

## **Advanced Accelerator Physics**



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# CHESS & LEPP

#### **Required:**

Particle Accelerator Physics I, Helmut Wiedemann, Springer, 2nd edition, 1999, ISBN 3 540 64671 x

#### **Optional:**

The Physics of Particle Accelerators, Klaus Wille, Oxford University Press, 2000, ISBN: 19 850549 3

#### **Related material:**

Handbook of Accelerator Physics and Engineering, Alexander Wu Chao and Maury Tigner, 2nd edition, 2002, World Scientific, ISBN: 981 02 3858 4

Particle Accelerator Physics II, Helmut Wiedemann, Springer, 2nd edition, 1999, ISBN 3 540 64504 7





<u>Accelerator Physics</u> has applications in particle accelerators for high energy physics or for x-ray science, in spectrometers, in electron microscopes, and in lithographic devices. These instruments have become so complex that an empirical approach to properties of the particle beams is by no means sufficient and a detailed theoretical understanding is necessary. This course will introduce into theoretical aspects of charged particle beams and into the technology used for their acceleration.

- Physics of beams
- Physics of non-neutral plasmas
- Physics of involved in the technology:
  - Superconductivity in magnets and radiofrequency (RF) devices
  - Surface physics in particle sources, vacuum technology, RF devices
  - Material science in collimators, beam dumps, superconducting materials





# A short history of accelerators

- 1862: Maxwell theory of electromagnetism
- 1887: Hertz discovery of the electromagnetic wave
- 1886: Goldstein discovers positively charged rays (ion beams)
- 1894: Lenard extracts cathode rays (with a 2.65um AI Lenard window)
- 1897: JJ Thomson shows that cathode rays are particles since they followed the classical Lorentz force  $m\vec{a} = e(\vec{E} + \vec{v} \times \vec{B})$  in an electromagnetic field
- 1926: GP Thomson shows that the electron is a wave (1929-1930 in Cornell, NP in 1937)





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• 1911: Rutherford discovers the nucleus with 7.7MeV <sup>4</sup>He from <sup>214</sup>Po alpha decay measuring the elastic crossection of <sup>197</sup>Au + <sup>4</sup>He  $\mapsto$  <sup>197</sup>Au + <sup>4</sup>He.



$$E = \frac{Z_1 e Z_2 e}{4\pi\varepsilon_0 d} = Z_1 Z_2 m_e c^2 \frac{r_e}{d},$$

$$r_e = 2.8 \text{fm}, \quad m_e c^2 = 0.511 \text{MeV}$$

d = smalles approach for back scattering

- 1919: Rutherford produces first nuclear reactions with natural <sup>4</sup>He  $^{14}N + {}^{4}He \mapsto {}^{17}O + p$
- 1921: Greinacher invents the cascade generator for several 100 keV
- Rutherford is convinced that several 10 MeV are in general needed for nuclear reactions. He therefore gave up the thought of accelerating particles.



## Tunneling allows low energies



1928: Explanation of alpha decay by Gamov as tunneling showed that several 100keV protons might suffice for nuclear reactions

Schroedinger equation:

$$\frac{\partial^2}{\partial r^2}u(r) = \frac{2m}{\hbar^2} [V(r) - E]u(r), \quad T = \left|\frac{u(L)}{u(0)}\right|^2$$

The transmission probability T for an alpha particle traveling from the inside towards the potential well that keeps the nucleus together determines the lifetime for alpha decay.





# Three historic lines of accelerators



#### **Direct Voltage Accelerators**



The energy limit is given by the maximum possible voltage. At the limiting voltage, electrons and ions are accelerated to such large energies that they hit the surface and produce new ions. An avalanche of charge carries causes a large current and therefore a breakdown of the voltage.







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### The Marx Generator



1932: Marx Generator achieves 6MV at General Electrics



After capacitors of around 2uF are filled to about 20kV, the spark gaps or switches close as fast as 40ns, allowing up to 500kA.

Today:

The Z-machine (Physics Today July 2003) for z-pinch initial confinement fusion has 40TW for 100ns from 36 Marx generators



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# **First Medical Applications**



1939: Lawrence uses 60' cyclotron for 9MeV protons, 19MeV deuterons, and 35MeV 4He. First tests of tumor therapy with neutrons via d + t  $\mapsto$  n +  $\alpha$  With 200-800keV d to get 10MeV neutrons.







# The microtron



Electrons are quickly relativistic and cannot be accelerated in a cyclotron.
In a microtron the revolution frequency changes, but each electron misses an integer number of RF waves.



•Nuclear physics: MAMI designed for 820MeV as race track microtron.



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# Accelerating cavities

1933: J.W. Beams uses resonant cavities for acceleration







### Phase focusing



 1945: Veksler (UDSSR) and McMillan (USA) realize the importance of phase focusing



Phase focusing is required in any RF accelerator.



# The RF quadrupole (RFQ)





#### 1970: Kapchinskii and Teplyakov invent the RFQ







TIME:  $\triangle T_1, \triangle T_5, \ldots$ 

 $t_0, t_2, t_4, \dots$ 







INJECTED BEAM ACCELERATE

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### **The Betatron Condition**



Condition: 
$$R = \frac{-p_{\varphi}(t)}{qB_{z}(R,t)} = \text{const.}$$
 given  $\oint_{\partial A} \vec{E} \cdot d\vec{s} = -\iint_{A} \frac{d}{dt} \vec{B} \cdot d\vec{a}$   
 $E_{\varphi}(R,t) = -\frac{1}{2\pi R} \int \frac{d}{dt} B_{z}(r,t) r dr d\varphi = -\frac{R}{2} \left\langle \frac{d}{dt} B_{z} \right\rangle$   
 $\frac{d}{dt} p_{\varphi}(t) = qE_{\varphi}(R,t) = -q \frac{R}{2} \left\langle \frac{d}{dt} B_{z} \right\rangle$   
 $p_{\varphi}(t) = p_{\varphi}(0) - q \frac{R}{2} [\left\langle B_{z} \right\rangle(t) - \left\langle B_{z} \right\rangle(0)] = -RqB_{z}(R,t)$   
 $B_{z}(R,t) - B_{z}(R,0) = \frac{1}{2} [\left\langle B_{z} \right\rangle(t) - \left\langle B_{z} \right\rangle(0)]$ 

Small deviations from this condition lead to transverse beam oscillations called betatron oscillations in all accelerators.

Today: Betatrons with typically about 20MeV for medical applications



# The Synchrotron



- 1945: Veksler (UDSSR) and McMillan (USA) invent the synchrotron
- 1946: Goward and Barnes build the first synchrotron (using a betatron magnet)
- 1949: Wilson et al. at Cornell are first to store beam in a synchrotron (later 300MeV, magnet of 80 Tons)
- 1949: McMillan builds a 320MeV electron synchrotron
- Many smaller magnets instead of one large magnet
- Only one acceleration section is needed, with

$$R = \frac{p(t)}{qB(R,t)} = \text{const.}$$
$$\omega = 2\pi \frac{v_{\text{particle}}}{n}$$

for an integer n called the harmonic number





## Rober R Wilson, Architecture



#### Wilson Hall, FNAL

Science Ed Center, FNAL (1990)



Robert R Wilson USA 1914-2000

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# Rober R Wilson, Cornell & FNAL





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# Strong focusing Synchrotrons



- 1952: Courant, Livingston, Snyder publish about strong focusing
- 1954: Wilson et al. build first synchrotron with strong focusing for 1.1MeV electrons at Cornell, 4cm beam pipe height, only 16 Tons of magnets.
- 1959: CERN builds the PS for 28GeV after proposing a 5GeV weak focusing accelerator for the same cost (still in use)

Transverse fields defocus in one plane if they focus in the other plane. But two successive elements, one focusing the other defocusing, can focus in both planes:







# **Colliding Beam Accelerators**



- 1961: First storage ring for electrons and positrons (AdA) in Frascati for 250MeV
- 1972: SPEAR electron positron collider at 4GeV. Discovery of the J/Psi at 3.097GeV by Richter (SPEAR) and Ting (AGS) starts the November revolution and was essential for the quarkmodel and chromodynamics.
- 1979: 5GeV electron positron collider CESR (designed for 8GeV)

#### Advantage:

More center of mass energy





Drawback:

Less dense target

The beams therefore must be stored for a long time.





# Storage Rings



To avoid the loss of collision time during filling of a synchrotron, the beams in colliders must be stored for many milions of turns.

#### Chalenges:

•Required vacuum of pressure below  $10^{-7}$  Pa =  $10^{-9}$  mbar, 3 orders of magnitude below that of other accelerators.

• Fields must be stable for a long time, often for hours.

• Field errors must be small, since their effect can add up over millions of turns.

• Even though a storage ring does not accelerate, it needs acceleration sections for phase focusing and to compensate energy loss due to the emission of radiation.



# **Further Development of Colliders**



- 1981: Rubbia and van der Meer use stochastic cooling of antiportons and discover W+,W- and Z vector bosons of the weak interaction
- 1987: Start of the superconducting TEVATRON at FNAL
- 1989: Start of the 27km long LEP electron positron collider
- 1990: Start of the first asymmetric collider, electron (27.5GeV) proton (920GeV) in HERA at DESY
- 1998: Start of asymmetric two ring electron positron colliders KEK-B / PEP-II
- Today: 27km, 7 TeV proton collider LHC being build at CERN





# **Special Relativity**

 $E = mc^2$ 



Albert Einstein, 1879-1955 Nobel Prize, 1921 Time Magazine Man of the Century

#### Four-Vectors:

Quantities that transform according to the Lorentz transformation when viewed from a different inertial frame.

#### Examples:

$$X^{\mu} \in \{ct, x, y, z\}$$

$$P^{\mu} \in \{\frac{1}{c}E, p_{x}, p_{y}, p_{z}\}$$

$$\Phi^{\mu} \in \{\frac{1}{c}\phi, A_{x}, A_{y}, A_{z}\}$$

$$J^{\mu} \in \{c\rho, j_{x}, j_{y}, j_{z}\}$$

$$K^{\mu} \in \{\frac{1}{c}\omega, k_{x}, k_{y}, k_{z}\}$$

$$X^{\mu} \in \{ct, x, y, z\} \implies X^{\mu} X_{\mu} = (ct)^{2} - \vec{x}^{2} = \text{const.}$$
$$P^{\mu} \in \{\frac{1}{c} E, p_{x}, p_{y}, p_{z}\} \implies P^{\mu} P_{\mu} = \left(\frac{E}{c}\right)^{2} - \vec{p}^{2} = (m_{0}c)^{2} = \text{const.}$$



38 Available Energy  

$$\frac{1}{c^2} E_{cm}^2 = (P_1^{\mu} + P_2^{\mu})_{cm} (P_{1\mu} + P_{2\mu})_{cm}$$

$$= (P_1^{\mu} + P_2^{\mu})(P_{1\mu} + P_{2\mu})$$

$$= \frac{1}{c^2}(E_1 + E_2)^2 - (p_{z1} - p_{z2})^2$$

$$= 2(\frac{E_1E_2}{c^2} + p_{z1}p_{z2}) + (m_{01}c)^2 + (m_{02}c)^2$$
Operation of synchrotrons: fixed target experiments  
where some energy is in the motion of the center off  
mass of the scattering products  

$$E_1 >> m_{01}c^2, m_{02}c^2; p_{z2} = 0; E_2 = m_{02}c^2 \implies E_{cm} = \sqrt{2E_1m_{02}c^2}$$
Operation of colliders:  
the detector is in the center of mass system  

$$E_1 >> m_{01}c^2; E_2 >> m_{02}c^2 \implies E_{cm} = 2\sqrt{E_1E_2}$$







1954: Operation of Bevatron, first proton synchrotron for 6.2GeV, production of the antiporton by Chamberlain and Segrè

$$p + p \mapsto p + p + p + \overline{p}$$

$$\frac{1}{c^2}E_{\rm cm}^2 = 2(\frac{E_1E_2}{c^2} + p_{z1}p_{z2}) + (m_{01}c)^2 + (m_{02}c)^2$$

$$(4m_{p0}c)^{2} < \frac{1}{c^{2}}E_{cm}^{2} = 2\frac{E_{1}m_{p0}}{c^{2}} + (m_{p0}c)^{2} + (m_{p0}c)^{2}$$

$$7m_{p0}c^2 < E_1$$



$$K_1 = E_1 - m_0 c^2 > 6m_{p0} c^2 = 5.628 \text{ GeV}$$

NP 1959

USA 1920 - 2006



NP 1959 Emilio Gino Segrè Italy 1905 - USA 1989

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# **Rings for Synchrotron Radiation**



- 1947: First detection of synchrotron light at General Electrics.
- 1952: First accurate measurement of synchrotron radiation power by Dale Corson with the Cornell 300MeV synchrotron.
- 1968: TANTALOS, first dedicated storage ring for synchrotron radiation





Dale Corson Cornell's 8<sup>th</sup> president USA 1914 –



# **3 Generations of Light Sources**



- 1<sup>st</sup> Genergation (1970s): Many HEP rings are parasitically used for X-ray production
- 2<sup>nd</sup> Generation (1980s): Many dedicated X-ray sources (light sources)
- 3<sup>rd</sup> Generation (1990s): Several rings with dedicated radiation devices (wigglers and undulators)
- Today (4<sup>th</sup> Generation): Construction of Free Electron Lasers (FELs) driven by LINACs





## Accelerators of the World



#### Sorted by Location

#### Europe

100P	Association Operation on Operation of Netherlands
AGUR	Accelerateur Groningen-ORsay, KVI Groningen, Netherlands
ANKA	Angstromquelle Karlsruhe, Karlsruhe, Germany (Forschungsgruppe Synchrotronstrahlung (FGS))
ASTRID	Aarhus Storage Ring in Denmark, ISA, Aarhus, Denmark
BESSY	Berliner Elektronenspeicherring-Gesellschaft für Synchrotronstrahlung, Germany (BESSY I status, BESSY II status)
BINP	Budker Institute for Nuclear Physics, Novosibirsk, Russian Federation (VEPP-2M collider, VEPP-4M collider (status))
CERN	Centre Europeen de Recherche Nucleaire, Geneva, Suisse (LEP & SPS Status, LHC, CLIC, PS-Division, SL-Division)
COSY	Cooler Synchrotron, IKP, FZ Jülich, Germany (COSY Status)
CYCLONE	Cyclotron of Louvain la Neuve, Louvain-la-Neuve, Belgium
DELTA	Dortmund Electron Test Accelerator, U of Dortmund, Germany (DELTA Status)
DESY	Deutsches Elektronen Synchrotron, Hamburg, Germany (HERA, PETRA and DORIS status, TESLA)
ELBE	ELectron source with high Brilliance and low Emittance, FZ Rossendorf, Germany
ELETTRA	Trieste, Italy (ELETTRA status)
ELSA	Electron Stretcher Accelerator, Bonn University, Germany (ELSA status)
ESRF	European Synchrotron Radiation Facility, Grenoble, France (ESRF status)
GANIL	Grand Accélérateur National d'Ions Lourds, Caen, France
GSI	Gesellschaft für Schwerionenforschung, Darmstadt, Germany
IHEP	Institute for High Energy Physics, Protvino, Moscow region, Russian Federation
INFN	Istituto Nazionale di Fisica Nucleare, Italy, LNF - Laboratori Nazionali di Frascati (DAFNE, other accelerators), LNL - Laboratori Nazionali di Legnaro (Tandem, CN Van de Graaff, AN 2000 Van de Graaff), LNS - Laboratori Nazionali del Sud, Catania, (Superconducting Collider & Van de Graaff Tandem)
ISIS	Rutherford Appleton Laboratory, Oxford, U.K. (ISIS Status)
ISL	IonenStrahlLabor am HMI, Berlin, Germany
JINR	Joint Institute for Nuclear Research, Dubna, Russian Federation (U-200, U-400, U-400M, Storage Ring, LHE Synchrophasotron / Nuclotron)
JYFL	Jyväskylän Yliopiston Fysiikan Laitos, Jyväskylä, Finland
КТН	Kungl Tekniska Högskola (Royal Institute of Technology), Stockholm, Sweden (Alfén Lab electron accelerators)



### Accelerators of the World



LMU/TUM	Accelerator of LMU and TU Muenchen, Munich, Germany
LURE	Laboratoire pour l'Utilisation du Rayonnement Electromagnétique, Orsay, France (DCI, Super-ACO status, CLIO)
MAMI	Mainzer Microtron, Mainz U, Germany
MAX-Lab	Lund University, Sweden
MSL	Manne Siegbahn Laboratory, Stockholm, Sweden (CRYRING)
NIKHEF	Nationaal Instituut voor Kernfysica en Hoge-Energie Fysica, Amsterdam, Netherlands (AmPS closed)
PSI	Paul Scherrer Institut, Villigen, Switzerland (PSI status, SLS under construction)
S-DALINAC	Darmstadt University of Technology, Germany (S-DALINAC status)
SRS	Synchrotron Radiation Source, Daresbury Laboratory, Daresbury, U.K. (SRS Status)

- TSL The Svedberg Laboratory, Uppsala University, Sweden (CELSIUS)
- TSR Heavy-Ion Test Storage Ring, Heidelberg, Germany

#### **North America**

88" Cycl.	88-Inch Cyclotron, Lawrence Berkeley Laboratory (LBL), Berkeley, CA	
ALS	Advanced Light Source, Lawrence Berkeley Laboratory (LBL), Berkeley, CA (ALS Status)	
ANL	Argonne National Laboratory, Chicago, IL (Advanced Photon Source APS [status], Intense Pulsed Neutron Source IPNS [status], Argonne Tandem Linac Accelerator System ATLAS)	
BNL	Brookhaven National Laboratory, Upton, NY (AGS, ATF, NSLS, RHIC)	
CAMD	Center for Advanced Microstructures and Devices	
CHESS	Cornell High Energy Synchrotron Source, Cornell University, Ithaca, NY	
CLS	Canadian Light Source, U of Saskatchewan, Saskatoon, Canada	
CESR	Cornell Electron-positron Storage Ring, Cornell University, Ithaca, NY (CESR Status)	
FNAL	Fermi National Accelerator Laboratory , Batavia, IL (Tevatron)	
IAC	Idaho accelerator center, Pocatello, Idaho	
IUCF	Indiana University Cyclotron Facility, Bloomington, Indiana	
JLab	aka TJNAF, Thomas Jefferson National Accelerator Facility (formerly known as CEBAF), Newport News, VA	
LAC	Louisiana Accelerator Center, U of Louisiana at Lafayette, Louisiana	
LANL	Los Alamos National Laboratory	
MIT-Bates	Bates Linear Accelerator Center, Massachusetts Institute of Technology (MIT)	
NSCL	National Superconducting Cyclotron Laboratory, Michigan State University	
ORNL	Oak Ridge National Laboratory (EN Tandem Accelerator), Oak Ridge, Tennessee	
SBSL	Stony Brook Superconducting Linac, State University of New York (SUNY)	
SLAC	Stanford Linear Accelerator Center (Linac, NLC - Next Linear Collider, PEP - Positron Electron Project (finished), PEP-II - asymmetric B Factory (in commissioning), SLC - SLAC Linear electron positron Collider, SPEAR - Stanford Positron Electron Asymmetric Ring (actually SPEAR-II, see SSRL), SSRL - Stanford Synchrotron Radiation Laboratory)	
SNS	Spallation Neutron Source, Oak Ridge, Tennessee	
SRC	Synchrotron Radiation Center, U of Wisconsin - Madison (Aladdin Status)	

- SURF II Synchrotron Ultraviolet Radiation Facility, National Institute of Standards and Technology (NIST), Gaithersburg, Maryland
- TASCC Tandem Accelerator Superconducting Cyclotron (Canada) (closed!)
- TRIUME TRI-University Meson Facility / National Meson Research Facility, Vancouver, BC (Canada)

#### South America

- LNLS Laboratorio Nacional de Luz Sincrotron, Campinas SP, Brazil
- TANDAR Tandem Accelerator, Buenos Aires, Argentina

#### Asia

- BEPC Beijing Electron-Positron Collider, Beijing, China
- KEK National Laboratory for High Energy Physics ("Koh-Ene-Ken"), Tsukuba, Japan (KEK-B, PF, JLC)
- NSC Nuclear Science Centre, New Delhi, India (15 UD Pelletron Accelerator)
- PLS Pohang Light Source, Pohang, Korea
- RIKEN Institute of Physical and Chemical Research ("Rikagaku Kenkyusho"), Hirosawa, Wako, Japan
  - SESAME Synchrotron-light for Experimental Science and Applications in the Middle East, Jordan (under construction)
- SPring-8 Super Photon ring 8 GeV, Japan
- SRRC Synchrotron Radiation Research Center, Hsinchu, Taiwan (SRRC Status)
- UVSOR Ultraviolet Synchrotron Orbital Radiation Facility, Japan
- VECC Variable Energy Cyclotron, Calcutta, India

#### Africa

NAC National Accelerator Centre, Cape Town, South Africa

#### Sorted by Accelerator Type

#### Electrons

#### Stretcher Ring/Continuous Beam facilities

ELSA (Bonn U), JLab, MAMI (Mainz U), MAX-Lab, MIT-Bates, PSR (SAL), S-DALINAC (TH Darmstadt), SLAC

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# Accelerators of the World



#### Synchrotron Light Sources

ANKA (FZK), ALS (LBL), APS (ANL), ASTRID (ISA), BESSY, CAMD (LSU), CHESS (Cornell Wilson Lab), CLS (U of Saskatchewan), DELTA (U of Dortmund), ELBE (FZ Rossendorf), Elettra, ELSA (Bonn U), ESRF, HASYLAB (DESY), LURE, MAX-Lab, LNLS, NSLS (BNL), PF (KEK), UVSOR (IMS), PLS, S-DALINAC (TH Darmstadt), SESAME, SLS (PSI), SPEAR (SSRL, SLAC), SPring-8, SRC (U of Wisconsin), SRRC, SRS (Daresbury), SURF II (NIST)

#### Other

Alfén Lab (KTH), IAC

#### Protons

88" Cyclotron (LBL), CELSIUS (TSL), COSY (FZ Jülich), IPNS (ANL), ISL (HMI), ISIS, IUCF, LHC (CERN), NAC, PS (CERN), PSI, SPS (CERN)

#### Light and Heavy lons

88" Cyclotron (LBL), AGOR, ASTRID (ISA), ATLAS (ANL), CELSIUS (TSL), CRYRING (MSL), CYCLONE, EN Tandem (ORNL), GANIL, GSI, ISL (HMI), IUCF, JYFL, LAC, LHC (CERN), LHE Synchrophasotron / Nuclotron (JINR), LMU/TUM, LNL (INFN), LNS (INFN), NAC, NSC, PSI, RHIC (BNL), SBSL, SNS, SPS (CERN), TANDAR, TSR, U-2007 U-4007 U-400M / Storage Ring (JINR), VECC

#### Collider

BEPC, CESR, DAFNE (LNF), HERA (DESY), LEP (CERN), LHC (CERN), PEP / PEP-II (SLAC), SLC (SLAC), KEK-B (KEK), TESLA (DESY), Tevatron (FNAL), VEPP-2M, VEPP-4M (BINP)

