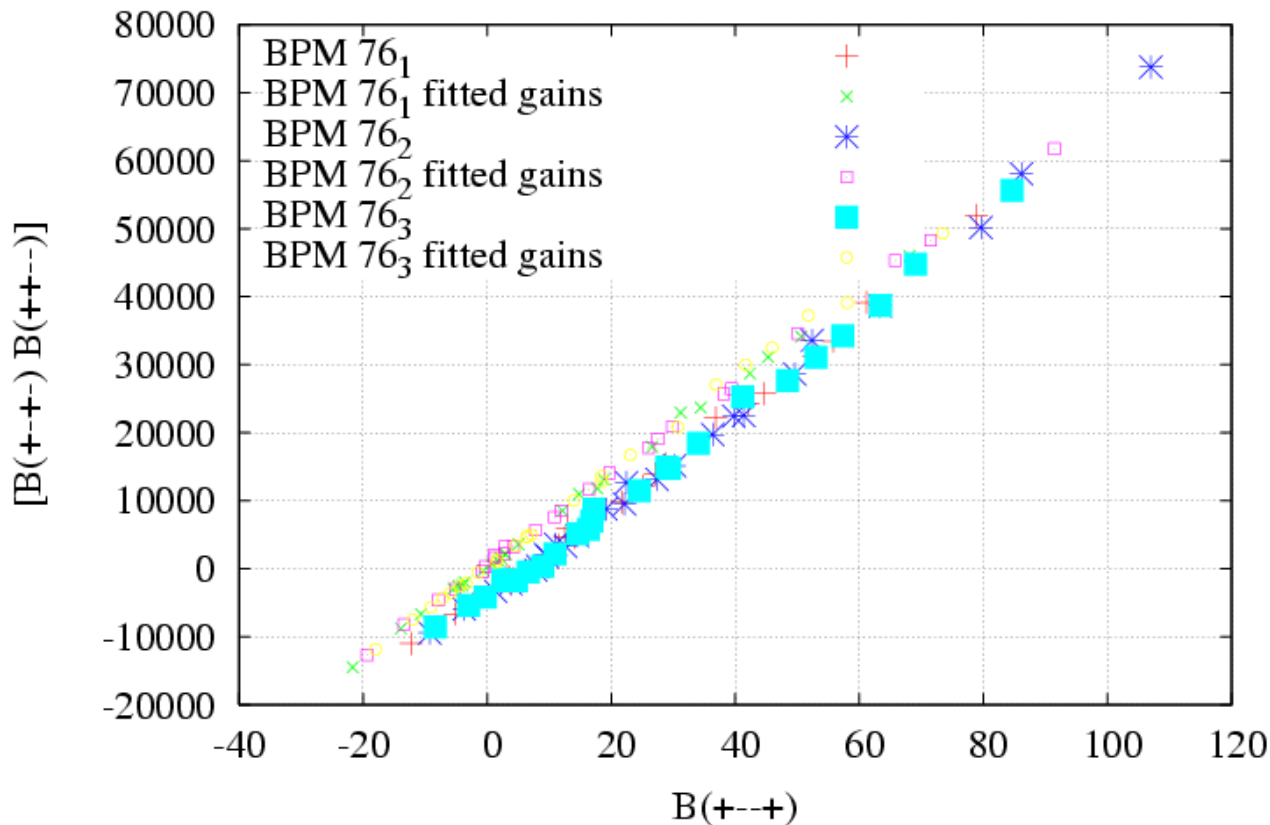
Orbit data collected on a grid

To fit for gains

Fix $g_1=1$, and minimize with respect to g_2, g_3, g_4, c

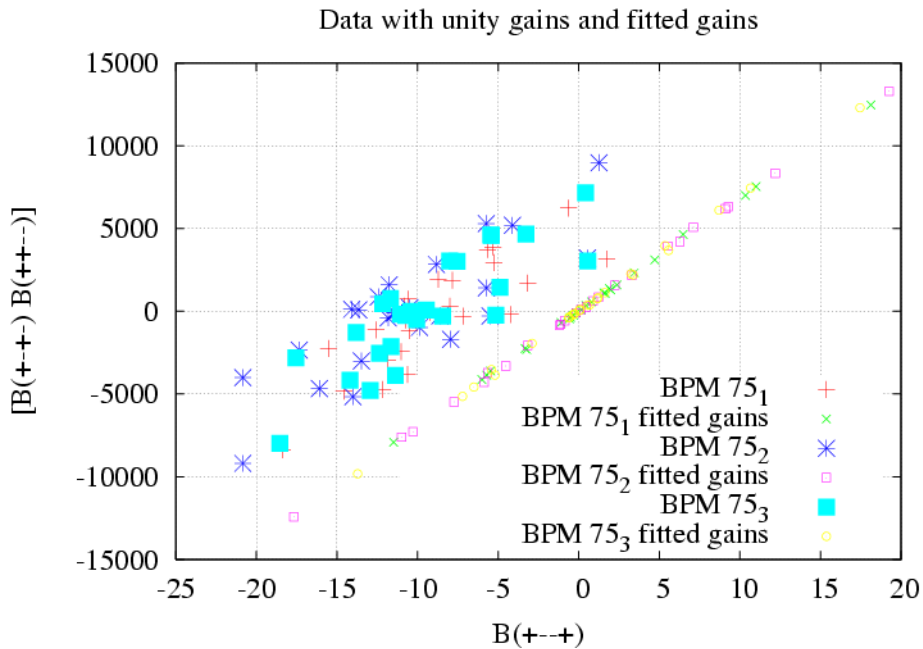
$$\sum_i [(g_1 B_1^i - g_2 B_2^i - g_3 B_3^i + g_4 B_4^i) - \frac{c}{I} (g_1 B_1^i - g_2 B_2^i + g_3 B_3^i - g_4 B_4^i)(g_1 B_1^i + g_2 B_2^i - g_3 B_3^i - g_4 B_4^i)]^2$$

Data with unity gains and fitted gains

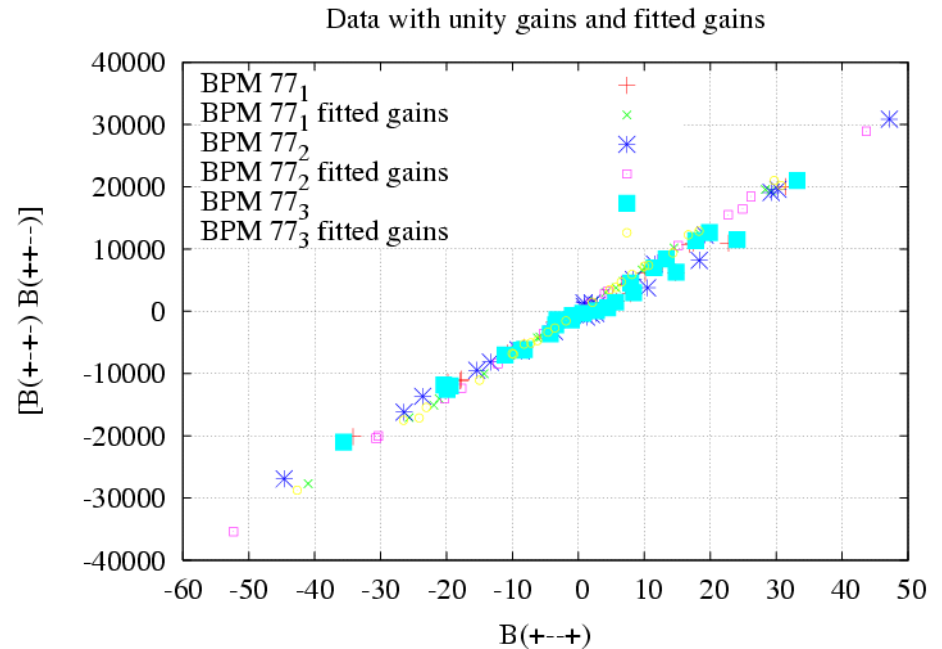


Fitted gains =
1, 0.95, 0.96, 0.97

Orbit data collected on a grid



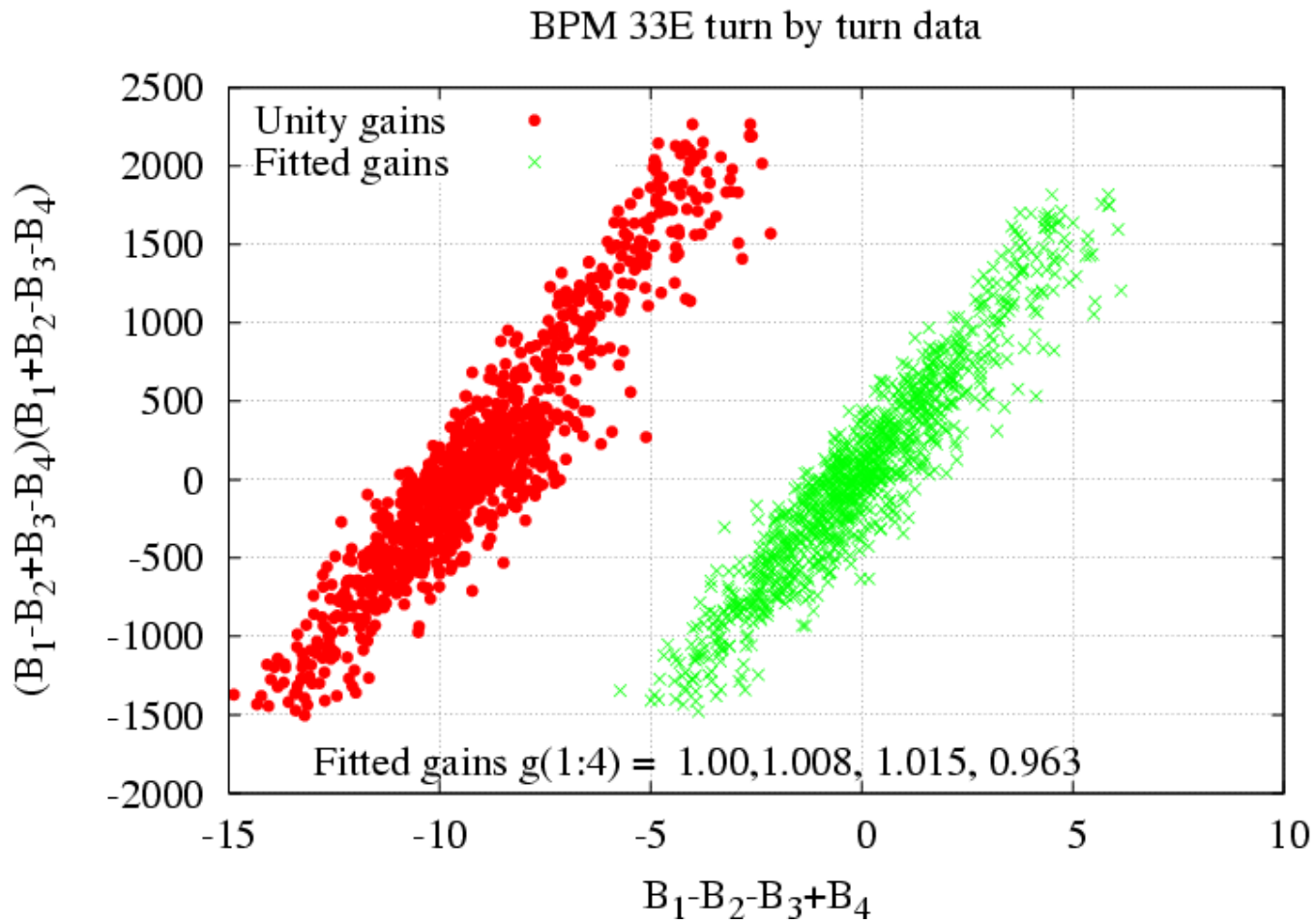
BPM 75 -
fitted gain = 1,1.02,0.96,0.91

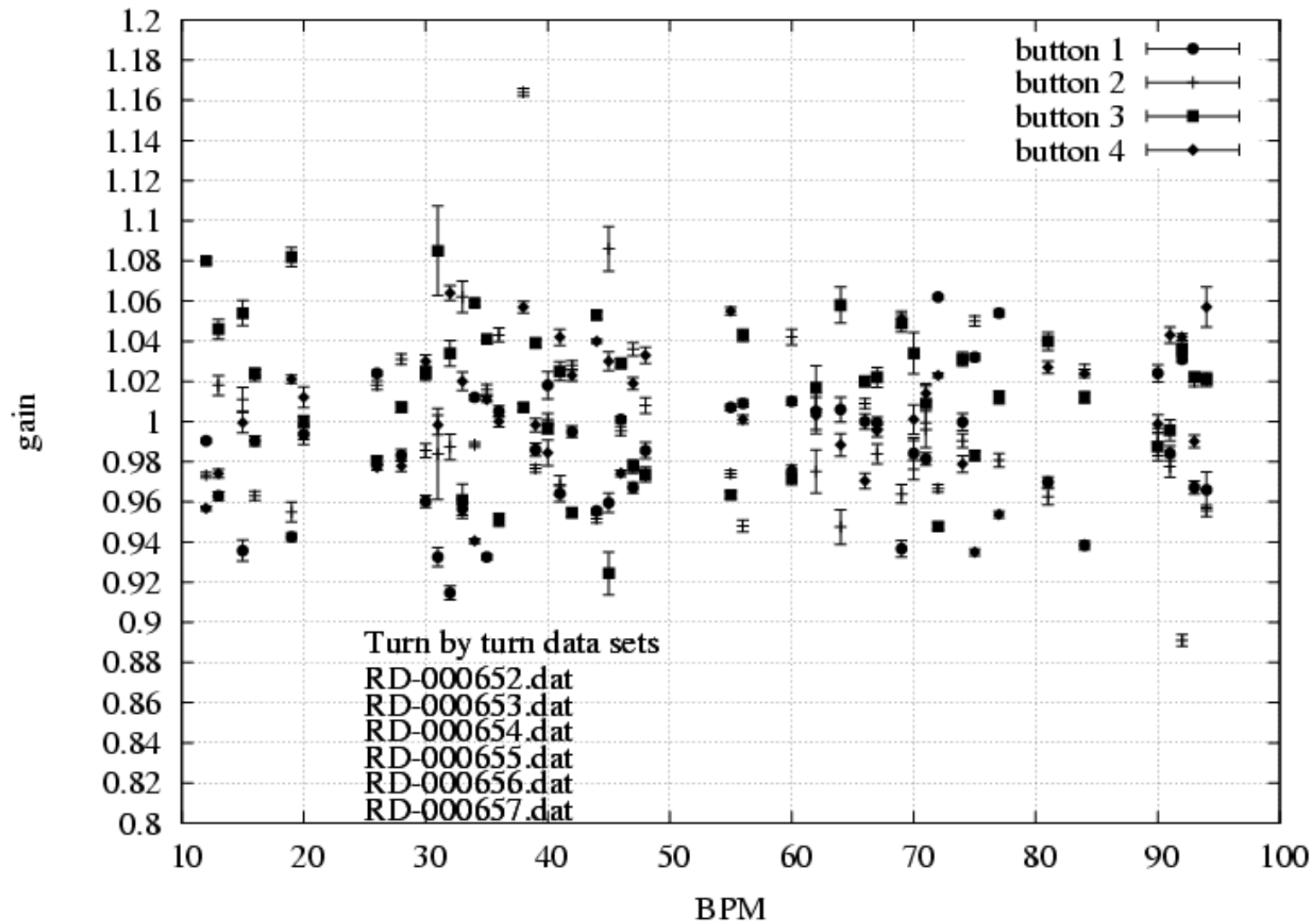


BPM 77 -
fitted gain = 1,0.92,0.96,0.9

Fit typically reduces χ^2 by two orders of magnitude

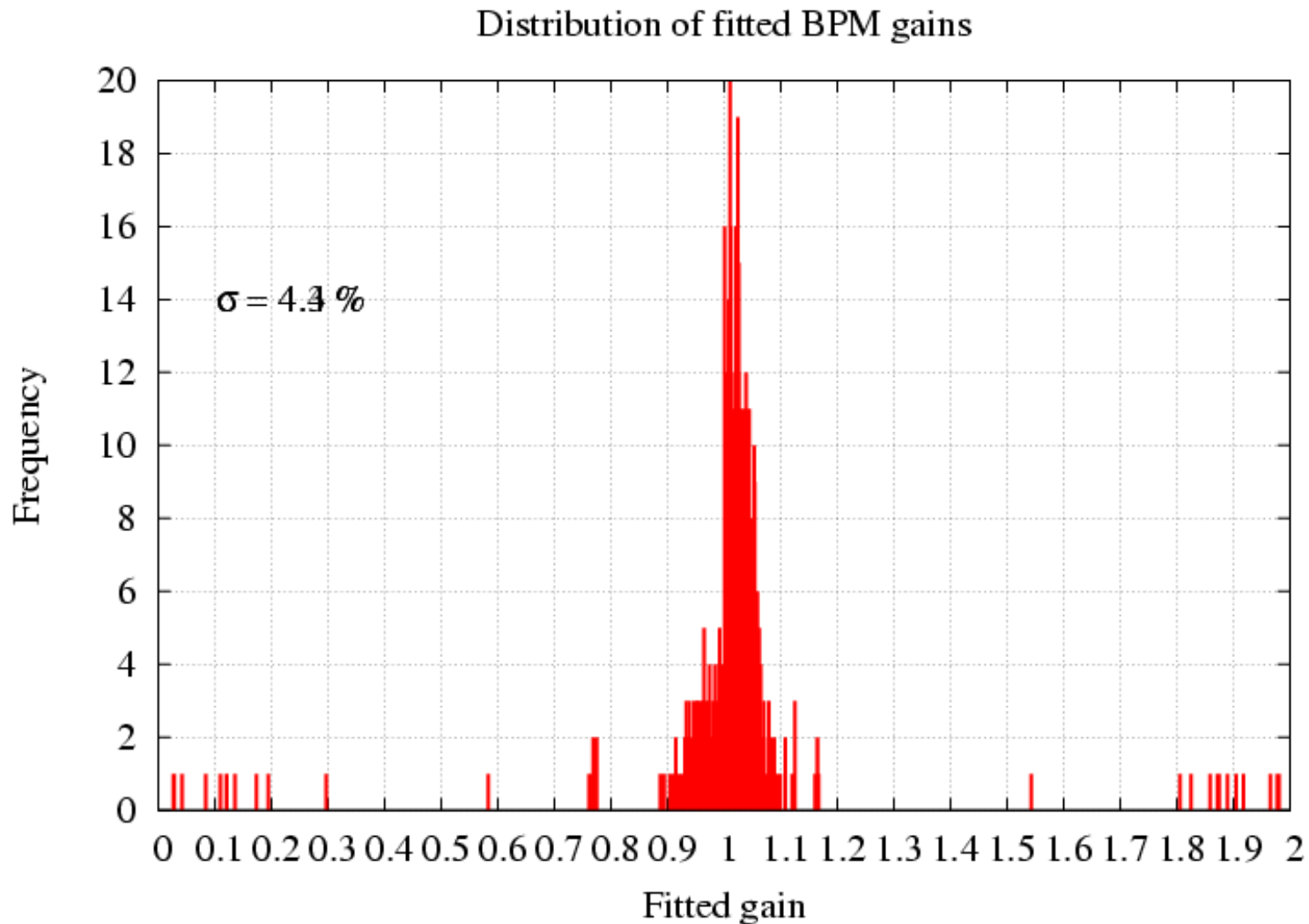
Turn by turn data, December 10, 2009





Average gains computed for 6 turn by turn data sets

Error bar is the standard deviation of the 6



Fitted gains from 6 turn by turn data sets, RD-000652, 653, 654, 655, 656, 657
 Normalized so that average at each BPM of 4 gains is unity
 Standard deviation, eliminating all points with gain errors greater than 50% is $\sigma = 4.3\%$

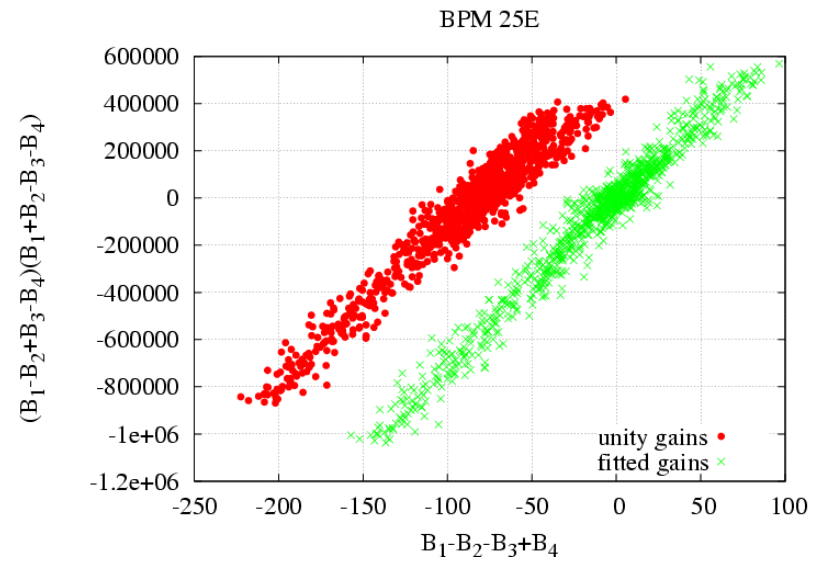
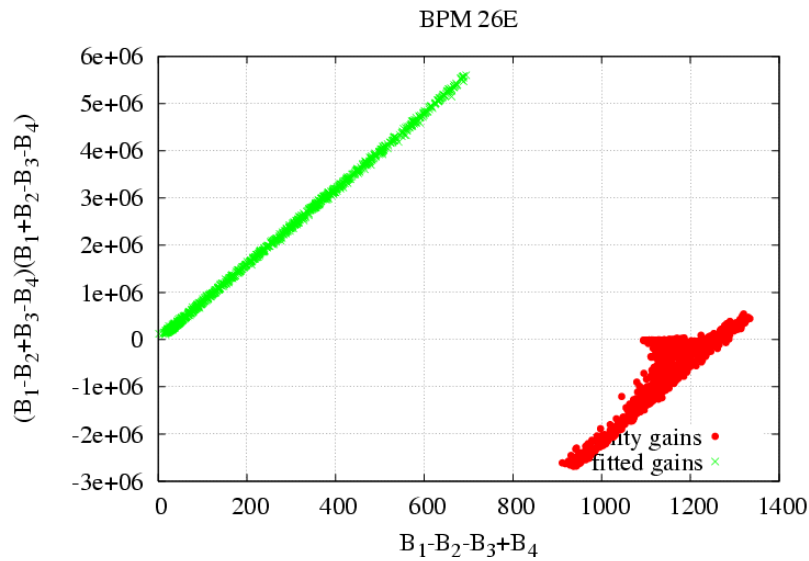
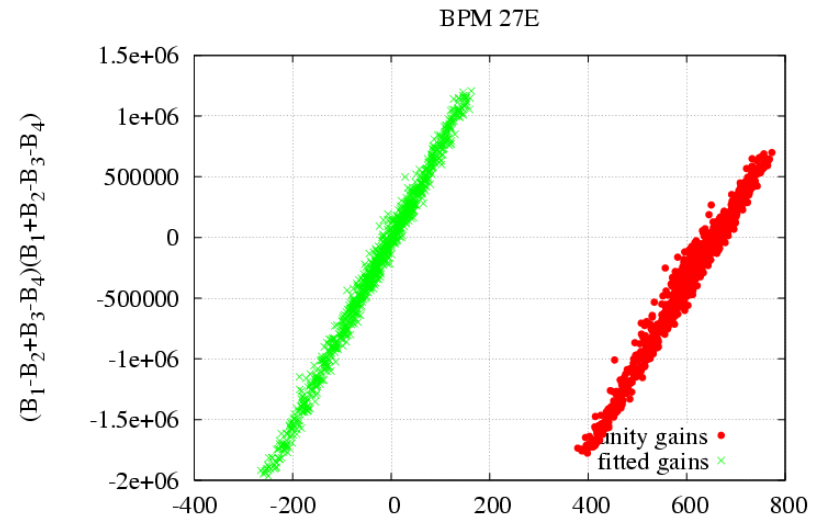
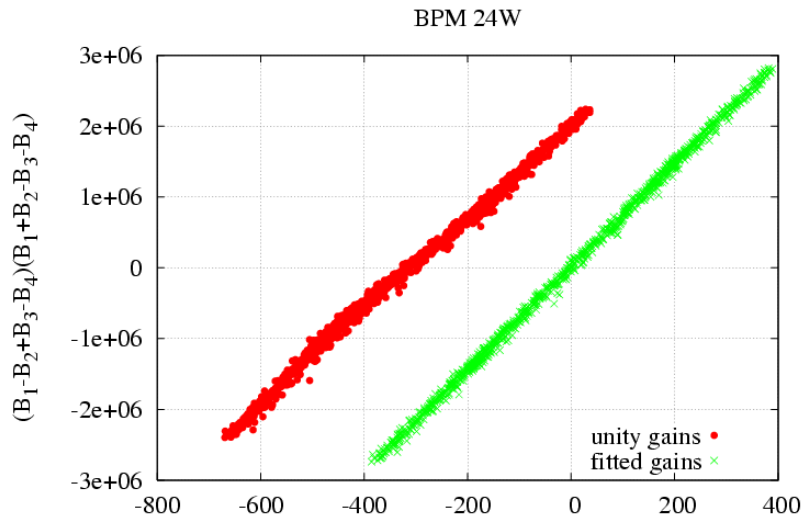
Data from December 19, 2009

Turn by turn data RD-000908.dat, RD-000909.dat

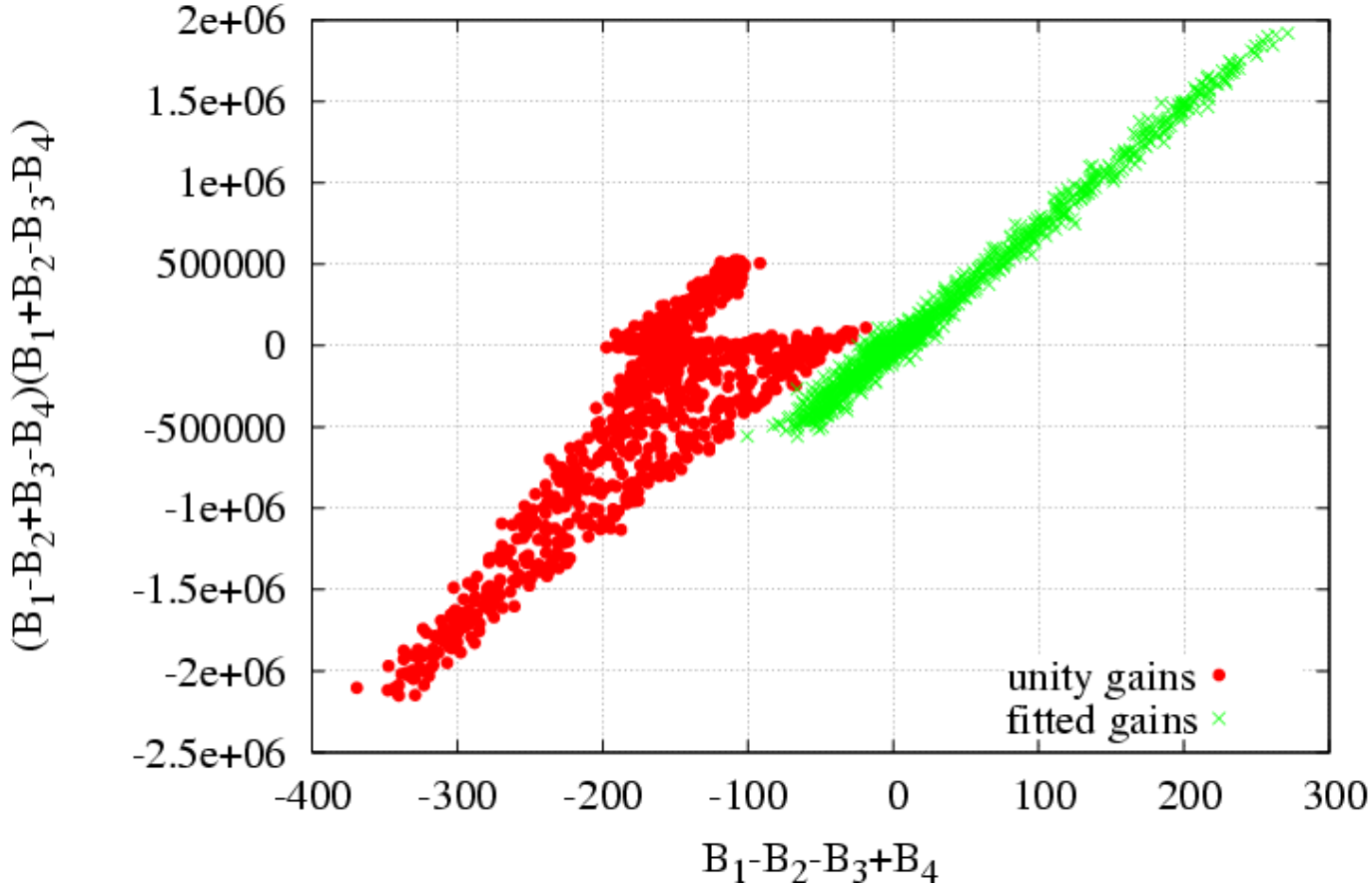
Immediately followed by
measurement of phase.8607
and ac_eta.165

1. Use turn by turn data to determine gains
2. Use fitted gains to correct coupling and eta measurements

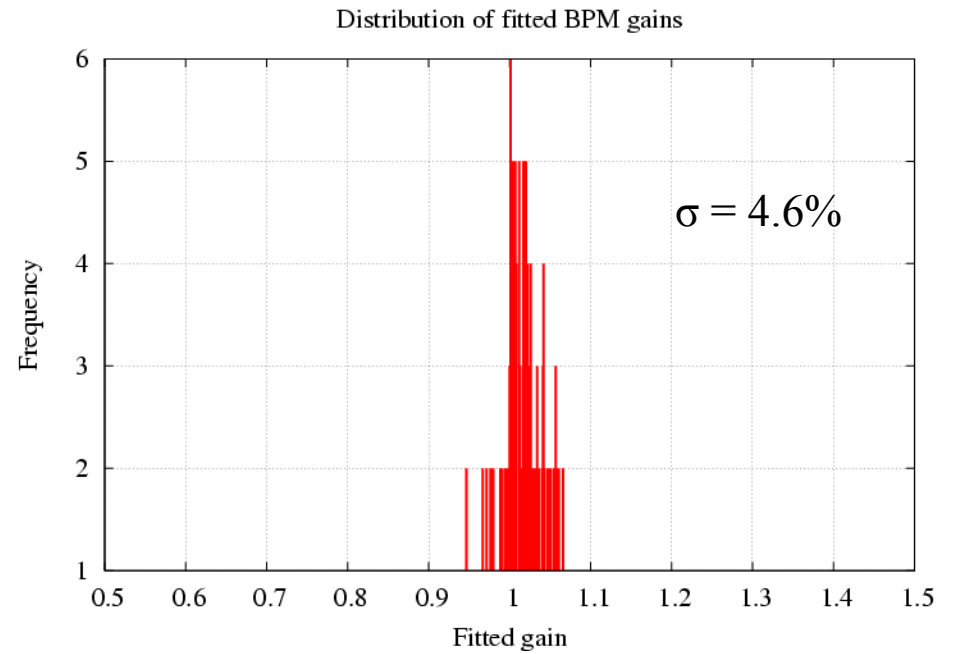
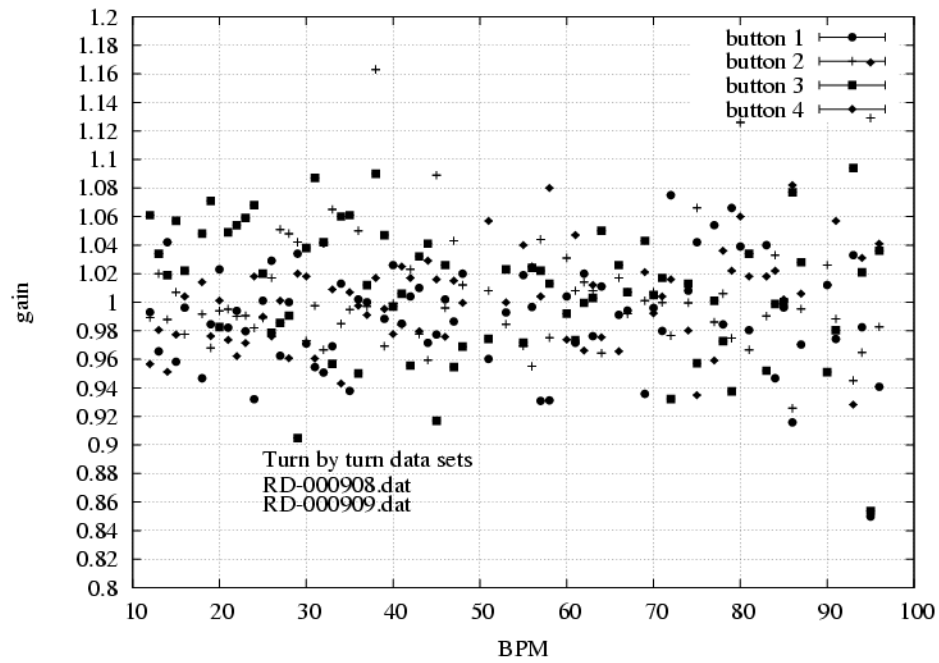
Examples of fits for various BPMs



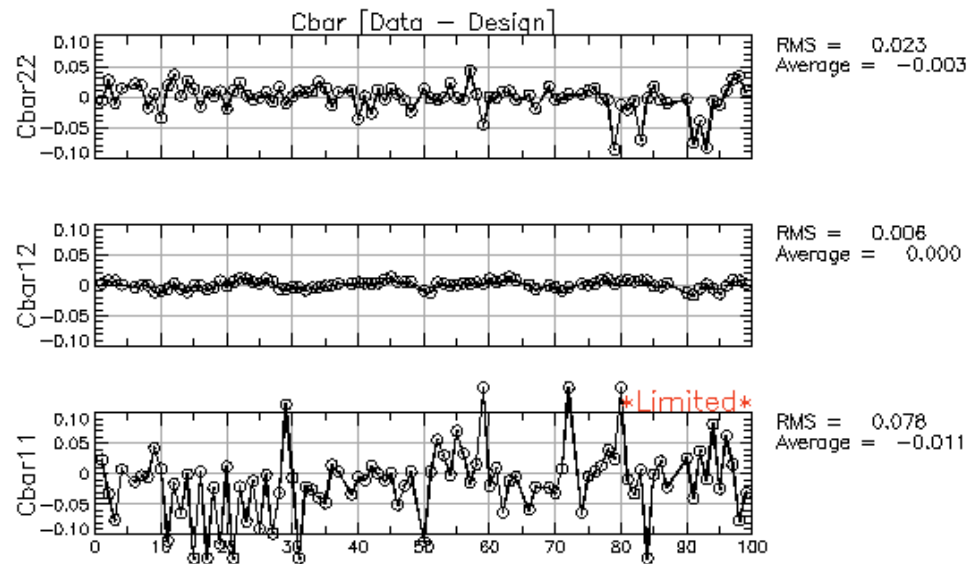
BPM 24E



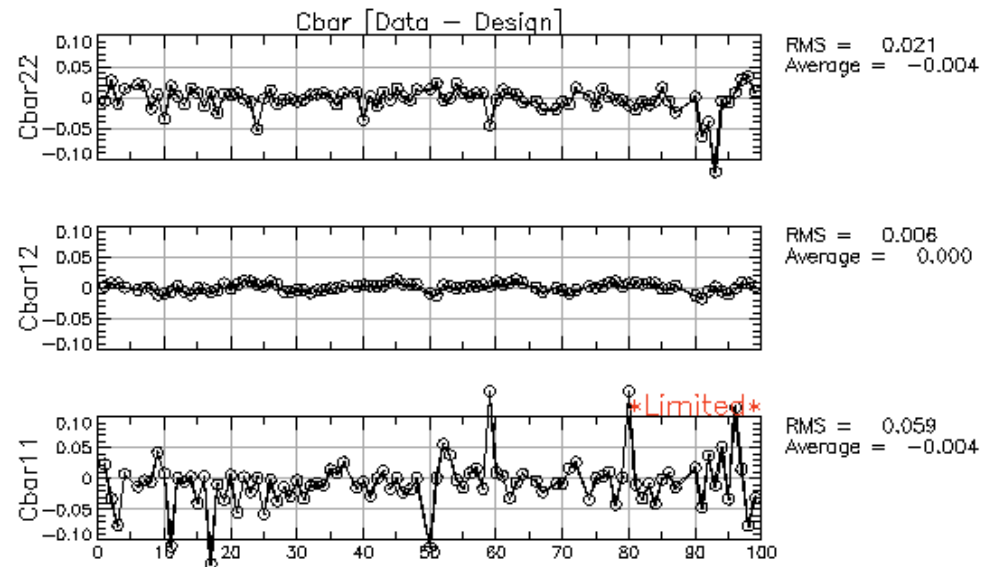
Summary of fitted gains



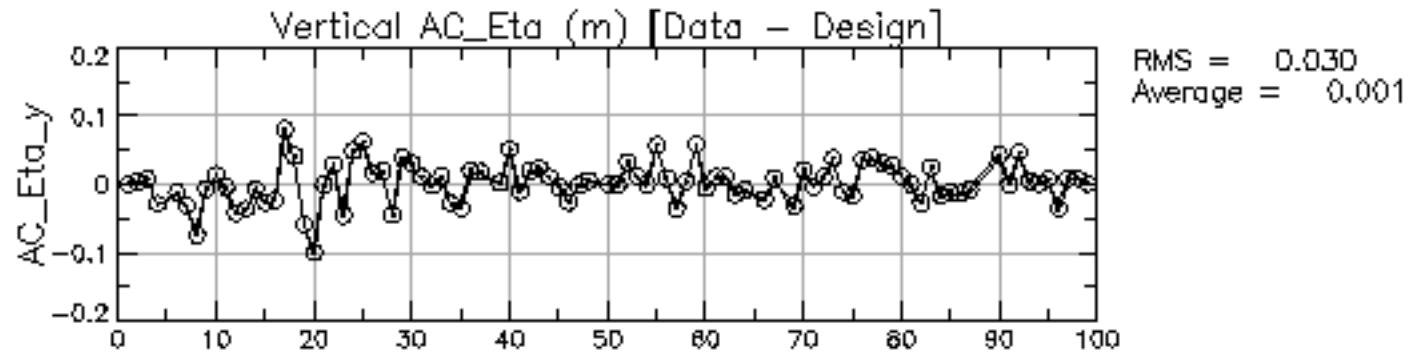
Coupling without gain correction



Coupling with gain correction



Dispersion without
gain correction



Dispersion with
gain correction

