

1. Ampere's law states that

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J}$$

Because $\nabla \cdot \mathbf{B} = 0$ we can write $\mathbf{B} = \nabla \times \mathbf{A}$, where \mathbf{A} is the so-called vector potential, since the divergence of a curl is always 0. Ampere's law can thus be written as

$$\nabla^2 \mathbf{A} = -\mu_0 \mathbf{J}$$

- A) always
- B) sometimes
- C) never
- D) as long as $\nabla \cdot \mathbf{A} = 0$

2. An infinite uniform surface current $\mathbf{K} = k\hat{\mathbf{x}}$ is flowing over the x-y plane. The magnetic field above the plane is

A) $\mathbf{B} = (\mu_0/2)k\hat{\mathbf{z}}$

B) $\mathbf{B} = (\mu_0/2)k\hat{\mathbf{x}}$

C) $\mathbf{B} = (\mu_0/2)k\hat{\mathbf{y}}$

D) $\mathbf{B} = -(\mu_0/2)k\hat{\mathbf{y}}$

3. An infinite uniform surface current $\mathbf{K} = k\hat{\mathbf{x}}$ is flowing over the x-y plane. The vector potential above the plane is

A) $\mathbf{A} = -\frac{\mu_0}{2}ky\hat{\mathbf{y}}$

B) $\mathbf{A} = \frac{\mu_0}{2}kx\hat{\mathbf{y}}$

C) $\mathbf{A} = \frac{\mu_0}{2}kx\hat{\mathbf{z}}$

D) $\mathbf{A} = -\frac{\mu_0}{2}ky\hat{\mathbf{z}}$

4. The magnetic dipole moment of a current loop is $\mathbf{m} = I \int d\mathbf{a} = I\mathbf{a}$ where \mathbf{a} is the vector area of the loop. The magnetic dipole moment of a square loop, with sides w that lies in the y-z plane is

A) $\mathbf{m} = w^2 I \hat{\mathbf{x}}$

B) $\mathbf{m} = -w^2 I \hat{\mathbf{x}}$

C) $\mathbf{m} = -2w I \hat{\mathbf{z}}$

D) $\mathbf{m} = -w^2 I \hat{\mathbf{y}}$

5. The magnetic field on the axis of a current loop with dipole moment \mathbf{m} is

A)

$$\mathbf{B} = \frac{2\mu_0}{4\pi} \frac{\mathbf{m}}{z^3}$$

B)

$$\mathbf{B} = -\frac{2\mu_0}{4\pi} \frac{\mathbf{m}}{z^2}$$

C)

$$\mathbf{B} = \frac{2\mu_0}{4\pi} \frac{\mathbf{m}}{z}$$

D)

$$\mathbf{B} = \frac{2\mu_0}{4\pi} \frac{\mathbf{m}}{z^4}$$