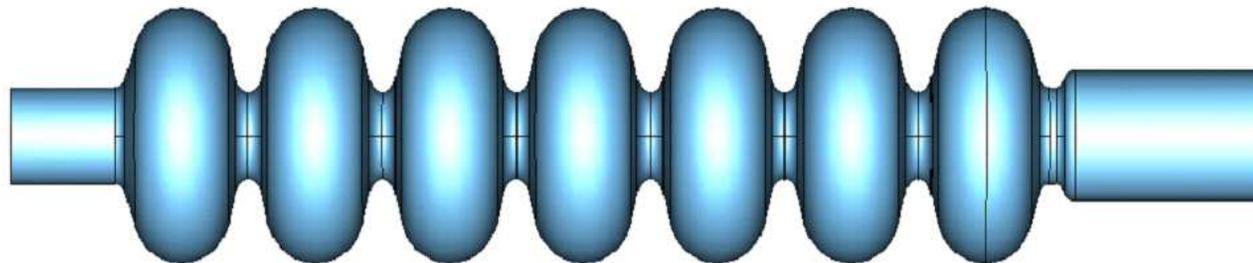


# Accelerating (S)RF Cavities

Matthias Liepe





- **RF Cavity Design**

- Design objectives
- Numerical Eigenmode solver
- Design examples:
  - NC vs. SC
  - SC cavity center cell shape
  - Number of cells of SC cavities
  - SC cavity end cell optimization

- **Higher order modes**

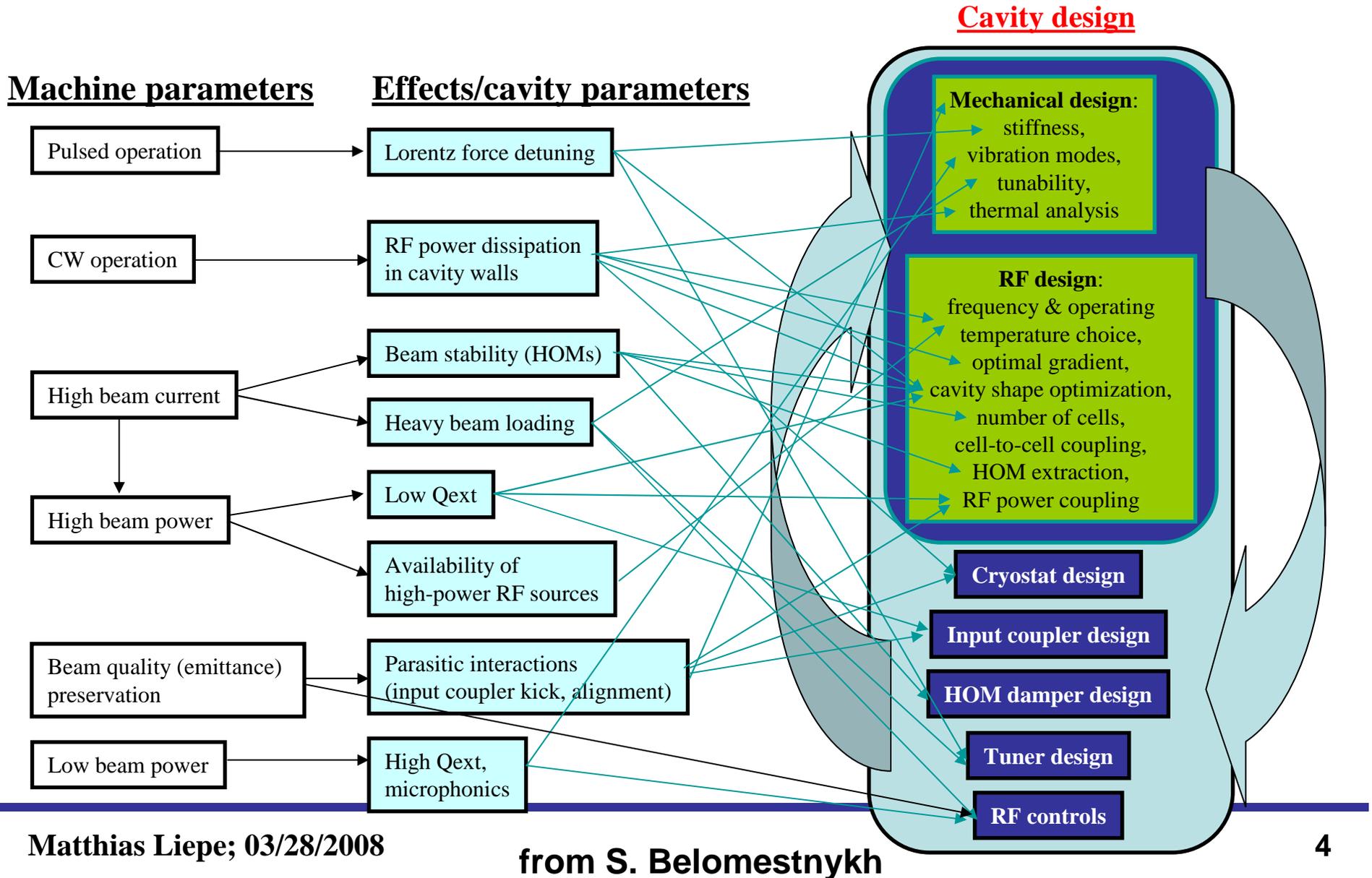
- Introduction: HOMs and excitation by a beam
- HOM damping schemes
- HOM damping examples and results



- **RF Cavity Design**
  - Design objectives
  - Numerical Eigenmode solver
  - Design examples:
    - NC vs. SC
    - SC cavity center cell shape
    - Number of cells of SC cavities
    - SC cavity end cell optimization



# Cavity Design Objectives





## Cavity Design Parameters

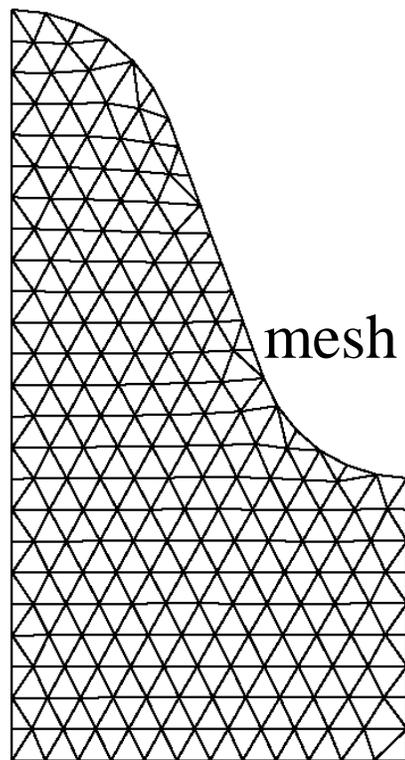
- Choice of material (impacts losses and operating gradient)
- Frequency (impacts size of cavity, cost, surface resistance, assembly technique ...)
- Number of cells (impacts field flatness, tunability, HOM extraction, pulsed operation ...)
- Aperture size (impacts beam stability, peak fields, HOM damping ...)
- Cavity shape (impacts peak surface fields at a given  $E_{acc}$ , power dissipation at a given  $E_{acc}$ , multipacting ...)
- ...



# Numerical Eigenmode Solver

The modes in real cavities (with beam tubes,...)  
cannot be calculated analytically.

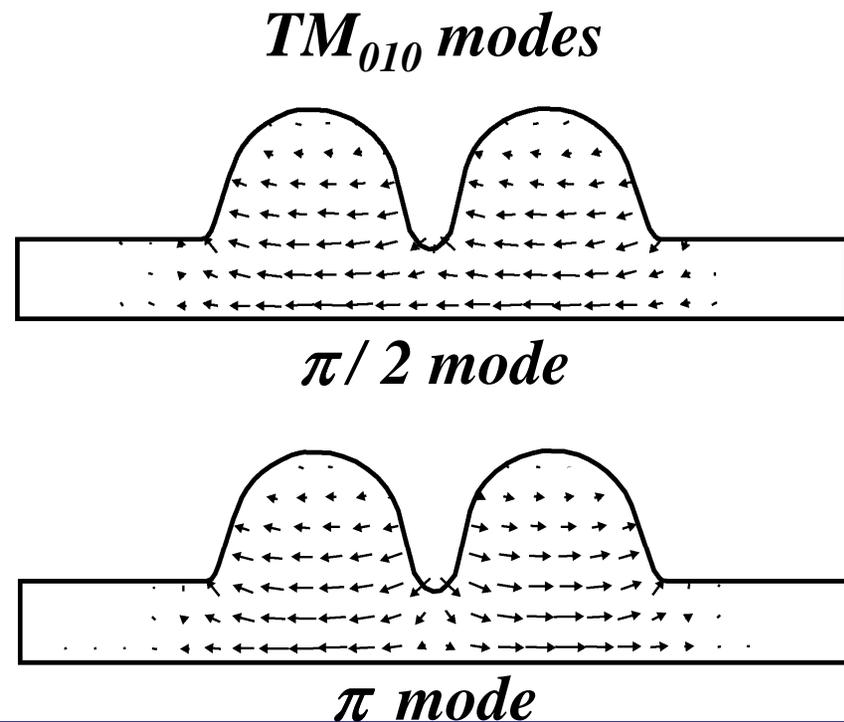
⇒ Use numerical codes (like MAFIA, Microwave studio, SLANS, Superfish,... ).



mesh



modes

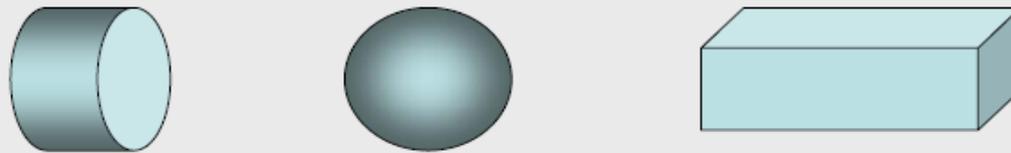




Usually the design of an elliptical cavity is performed in two steps “2D” and “3D” :

- “2D” is fast and allows to define geometry of a cylindrical symmetric body (inner and end-cells) of the cavity.
- “3D” is much more time consuming but necessary for modeling of full equipped cavity with FPC and HOM couplers and if needed to model fabrication errors. Also coupling strength for FPC and damping of HOMs can be modeled only 3D.

The solution to 2D (or 3D) Helmholtz equation can be analytically found only for very few geometries (pillbox, spherical resonators or rectangular resonator):



We need numerical methods:

$$(\nabla^2 + \omega^2 \epsilon \mu) A = 0$$

Approximating operator  
(Finite Difference Methods)

Approximating function  
(Finite Element Methods)

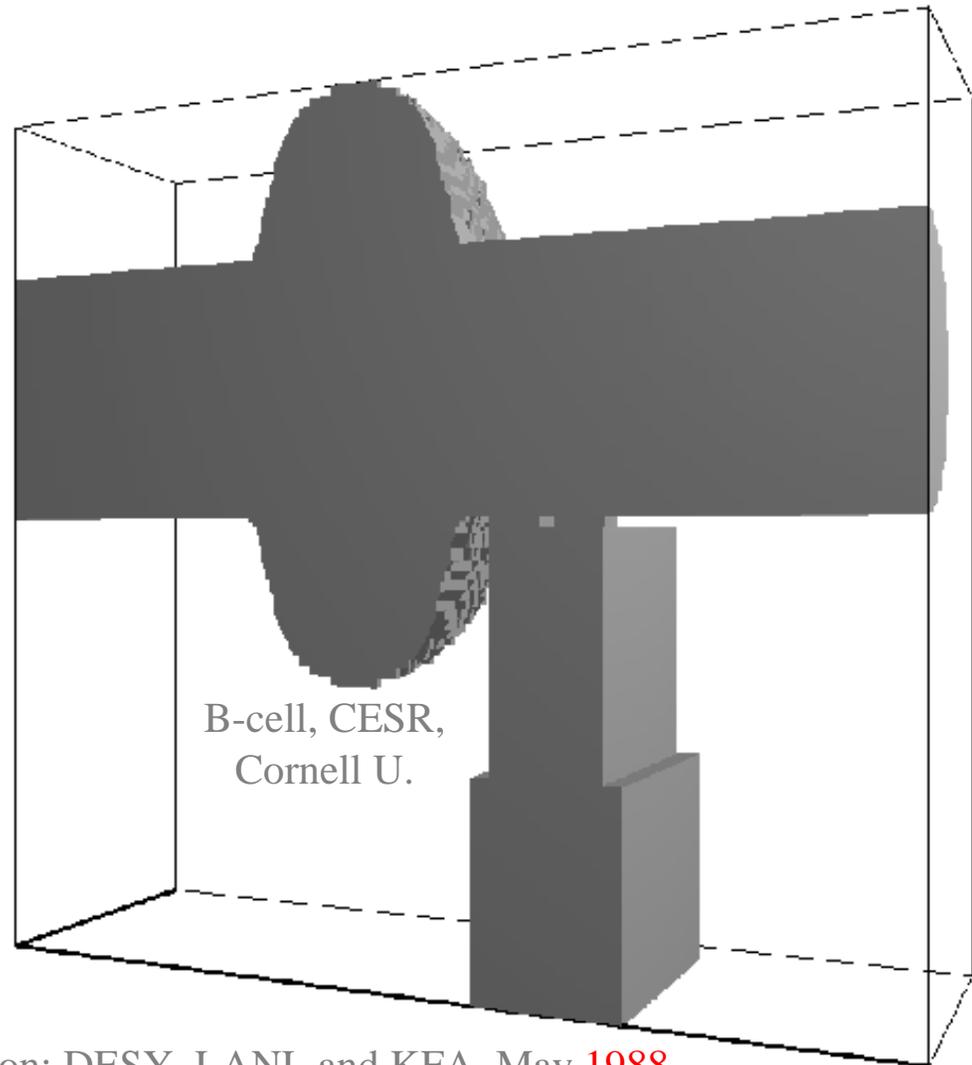


## Examples - MAFIA

MAFIA is a 3D simulation code used for the design of RF cavities and other electromagnetic structures, including electrostatic and magnetostatic devices. It is an acronym for the solution of **MA**xwell's equations using the **F**inite **I**ntegration **A**lgorithm. MAFIA uses a rectangular mesh generation routine which is flexible enough to model even the most complex geometries. The routine allows the user to specify the "coarseness" of the mesh in a particular area of interest.

V. Shemelin, S. Belomestnykh. Calculation of the B-cell cavity external  $Q$  with MAFIA and Microwave Studio. Workshop on high power couplers for SC accelerators. Newport News, VA, 2002.

MAFIA User Guide, The MAFIA Collaboration: DESY, LANL and KFA, May 1988.





## Examples - Microwave Studio

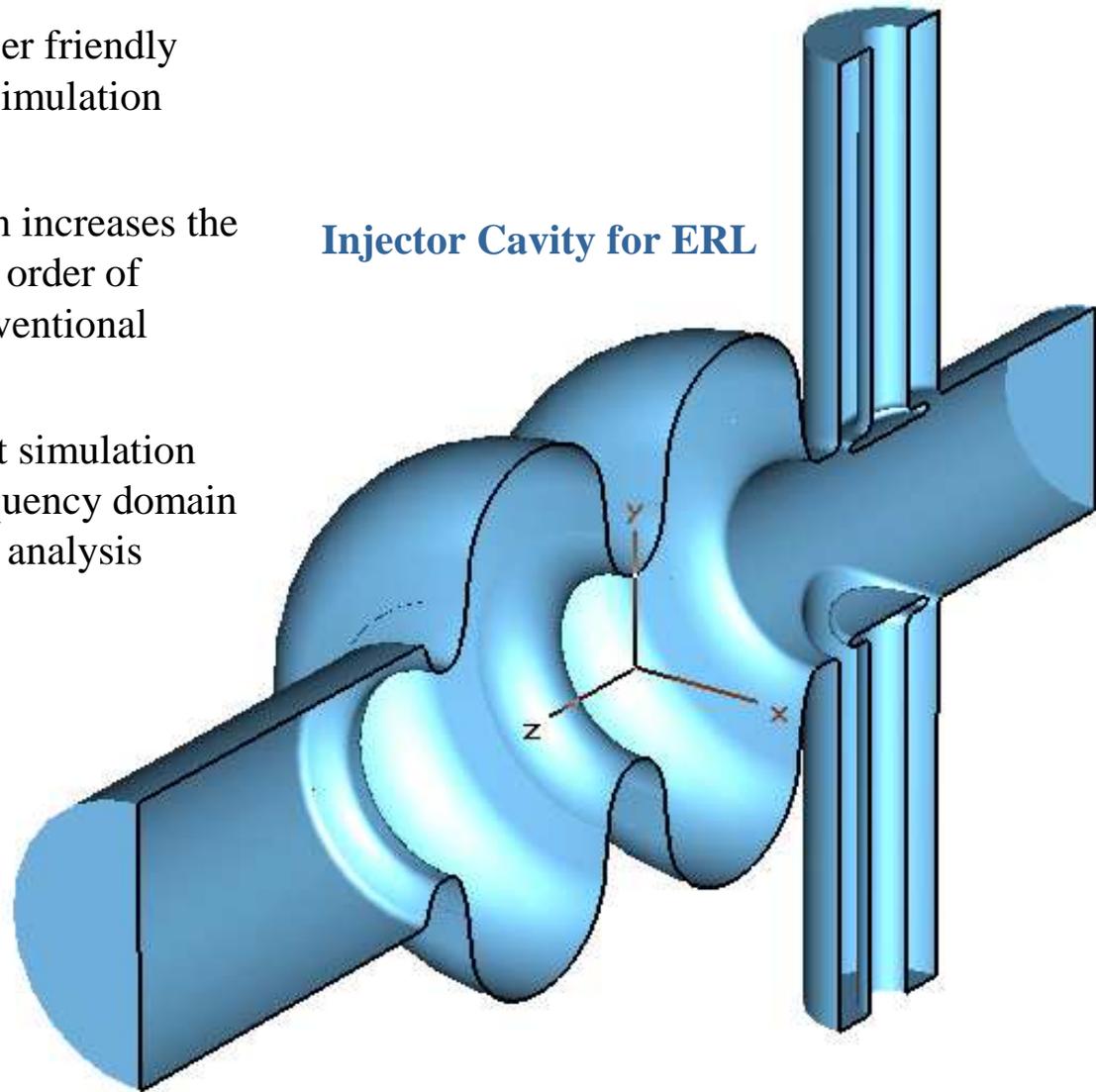
The program combines both a user friendly interface (Windows based) and simulation performance.

Perfect Boundary Approximation increases the accuracy of the simulation by an order of magnitude in comparison to conventional simulators.

The software contains 4 different simulation techniques (transient solver, frequency domain solver, eigenmode solver, modal analysis solver).

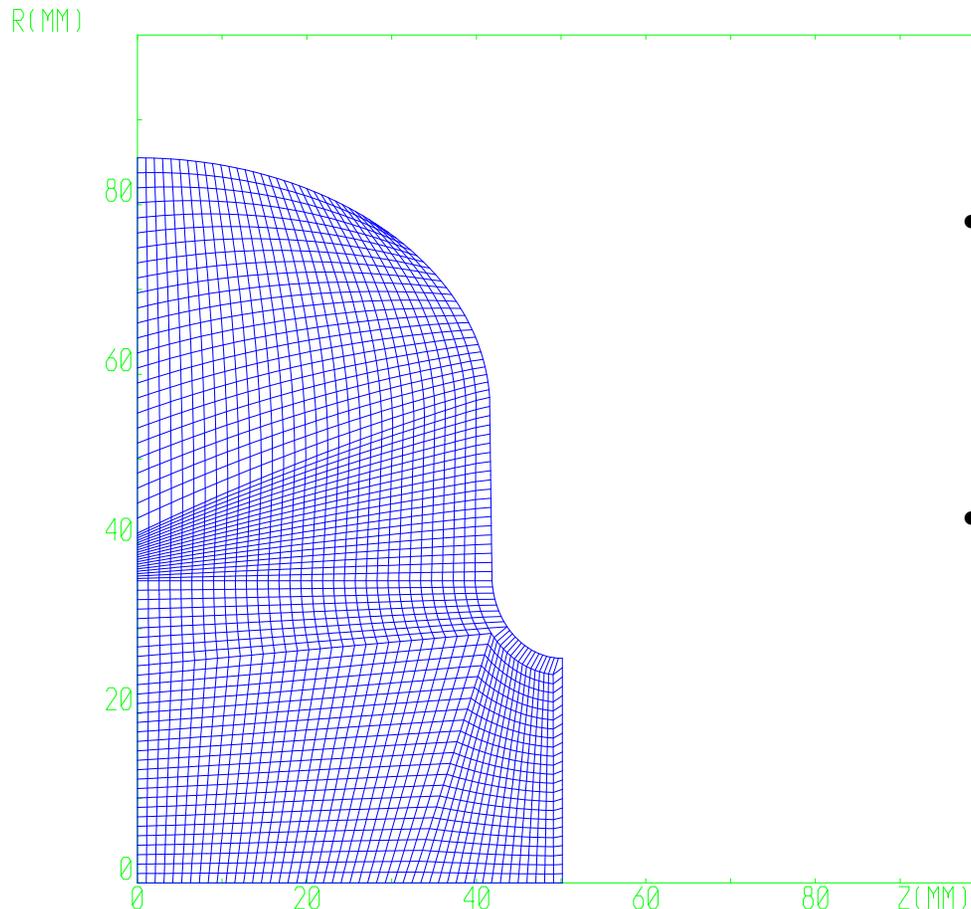
CST Microwave Studio, User Guide, CST GmbH, Buedinger Str. 2a, D-64289, Darmstadt, Germany.

Injector Cavity for ERL





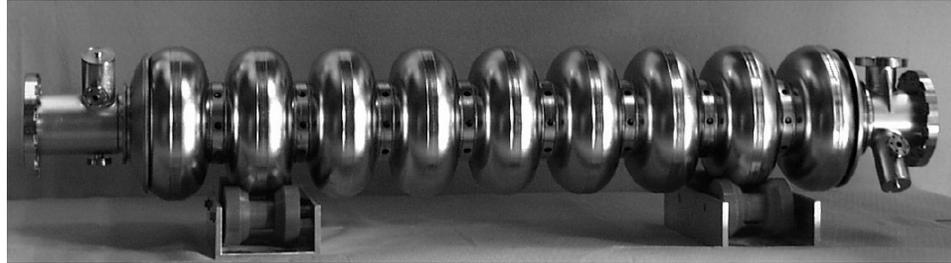
## Examples-SuperLANS / CLANS



- **SuperLANS (or SLANS) is a computer program designed to calculate the monopole modes of RF cavities using a finite element method of calculation and a mesh with quadrilateral biquadratic elements.**
- **SLANS has the ability to calculate the mode frequency, quality factor, stored energy, transit time factor, effective impedance, max electric and magnetic field, acceleration, acceleration rate, average field on the axis, force lines for a given mode, and surface fields.**
- **Later versions, SLANS2 and CLANS2, calculate azimuthally asymmetric modes, and CLANS and CLANS2 can include into geometry lossy dielectrics and ferromagnetics.**



# Design Example 1: Normal conducting vs. Superconducting RF



Power dissipated into the wall:

$$P_{diss} = \frac{1}{2} R_s \int_S |\vec{H}|^2 ds = \frac{V_{acc}^2}{R/Q \cdot G} R_s$$

Example:

- Accelerating voltage: let's take only 1 MV
- Constant R/Q (depends on cell shape): 1000  $\Omega$
- Geometry constant: 270  $\Omega$
- Surface resistance:  $R_{s,copper} = 10 \text{ m}\Omega$   $R_{s,Nb} = 10 \text{ n}\Omega$

$$\Rightarrow P_{diss,copper} = 37 \text{ kW} \quad P_{diss,Nb} = 37 \text{ mW}$$

$\Rightarrow$  Copper is not the best choice for a ILC shape cavity...



**Minimize surface resistance!**

**⇒ Superconducting cavities.**

**mΩ (copper) ⇒ nΩ**

$$P_{diss} = \frac{1}{2} R_s \int_S |\vec{H}|^2 ds = \frac{V_{acc}^2}{R/Q \cdot G} R_s$$

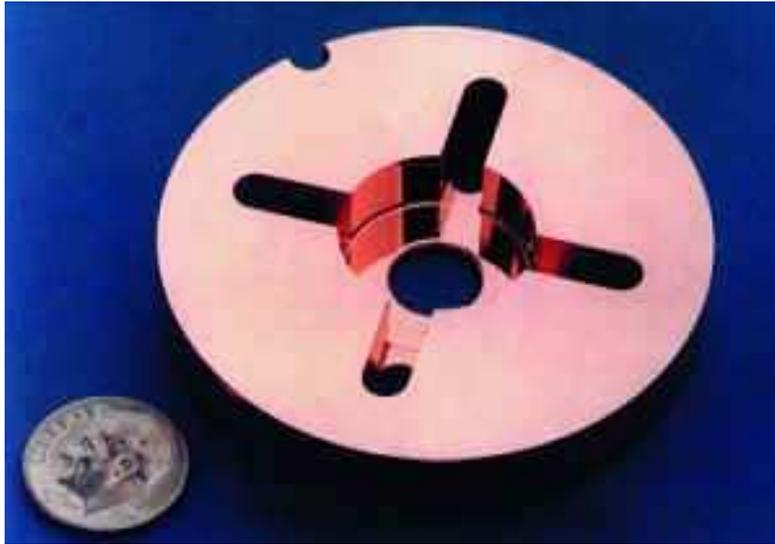
~~**Depend only on cavity geometry.**~~

~~**⇒ Maximize for copper cavities.**~~

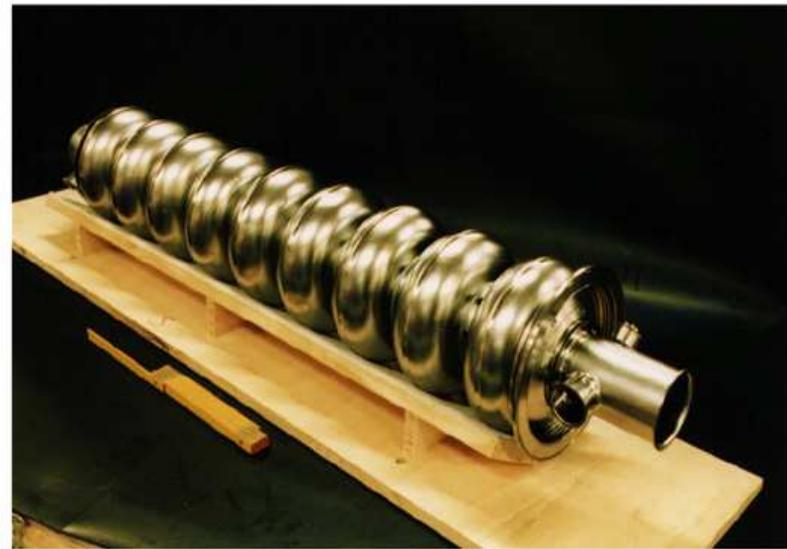
**Less important for SRF cavities!**



## RF Cavities for Linacs



- one cell from NLC
- normal conducting cavity
- copper
- 11.4 GHz
- water cooled



- TESLA
- superconducting cavity
- niobium
- 1.3 GHz
- 2 K (LHe)

**Fundamental differences due to difference in wall losses.**



## Superconducting Cavities: Advantages

- **Can operate at a higher voltage in cw operation or long pulse operation because of low losses.**
- **Power consumption is less.  $\Rightarrow$  Operating cost savings, better conversion of ac power to beam power.**
- **Power dissipation is not the primary concern!  
Can tailor design to a given accelerator application.**

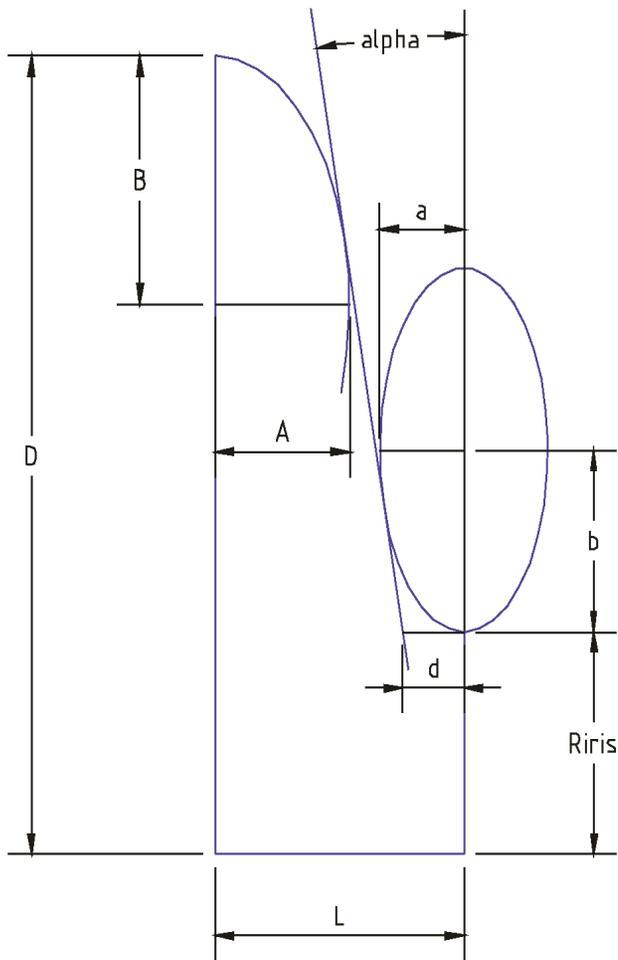


## Superconducting Cavities: Advantages (cont.)

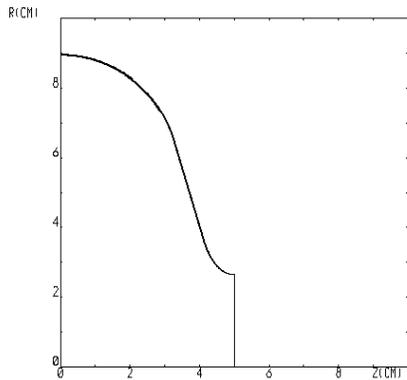
- **Freedom to adapt design better to the accelerator requirements allows, for example, the beam-tube and the cell iris size to be increased:**
  - **Reduces the interaction of the beam with the cavity.**  
(scales as iris radius<sup>2 to 3</sup>) ⇒ The beam quality is better preserved.  
**Important for, e.g., FELs.**
  - **HOMs are removed more easily.** Better beam stability.  
⇒ More current accelerated.  
**Important for, e.g., B-factories.**
  - **Reduce the amount of beam scraping.** ⇒ Less activation in, e.g., proton machines.  
**Important for, e.g., SNS, Neutrino factory.**
  - **Allows more coupling between cells in multicell structures.**  
⇒ Better energy exchange between cells.  
**Important for e.g., high-energy machines.**



## Design Example 2: Center Cell Shape of an SRF Cavity

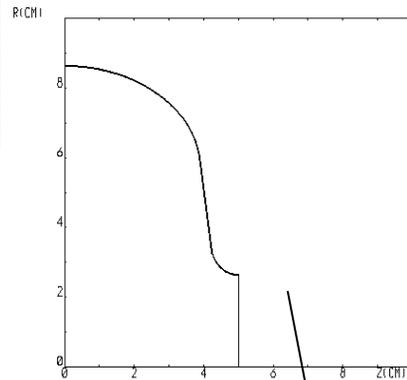


- The **cell length (L)** determines the cavity geometrical beta value.
- The **cell iris radius ( $R_{iris}$ )** is mainly determined by the cell-to-cell coupling requirements and cavity impedance limitations.
- The **iris ellipse ratio ( $r=b/a$ )** is primary determined by the local optimization of the peak electric field.
- The **cell radius (D)** is used for the frequency tuning without modifying any electromagnetic or mechanical cavity parameter.
- The **side wall inclination ( $\alpha$ )** and **B** and **A** can be use to minimize relative surface peak fields.
- **Usual design goal: Maximize  $R/Q * G$  / minimize peak magnetic surface field for given wall angle, maximum peak electric field and minimum iris radius**

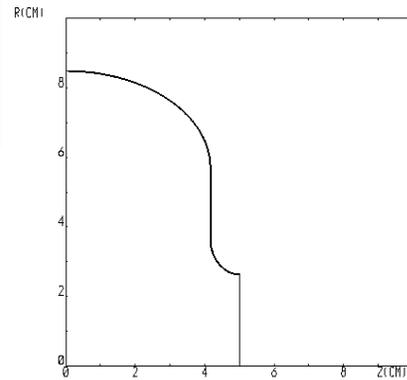


**$G^*R/Q$ , relative units:**

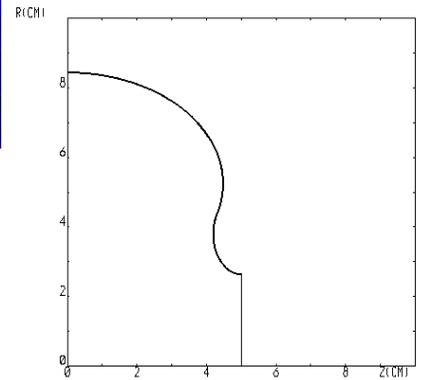
**0.90 (75deg)**



**1.00 (82deg)**



**1.02 (90deg)**

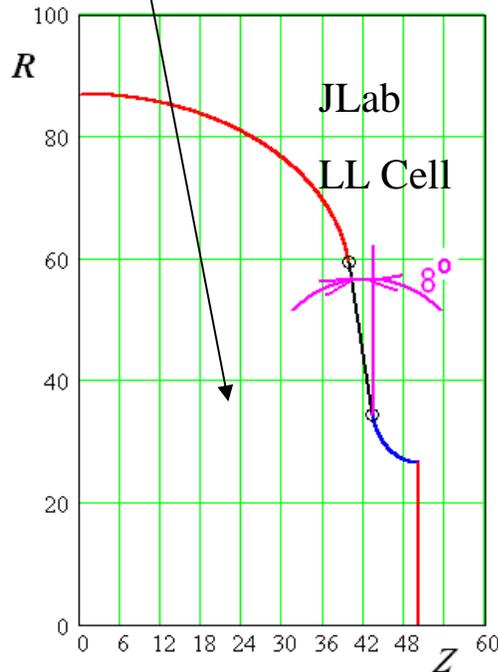


**1.042 (105 deg)**

**If one rejects the limitation of the angle we can further improve the value of  $G^*R/Q$**

JLab's optimized shape was designed under restriction that the angle of the wall slope is not less than 8 deg. This angle is useful to let liquid easily flow from the surface when chemical treatment or rinsing are performed.

This shape is also more mechanically strong.

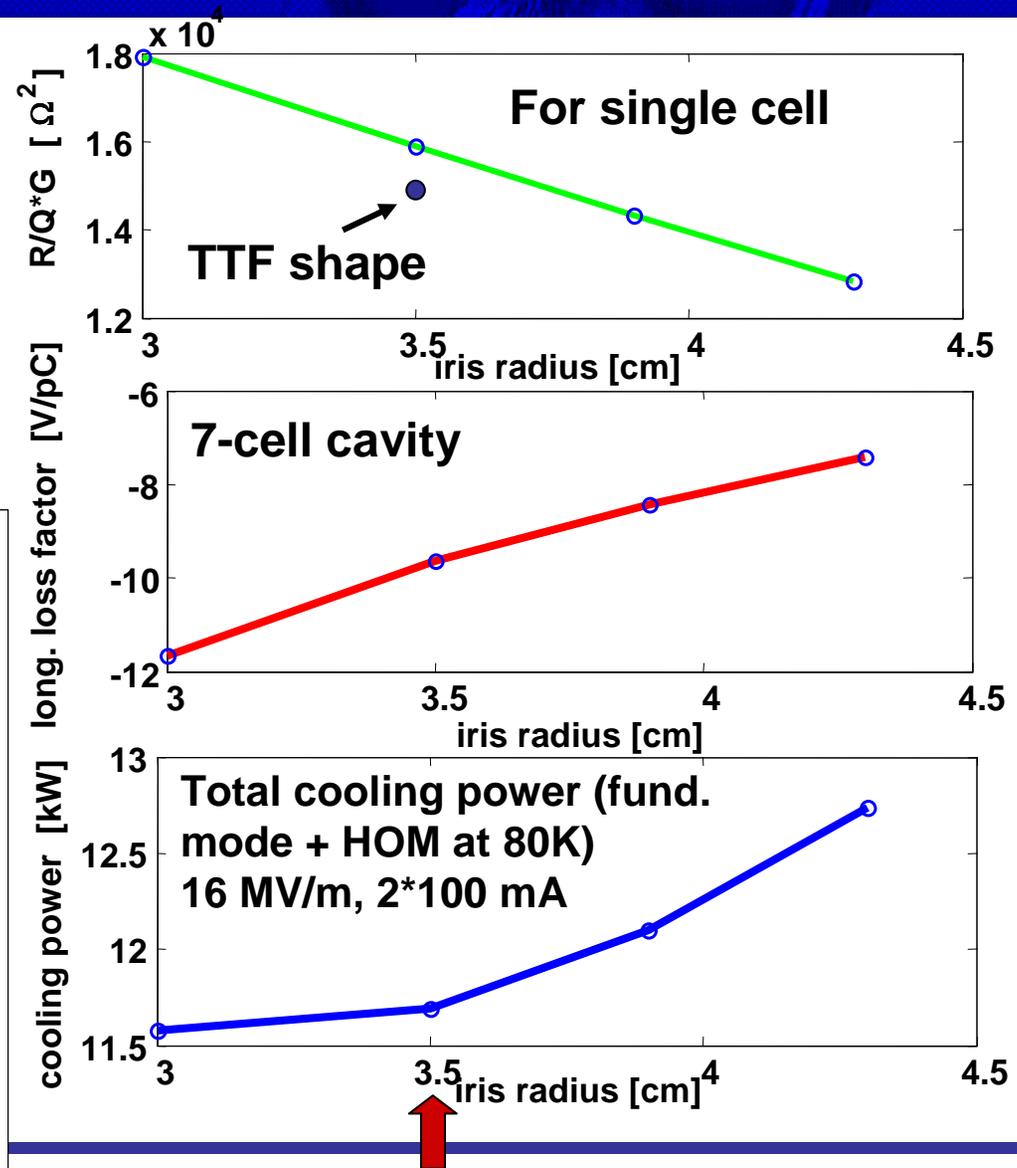
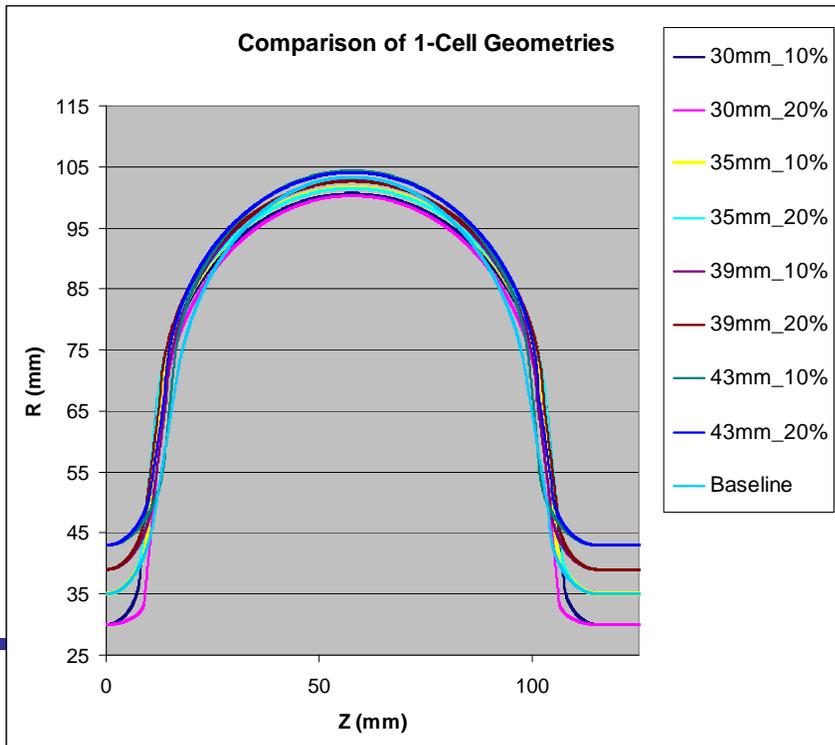




# Cavity Cell Shape and $R/Q \cdot G$ and Loss Factor

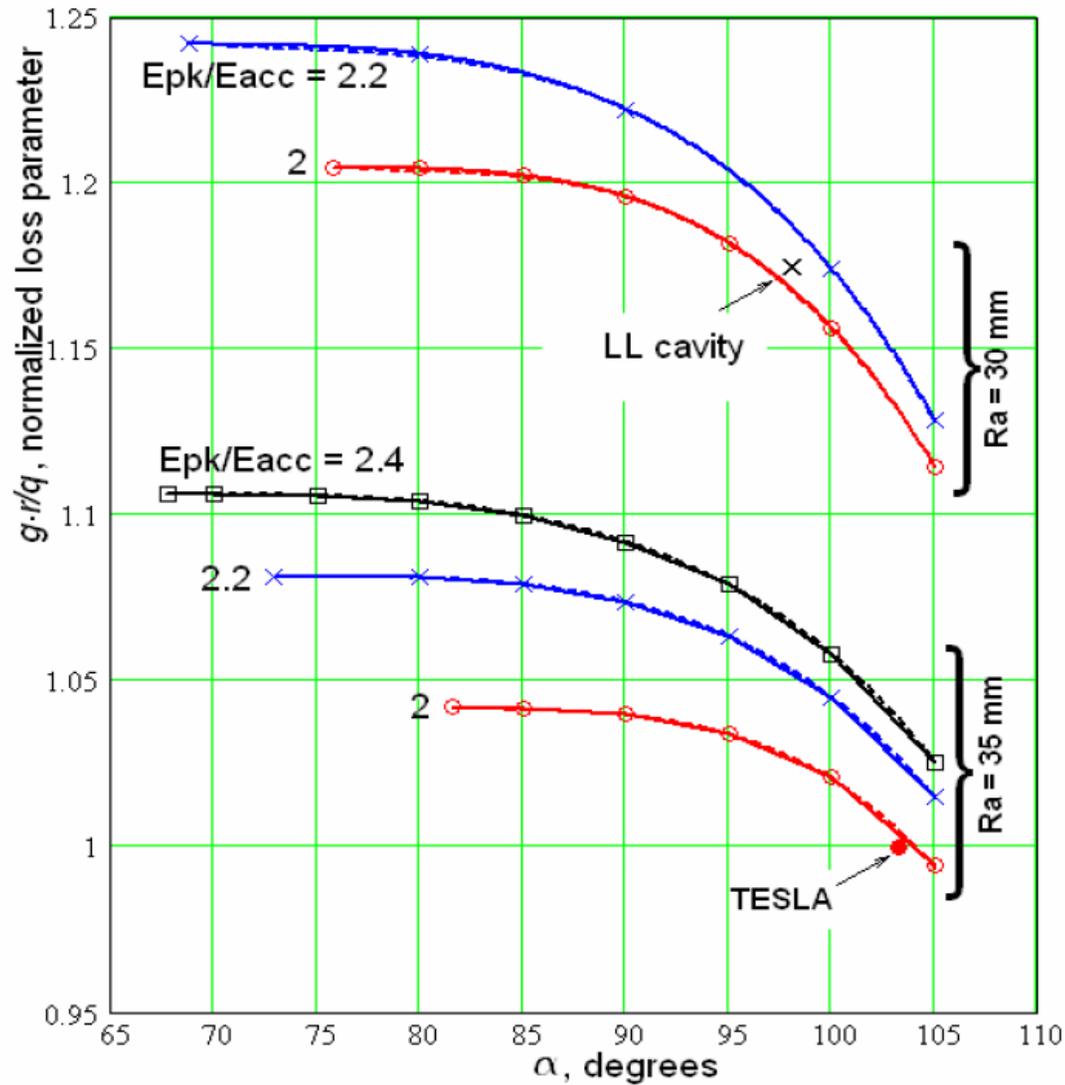
## 1.3 GHz center-cell:

- Cells optimized for fixed side wall angle (82 deg) and electric peak field ( $E/E_{acc} = 2.2$ )



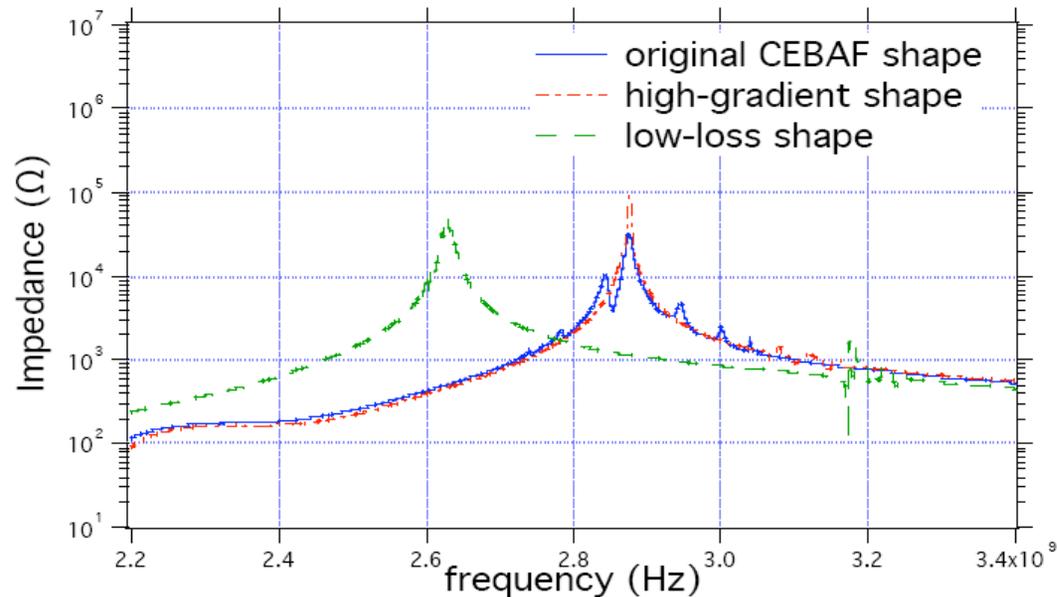


# Wall Angle, Peak Field and R/Q\*G





# Impact of Cell Shape on HOM Impedances (I)



TM<sub>011</sub> band, OC, HG, LL shapes, 7-cells, beam-pipe damping

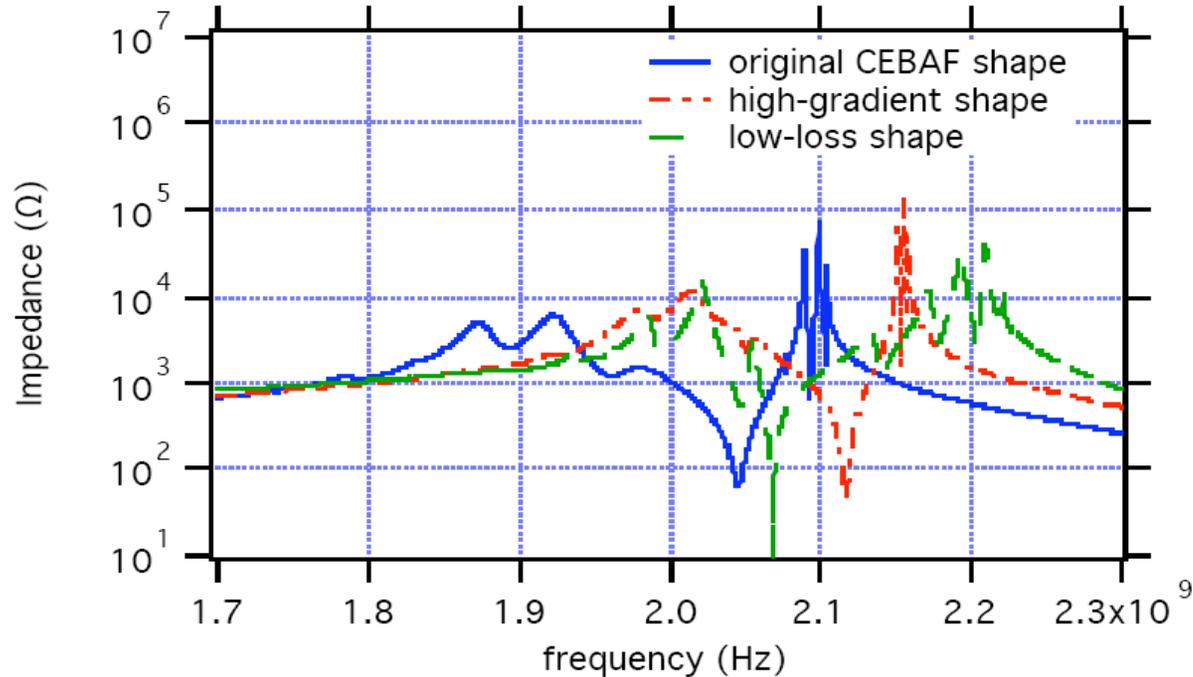
TM<sub>011</sub> mode data for multi-cell cavities.

	#cells	Freq, MHz	Q <sub>ext</sub>	R <sup>†</sup> ( )	R/Q ( )
OC	7	2876	527	31463	59.7
HG	7	2876	1348	90380	67.0
LL	7	2629	985	53556	54.4
OC*	5	2871	707	35453	50.1
DESY**	4	910	600		

\*waveguide damped. \*\*500 MHz cavity, meas.  $Q \cdot R^\dagger = V^2/2P$



# Impact of Cell Shape on HOM Impedances (II)



7-cells, OC, HG, LL shapes, TE<sub>111</sub>/TM<sub>110</sub> dipole, beam-pipe damping

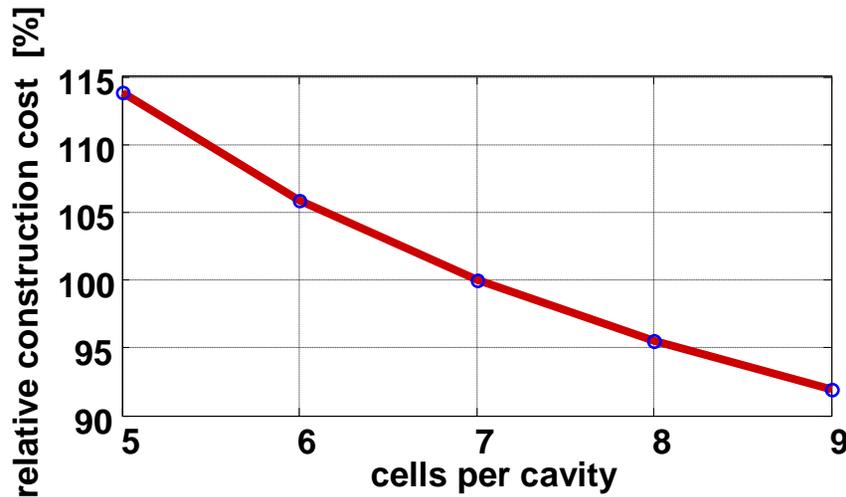
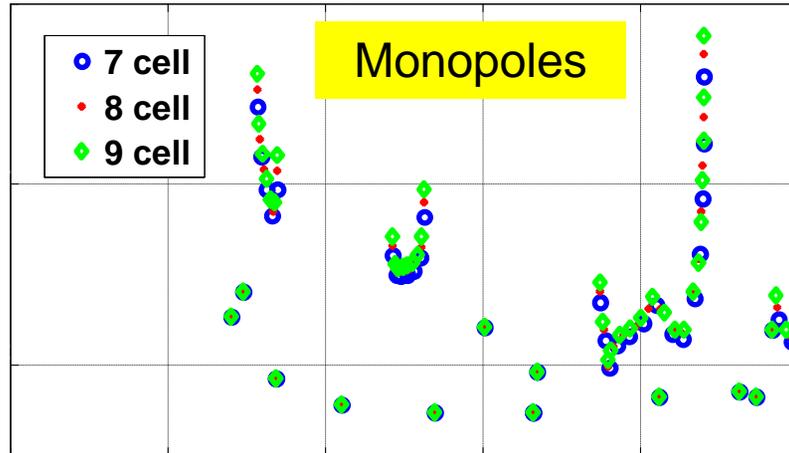
TE<sub>111</sub>/TM<sub>110</sub> mode data for multi-cell cavities.

	# cells	TE <sub>111</sub> f, MHz	TE <sub>111</sub> Q <sub>ext</sub>	TE <sub>111</sub> R <sup>†</sup> , ( )	TM <sub>110</sub> f, MHz	TM <sub>110</sub> Q <sub>ext</sub>	TM <sub>110</sub> R <sup>†</sup> , ( )
OC	7	1922	135	6088	2099	4177	72101
HG	7	2014	185	11359	2156	5694	146409
LL	7	2021	490	14107	2209	2071	39510
OC*	5	1894	956	22949	2103	3274	47064
DESY	4	650	4000		716	6000	

\*waveguide damped. †R calculated at 25mm offset in cavity.



# Design Example 3: Number of Cells per SC Cavity



$\sqrt{|\Delta S_{21}|} \sim |E(z)|$  F. Marhauser et al. PAC 1999

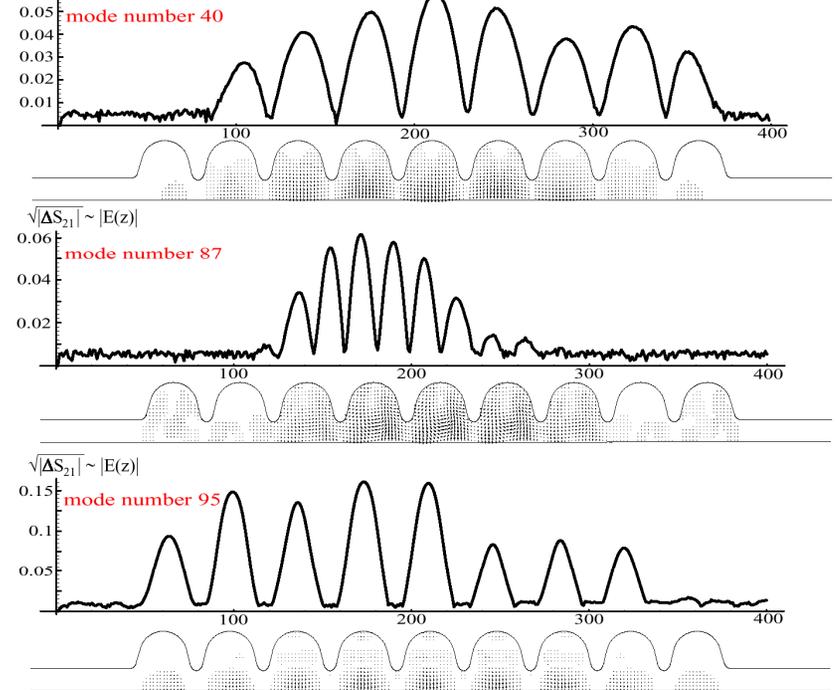


Figure 5: Trapped dipole mode (comp. Figure 4) no. 40 ( $f = 3.084$  GHz MAFIA; 3.078 GHz meas.), mode no. 87 ( $f = 4.323$  GHz MAFIA; 4.314 GHz meas.) and mode no. 95 ( $f = 4.426$  GHz MAFIA; 4.421 GHz meas.).

- **Risk of trapped modes increases with number of cells**

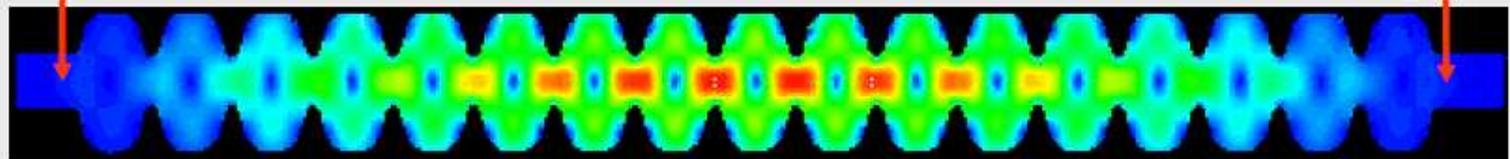


# Trapped Modes

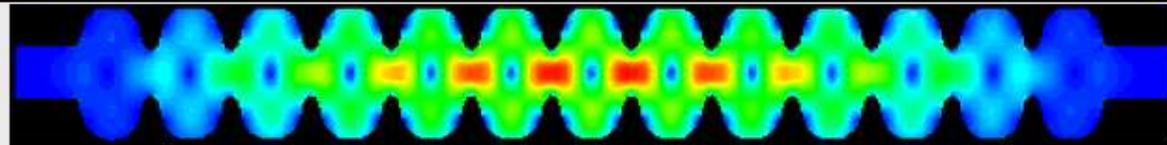
Example: how  $N$  influences strength of the E-H fields at HOM couplers locations

no E-H fields at HOM couplers locations (trapping),  
which are always placed at the end beam tubes

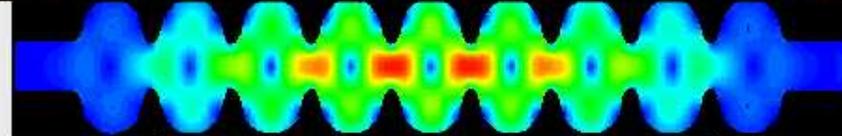
$N = 17$



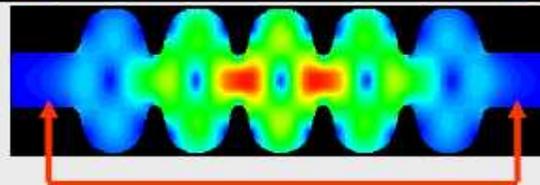
$N = 13$



$N = 9$



$N = 5$



E-H fields at HOM couplers locations

Less cells in a structure helps always to reach low  $Q$ s of HOMs.



# HOM strength (number of Cells)

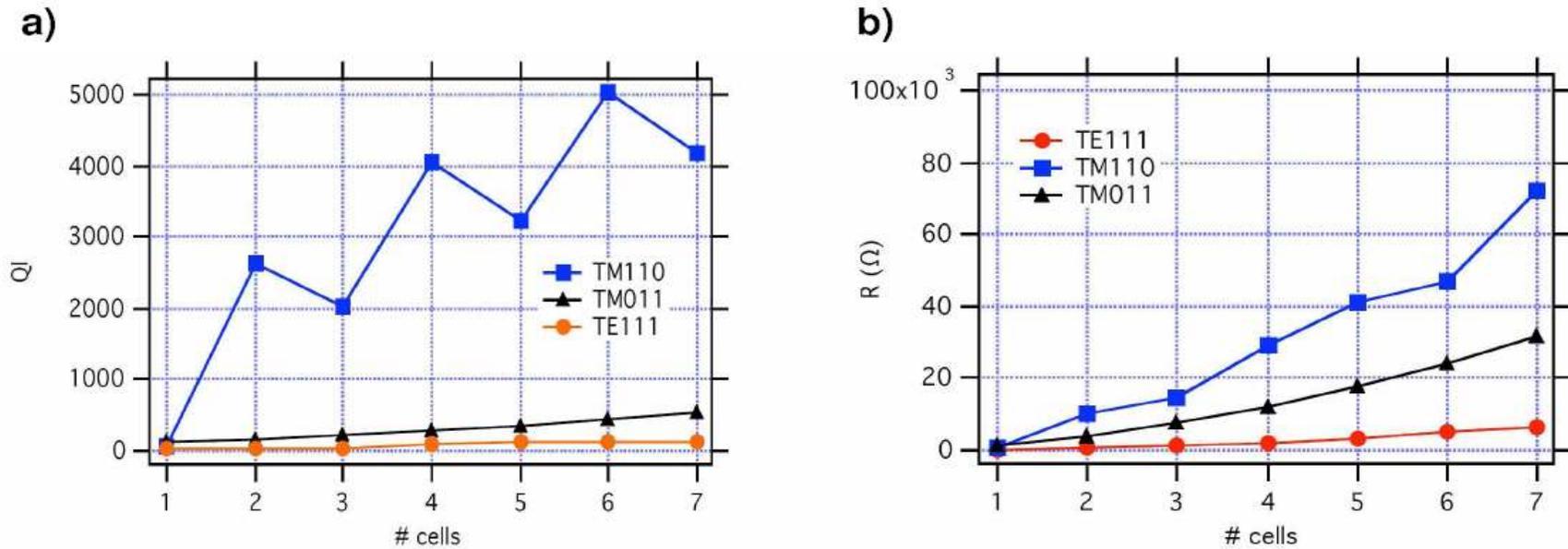
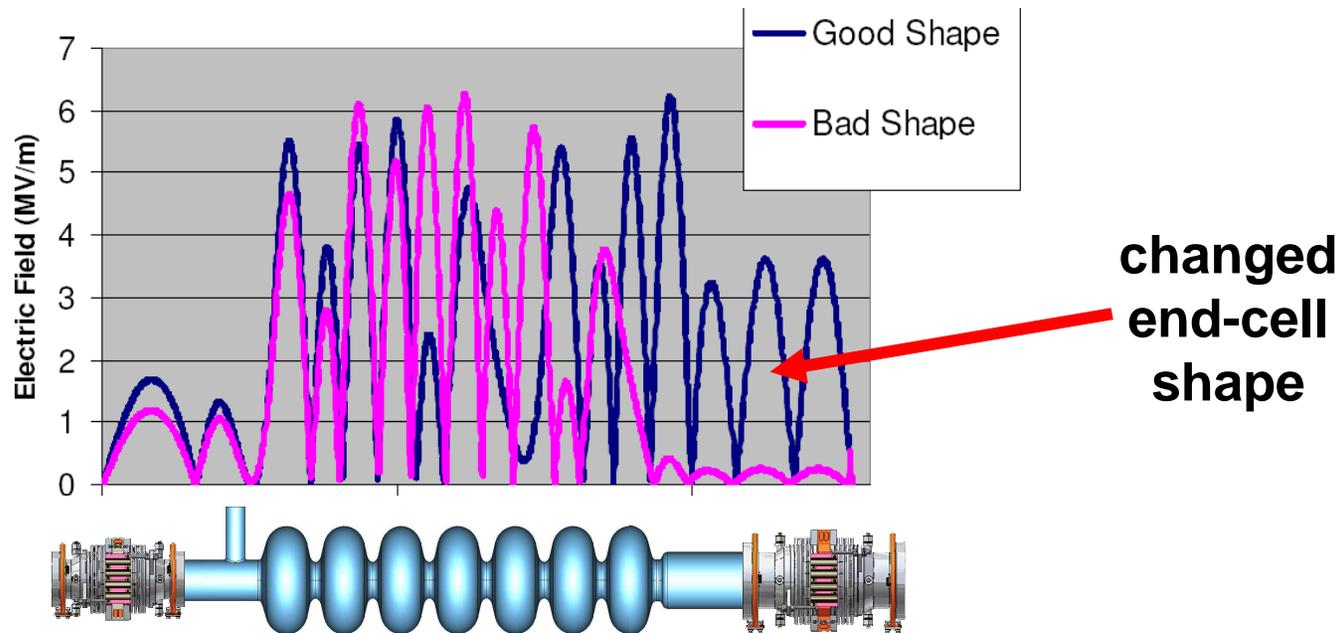


Fig. 11. Impact of number of cavity cells on HOM impedance (TM011, TE111 and TM110 passband modes with beam pipe damping). a) Loaded Q vs. number of cells. b) Impedance vs. number of cells (dipoles at 25 mm transverse offset). Courtesy of B. Rimmer.



## Design Example 4: 7-Cell SRF Cavity End-Cell Design

- End cell shape has significant impact (example HOM):



- Can fine-tuning of end cell to
  - Increase damping of most dangerous HOM(s)
  - Avoid strong monopole modes at beam harmonics
  - Note: Can optimize end cell shape only for a few selected modes!!



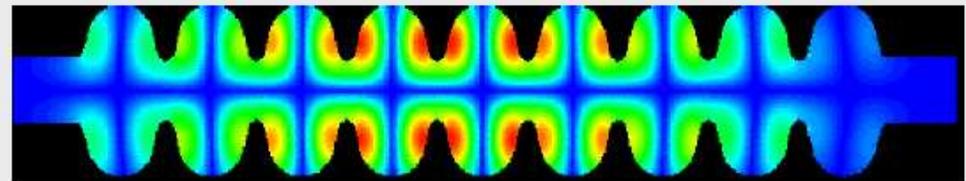
# End Cell Optimization: ILC Cavity

2. Tailor end-cells to equalize HOM frequencies of inner- and end-cells.

Example: TESLA 9-cell cavity, which has two different end-cells (asymmetric cavity)

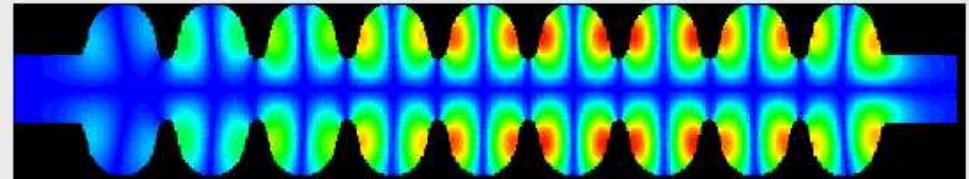
The lowest mode in the passband

$$f_{HOM} = 2382 \text{ MHz}$$



The highest mode in the passband

$$f_{HOM} = 2458 \text{ MHz}$$

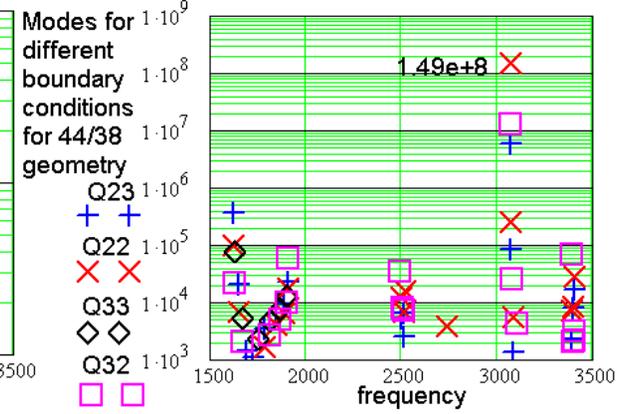
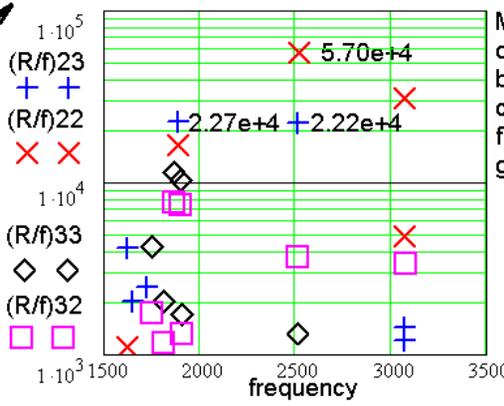
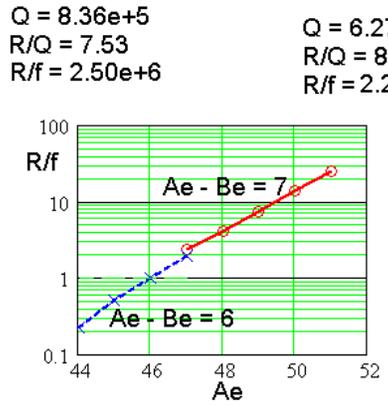
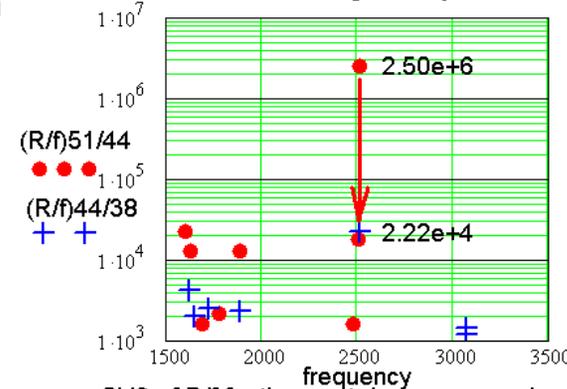
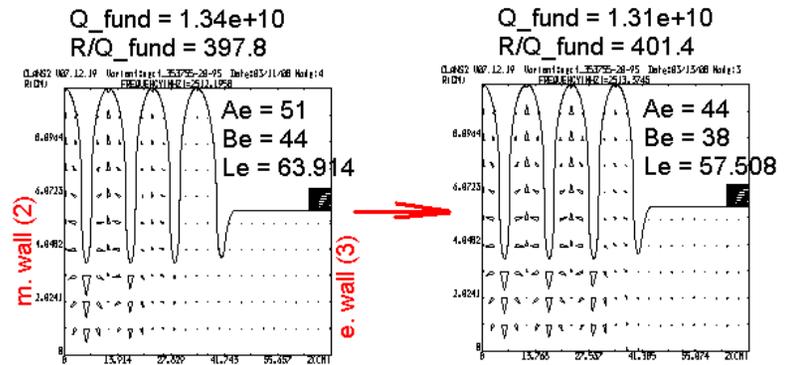
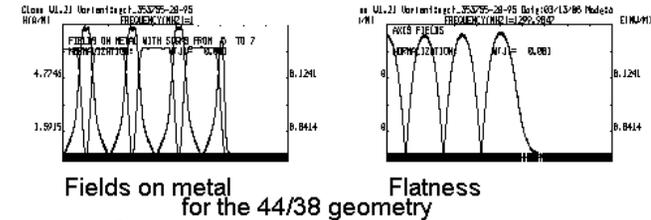
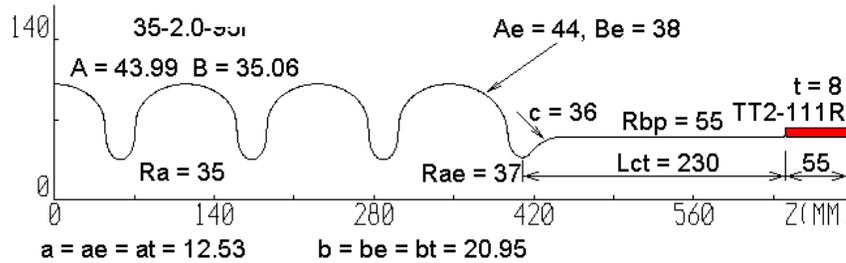


The method works for very few modes but keeps the (R/Q) value high of the fundamental mode.



# 7-Cell SRF Cavity End-Cell Design

II. Cavity with  $Epk/Eacc = 2.0$ . Suppression of the worst Dipole (2513 MHz).





# Cavity Examples: SRF High beta Cavities

The “heart” of all mentioned facilities are sc standing wave (usually multi-cell) accelerating structures.

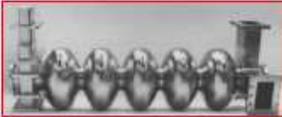
FERMI 3.9 GHz



S-DALINAC 3 GHz



CESR/CEBAF 1.5 GHz



HEPL 1.3 GHz



TESLA/ILC 1.3 GHz



SNS  $\beta=0.61, 0.81, 0.805$  GHz



HERA 0.5 GHz



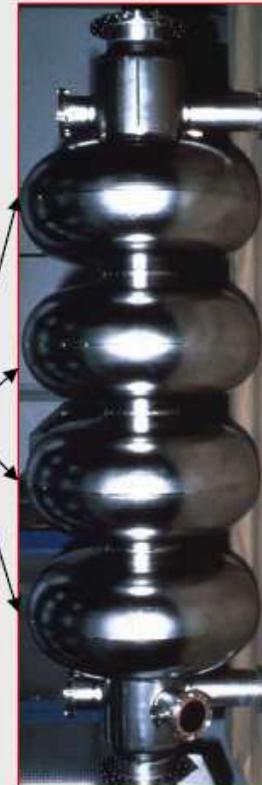
KEK-B 0.5 GHz



CESR 0.5 GHz



LEP 0.352 GHz



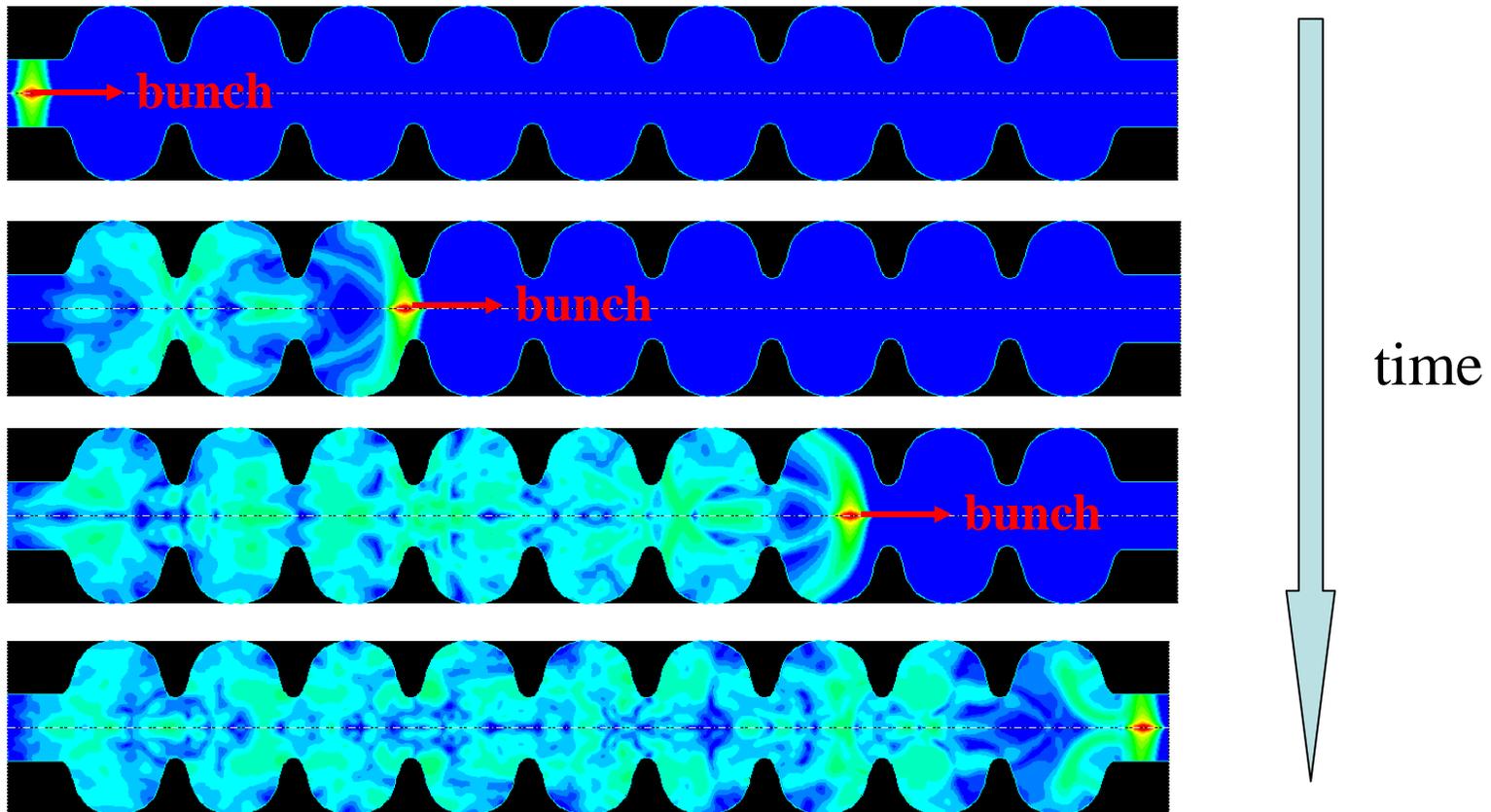
cells



- **Higher order modes**
  - Introduction: HOMs
  - HOM excitation by a beam
  - HOM damping schemes
  - HOM damping examples and results



# HOM Excitation by a Bunch

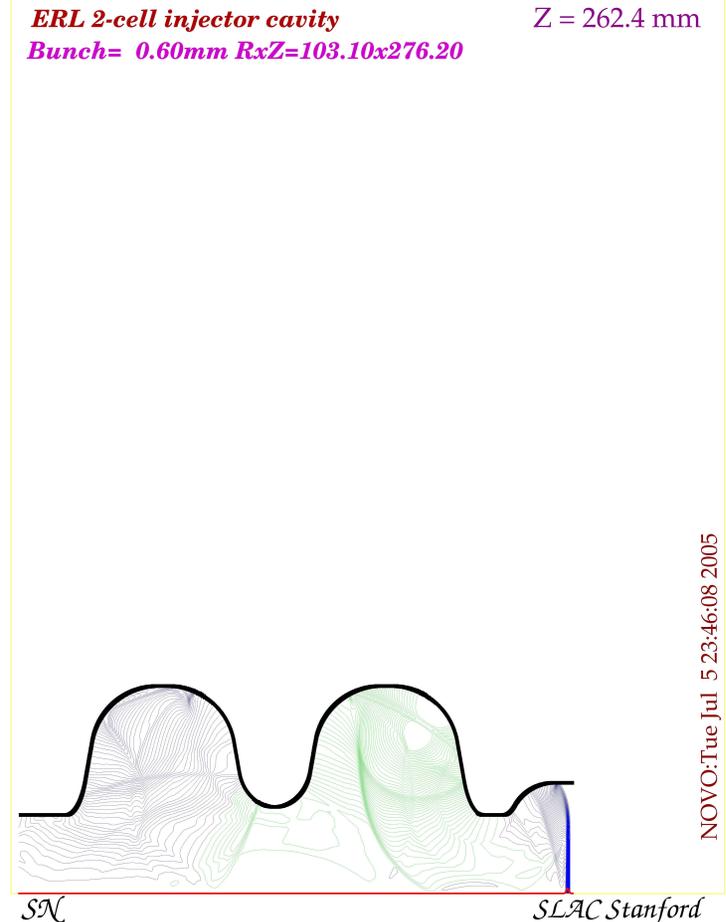


**The bunched beam excites higher-order-modes (HOMs)  
= wakefields = electromagnetic fields in the cavity.**



# Beam-Cavity Interaction

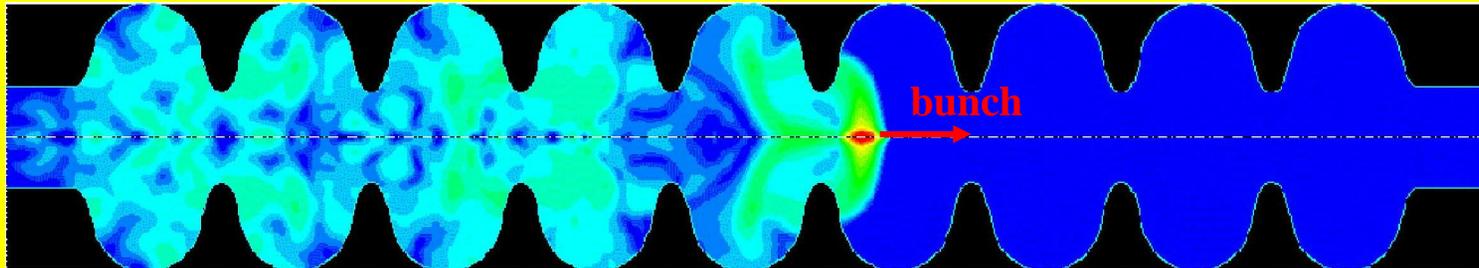
- **Bunch traverses a cavity**
- $\Rightarrow$  **deposits electromagnetic energy, which is described as wakefields (time domain) or higher-order modes (HOMs, frequency domain)**
- **Subsequent bunches are affected by these fields and at high beam current one must consider instabilities**





## Single Bunch Monopole Losses: Wake Potential of a Point-Charge

The beam excites higher-order-modes (HOMs) in a cavity:

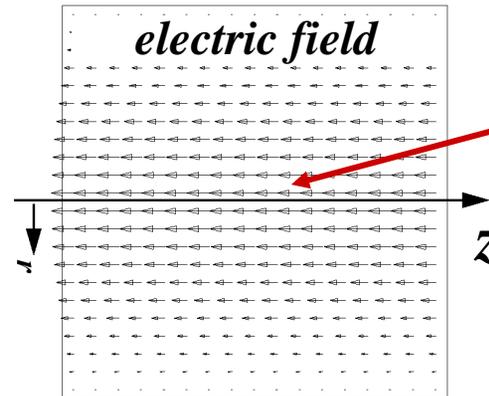


- When a charge passes through a cavity, it excites HOMs.
- If it passes exactly an axis, it will only excite **monopole modes**.
- For a point charge, the HOM excitation depends only on the bunch charge and the cavity shape.
- The excited field can be described by the **wake potential**.



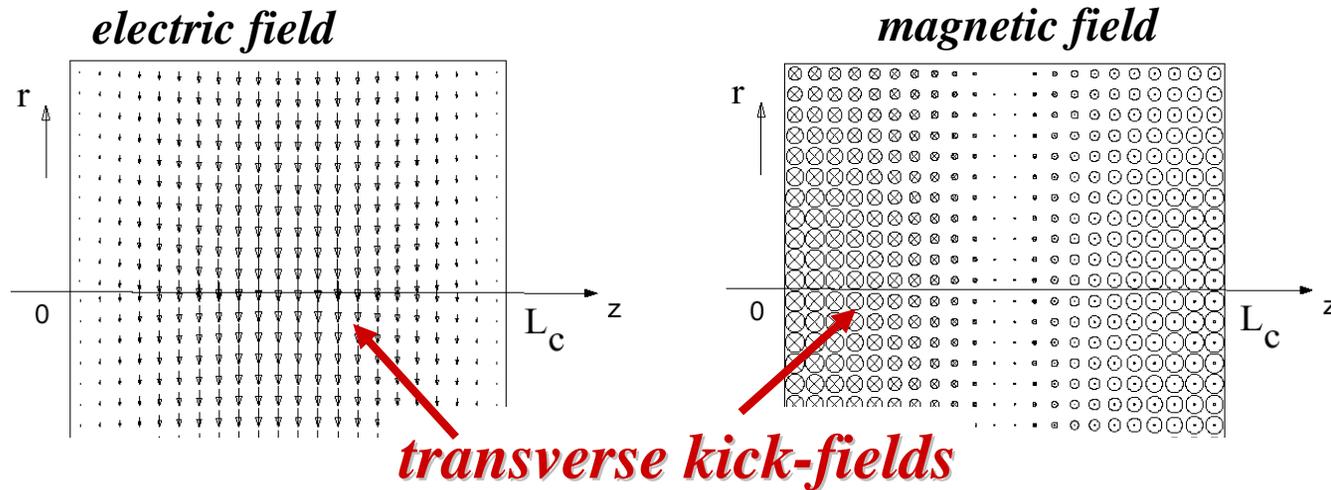
# Higher-Order-Modes (HOMs)

## Monopole modes



*longitudinal electric field on axis*

## Dipole modes, quadrupole modes,...



*transverse kick-fields*



# Monopole, Dipole and Quadrupole Modes...

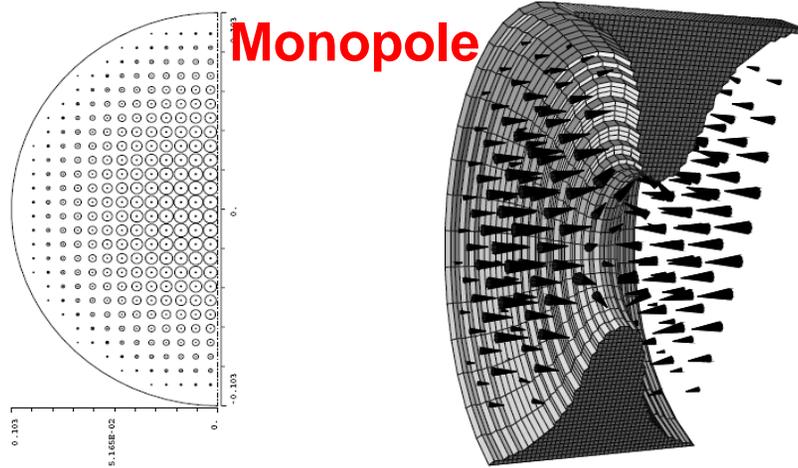


Figure 5: One mid-cell of a TESLA cavity. The electric field of the 1.3 GHz accelerating  $\pi$ -mode is shown. The left graph shows the electric field in a plane perpendicular to the cavity axis.

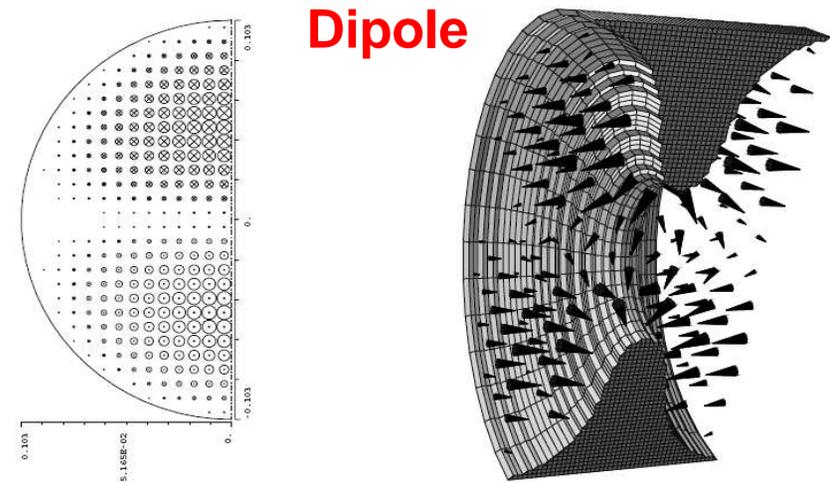


Figure 6: One mid-cell of a TESLA cavity. The electric field of the 1.79 GHz  $\pi$ -mode of the first dipole passband is shown. The left graph shows the electric field in a plane perpendicular to the cavity axis.

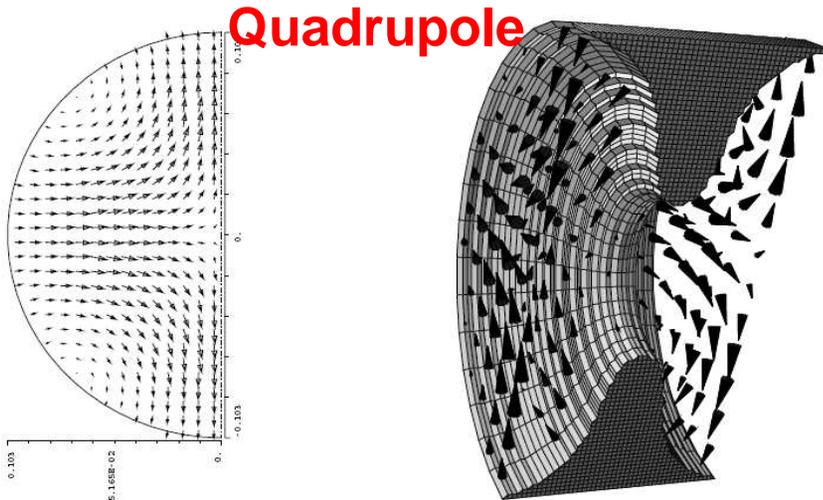


Figure 7: One mid-cell of a TESLA cavity. The electric field of the 2.32 GHz  $\pi$ -mode of the first quadrupole passband is shown. The left graph shows the electric field in a plane perpendicular to the cavity axis.

$$\vec{E}(r, \phi, z) = \sum_m \left( \begin{array}{l} \widetilde{E}_r^{(m)}(r, z) \cos(m\phi) \mathbf{e}_r \\ + \widetilde{E}_\phi^{(m)}(r, z) \sin(m\phi) \mathbf{e}_\phi \\ + \widetilde{E}_z^{(m)}(r, z) \cos(m\phi) \mathbf{e}_z \end{array} \right)$$

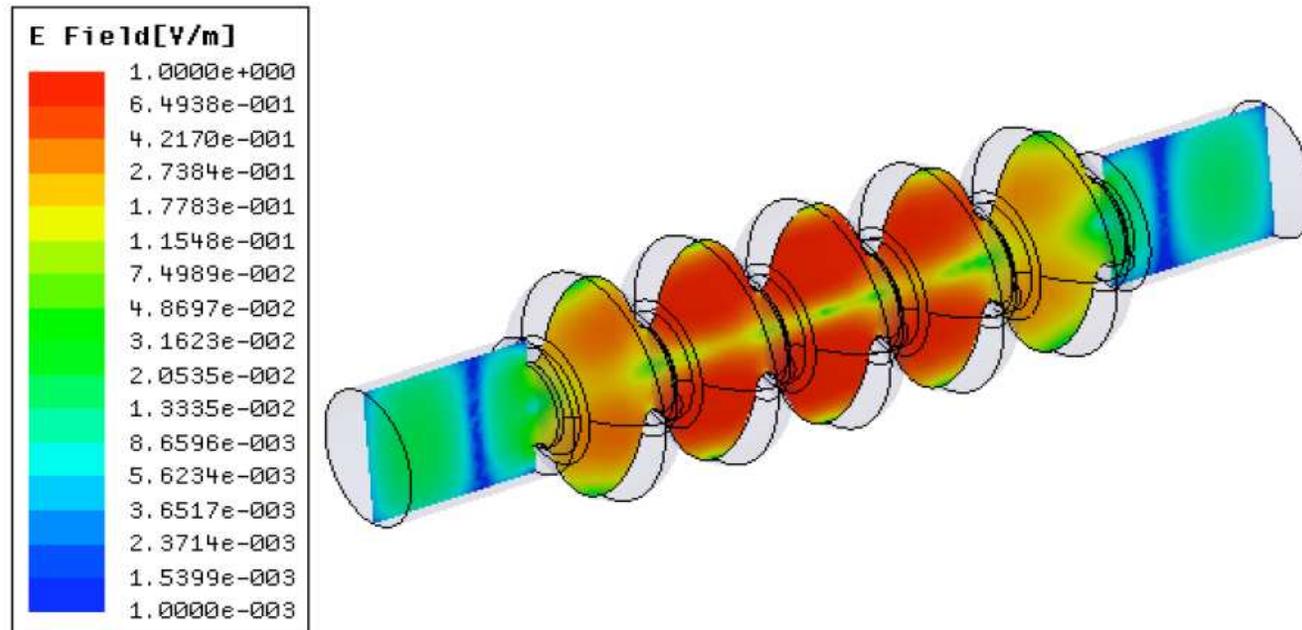
$$\vec{B}(r, \phi, z) = \sum_m \left( \begin{array}{l} \widetilde{B}_r^{(m)}(r, z) \sin(m\phi) \mathbf{e}_r \\ + \widetilde{B}_\phi^{(m)}(r, z) \cos(m\phi) \mathbf{e}_\phi \\ + \widetilde{B}_z^{(m)}(r, z) \sin(m\phi) \mathbf{e}_z \end{array} \right).$$

from R. Wanzenberg



# Methods of HOM Calculations: Frequency Domain

**Complex eigenvalue solution** (becoming available, SLAC codes, ANSYS beta, HFSS) gives real and imaginary parts of impedance directly, hence R and Q.

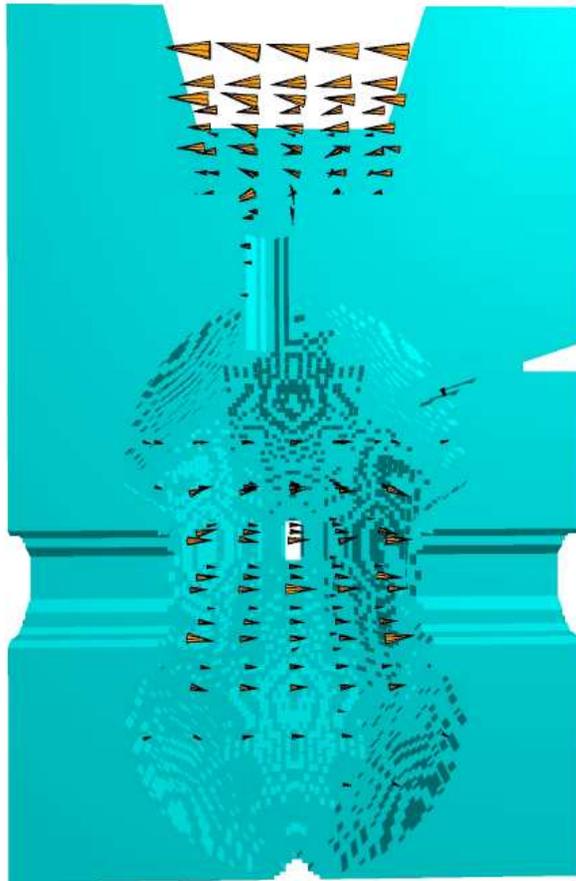


HFSS 3D complex Eigenvalue solution, 5-cell cavity with enlarged beam-pipes.

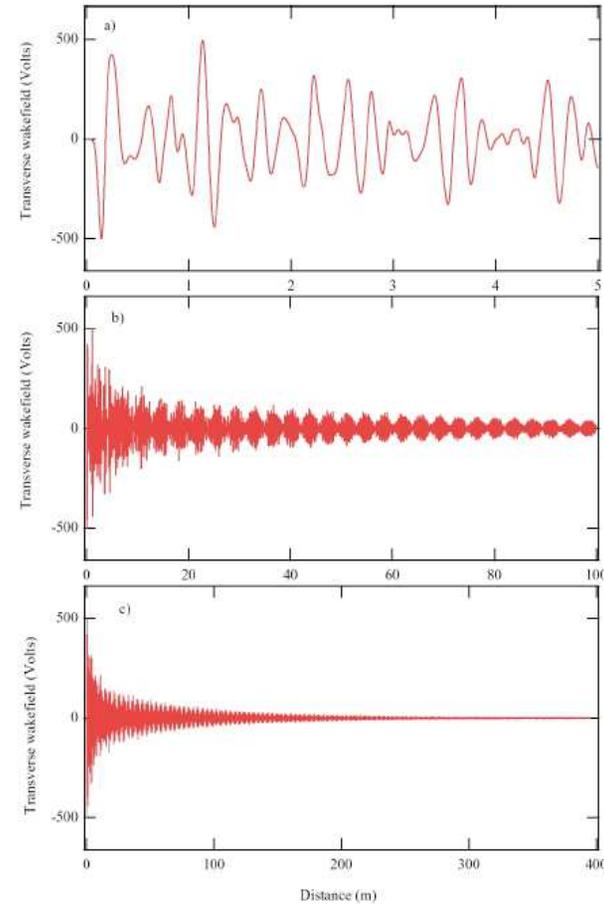


# Time-Domain Method (I)

Time domain (FFT) method (developed at SLAC, widely used, ABCI, MAFIA etc.)



3D MAFIA model of PEP-II cavity.

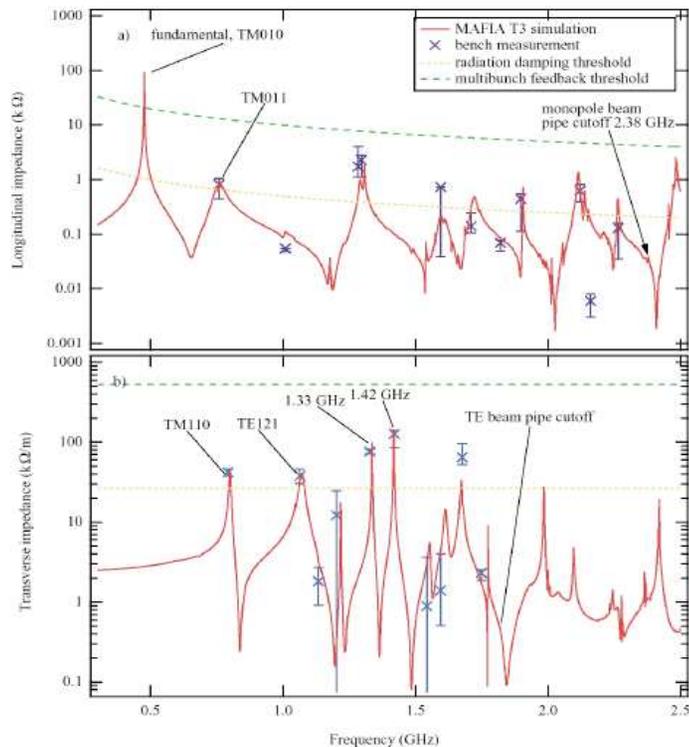


Short-, medium- and long-range wakes\*.

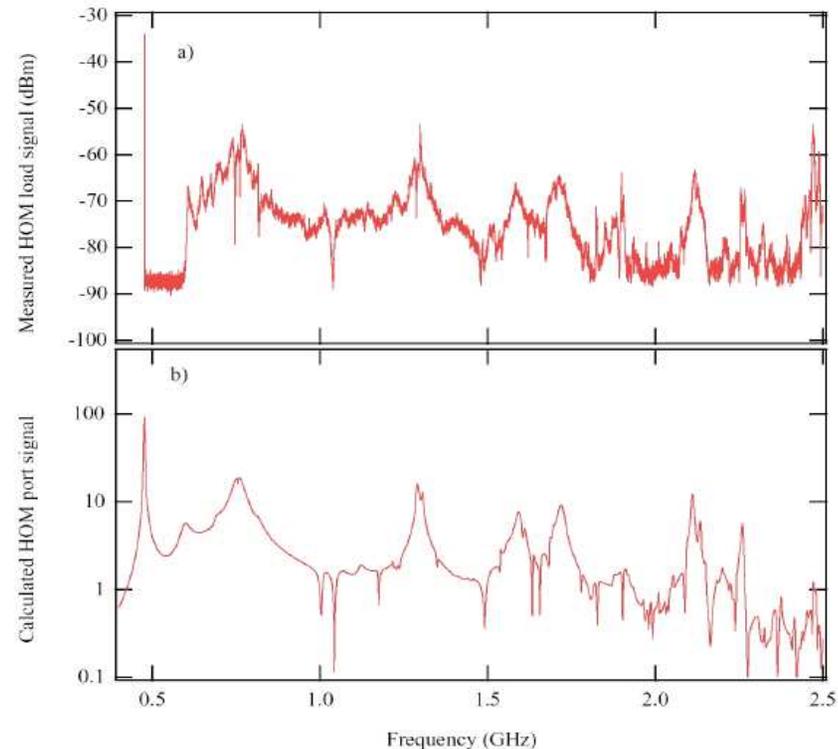
\*(2000) Physical Review Special Topics - Accelerators and Beams, Volume 3, 102001



# Time-Domain Method (II)



Calculation vs bead-pull measurements.



Measured vs calculated HOM spectrum.

Method uses open boundaries on ports. FFT of long-range wake gives broad-band impedance spectrum in one run. Works best for strong coupling ( $\beta \gg 1$ ). Frequency resolution set by wake length, max frequency set by mesh size (typ.  $\sim 10$  GHz).

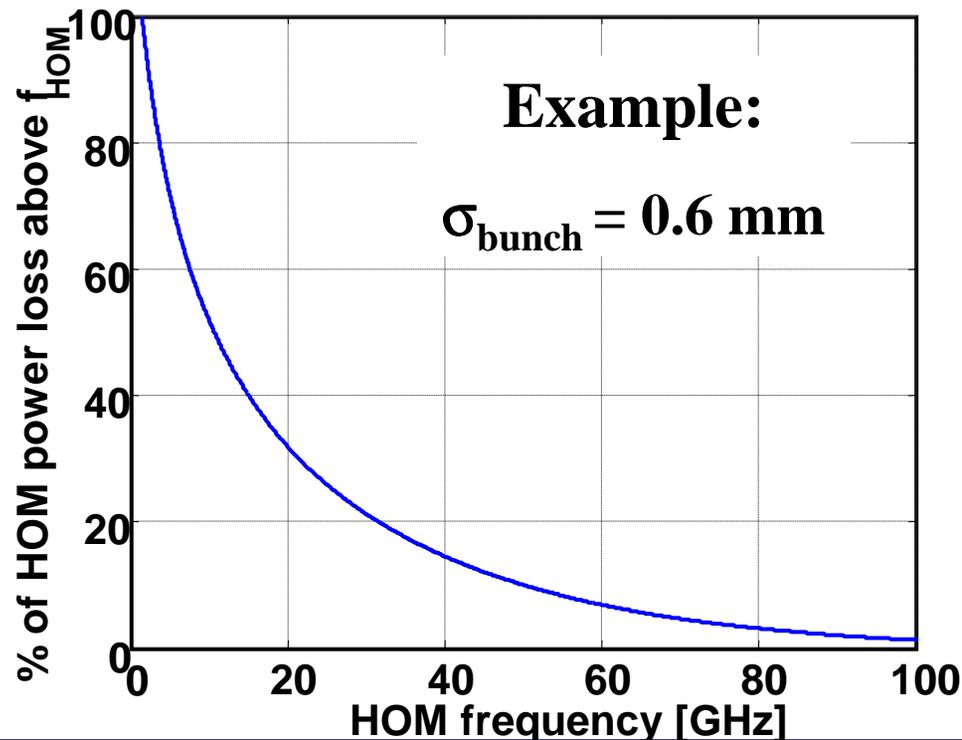


- **Higher order modes**
  - Introduction: HOMs
  - **HOM excitation by a beam**
  - HOM damping schemes
  - HOM damping examples and results



*The excited HOM power of a single bunch depends on:*

- the HOMs of the cavity (i.e. their shunt impedance),
- the bunch charge ( $P_{\text{HOM}} \propto q_b^2$ ),
- the bunch length (i.e. the spectrum of a bunch).

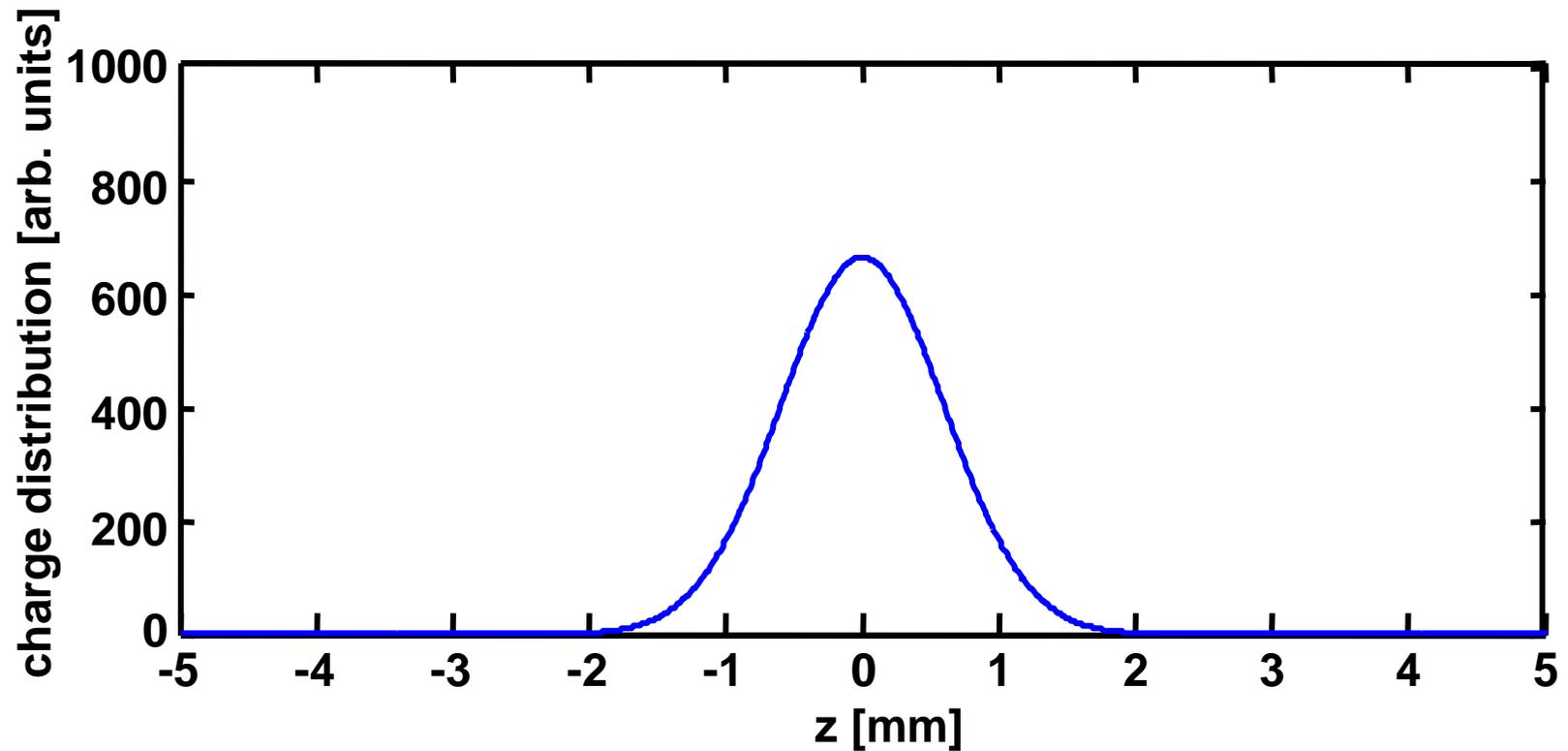


**⇒ Short bunches excite very high frequency modes!**



# Single Bunch Monopole Losses: The Bunch

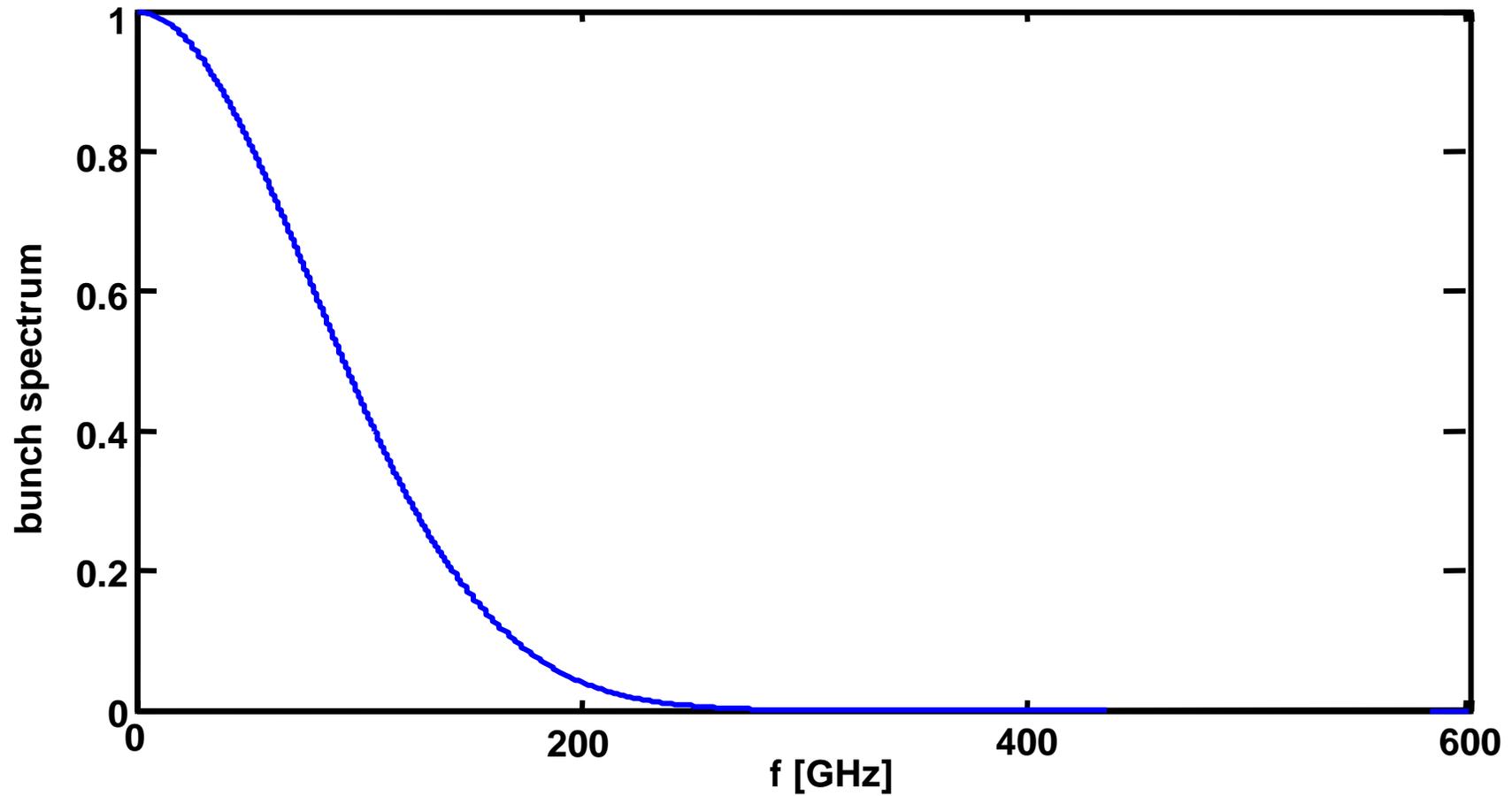
Longitudinal charge distribution for a 600  $\mu\text{m}$  bunch:





# Single Bunch Monopole Losses: The Bunch Spectrum

*Spectrum of a 600  $\mu\text{m}$  bunch:*





# Beam-cavity interaction: Wave Function

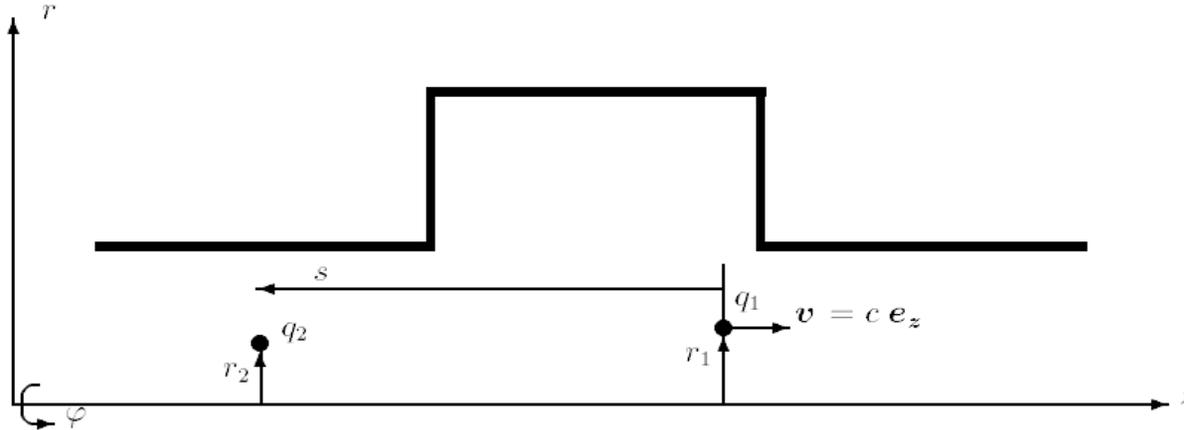
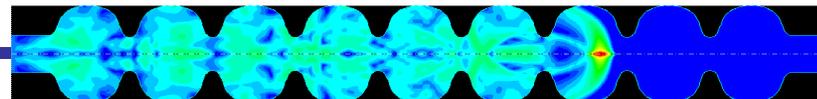


Figure 8: A point charge  $q_1$  traversing a cavity with an offset  $r_1$  followed by a test charge  $q_2$  with offset  $r_2$ .

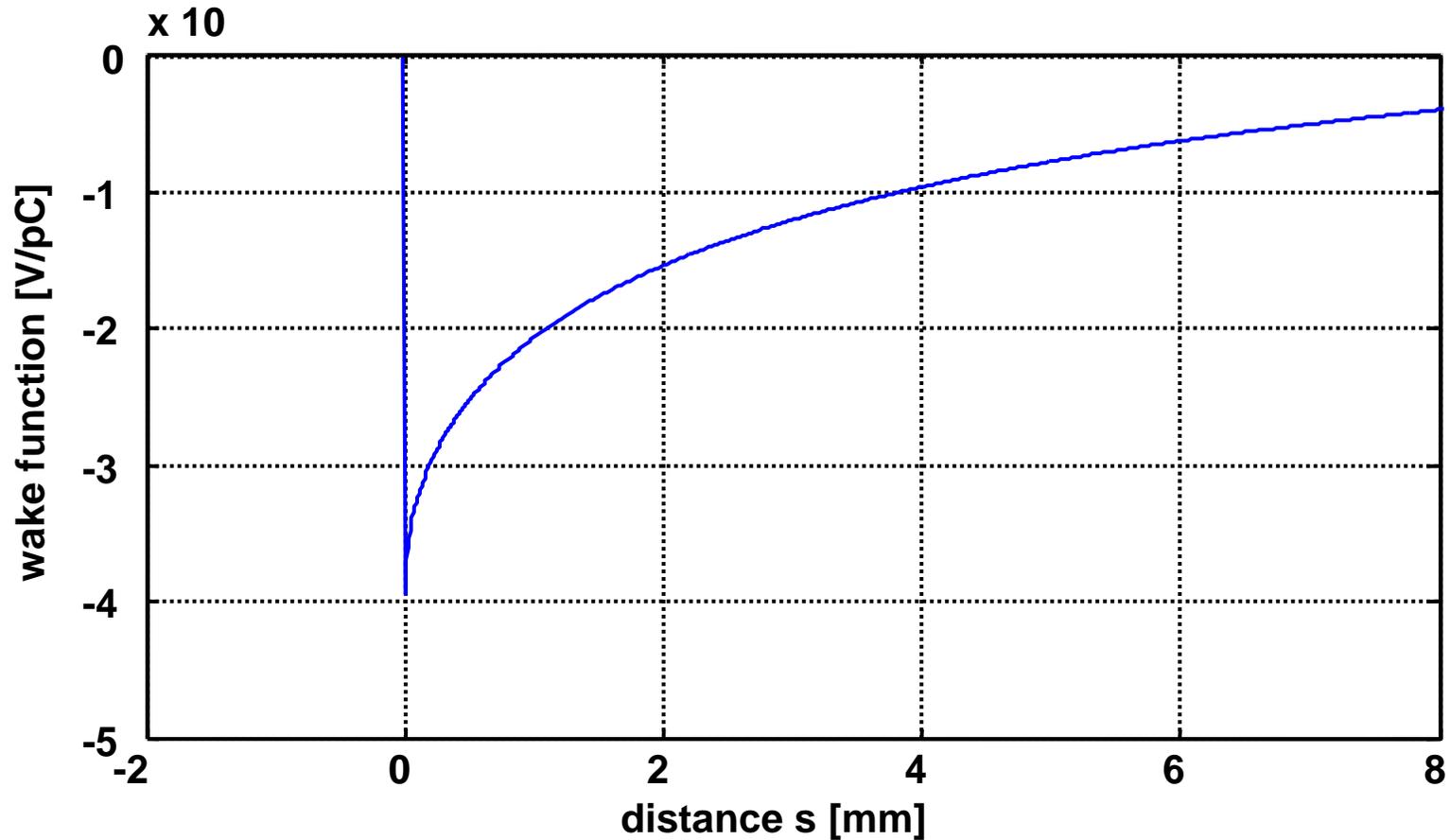
**Lorentz-Forces on test charge:** 
$$\mathbf{F} = \frac{d\mathbf{p}}{dt} = q_2 (\mathbf{E} + c \mathbf{e}_z \times \mathbf{B}).$$

**The integrated field seen by a test particle traveling on the same path at a constant distance  $s$  behind a point charge  $q$  is the longitudinal wake (Green) function  $w(s)$ .**





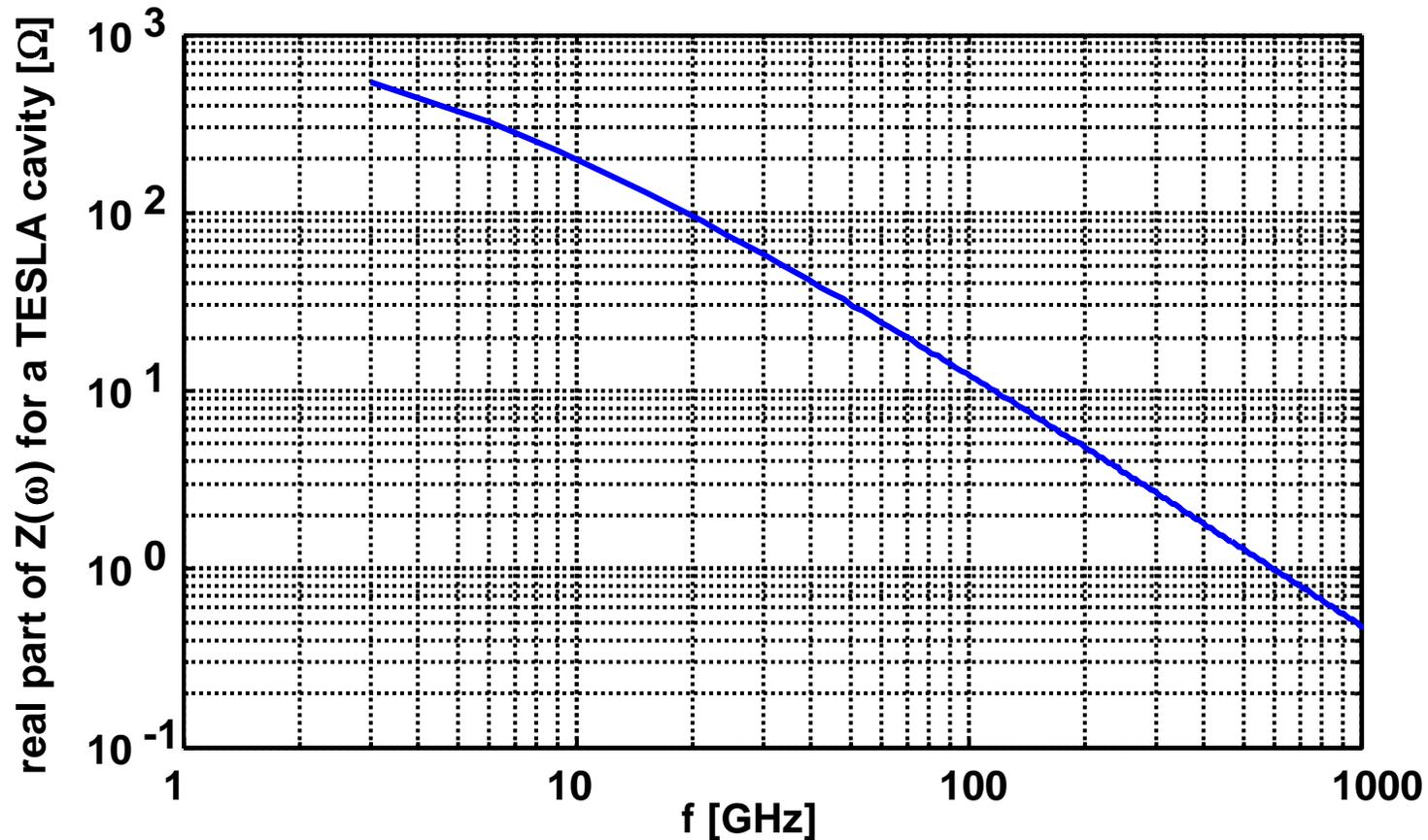
# Single Bunch Monopole Losses: Wake Function of a Point Charge after a TESLA Cavity





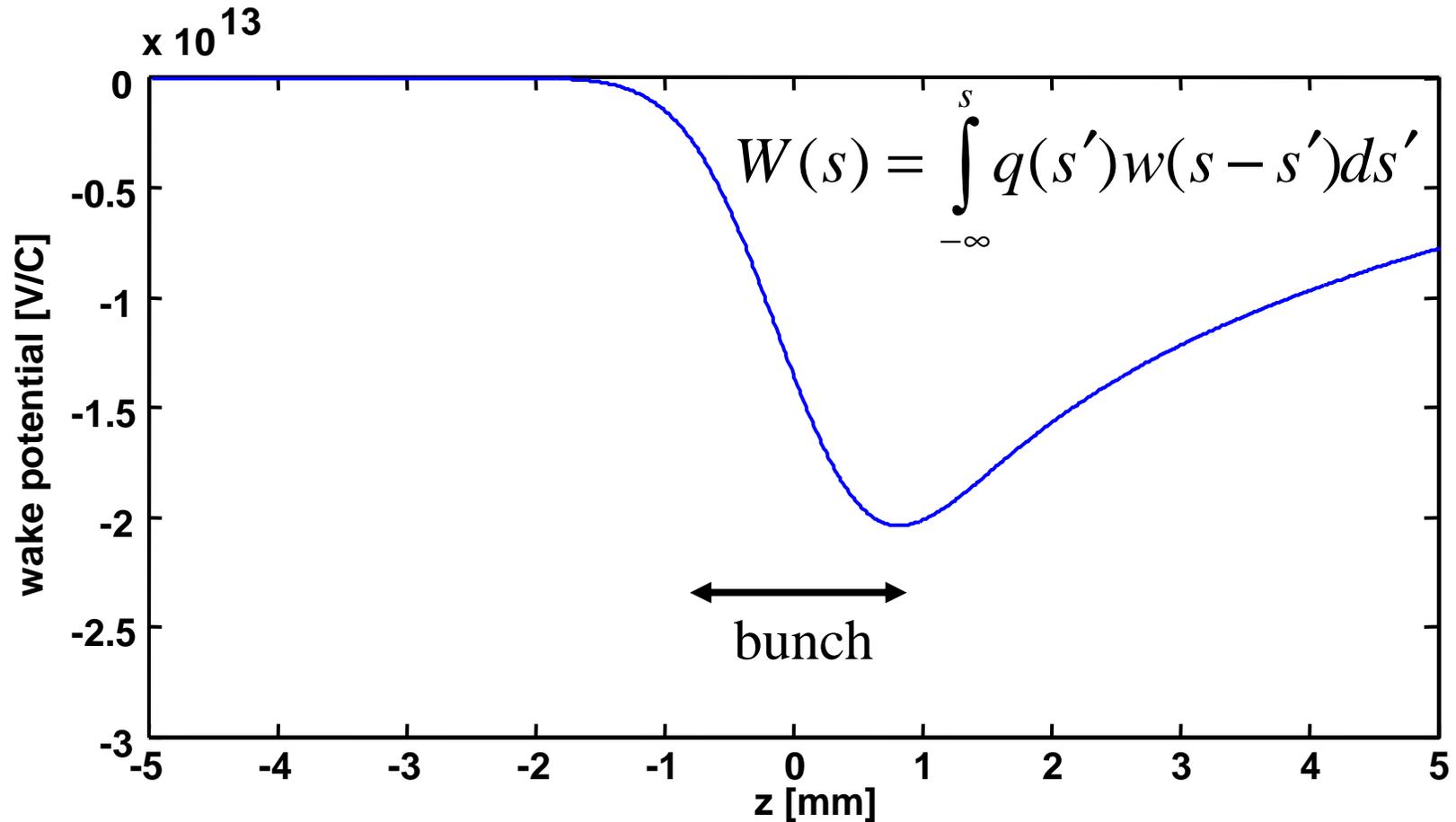
# Single Bunch Monopole Losses: Wake Potential of a Point Charge after a TESLA Cavity

*The fft of the wake function gives the cavity impedance  $Z(\omega)$ :*





# Single Bunch Monopole Losses: Wake Potential of a Bunch after a TESLA Cavity



The wake potential  $W$  is a convolution of the linear bunch charge density distribution  $q(s)$  and the wake function  $w$



## Single Bunch Monopole Losses: Loss Factor

Once the longitudinal wake potential is known, the **longitudinal loss factor**, which tells us how much electromagnetic energy a bunch leaves behind in a structure can be defined as:

$$k = \frac{\Delta U}{q^2} \quad k_{\parallel} = \int_{-\infty}^{\infty} q(s)W(s)ds$$

**Average power loss:**

$$P_{\parallel} = k_{\parallel} Q_{bunch} I_{beam}$$

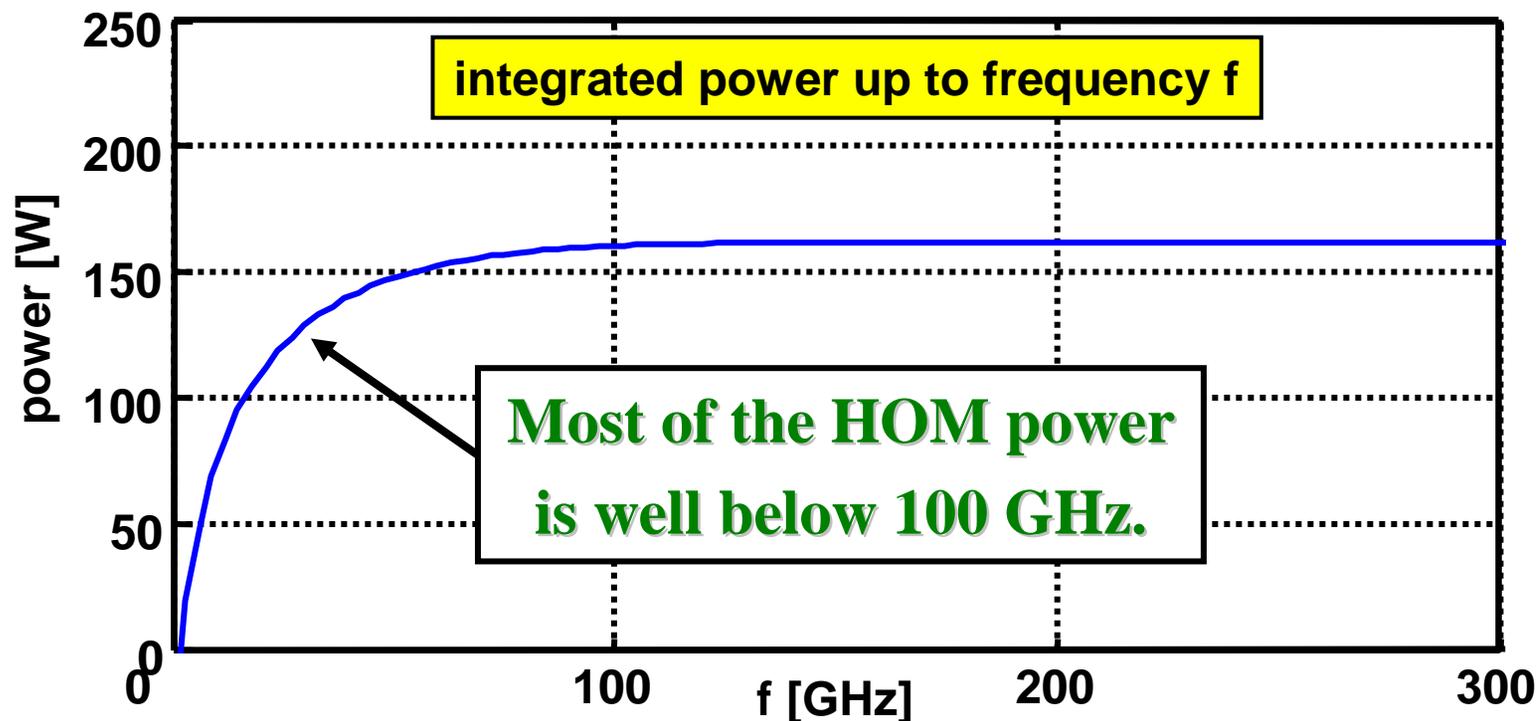
- **This is the total energy lost by a bunch divided by the time separation of two consecutive bunches.**
- **This does not include any interaction between bunches (i.e. resonant mode excitation)!!!**



# Single Bunch Monopole Losses: HOM Power Frequency Distribution

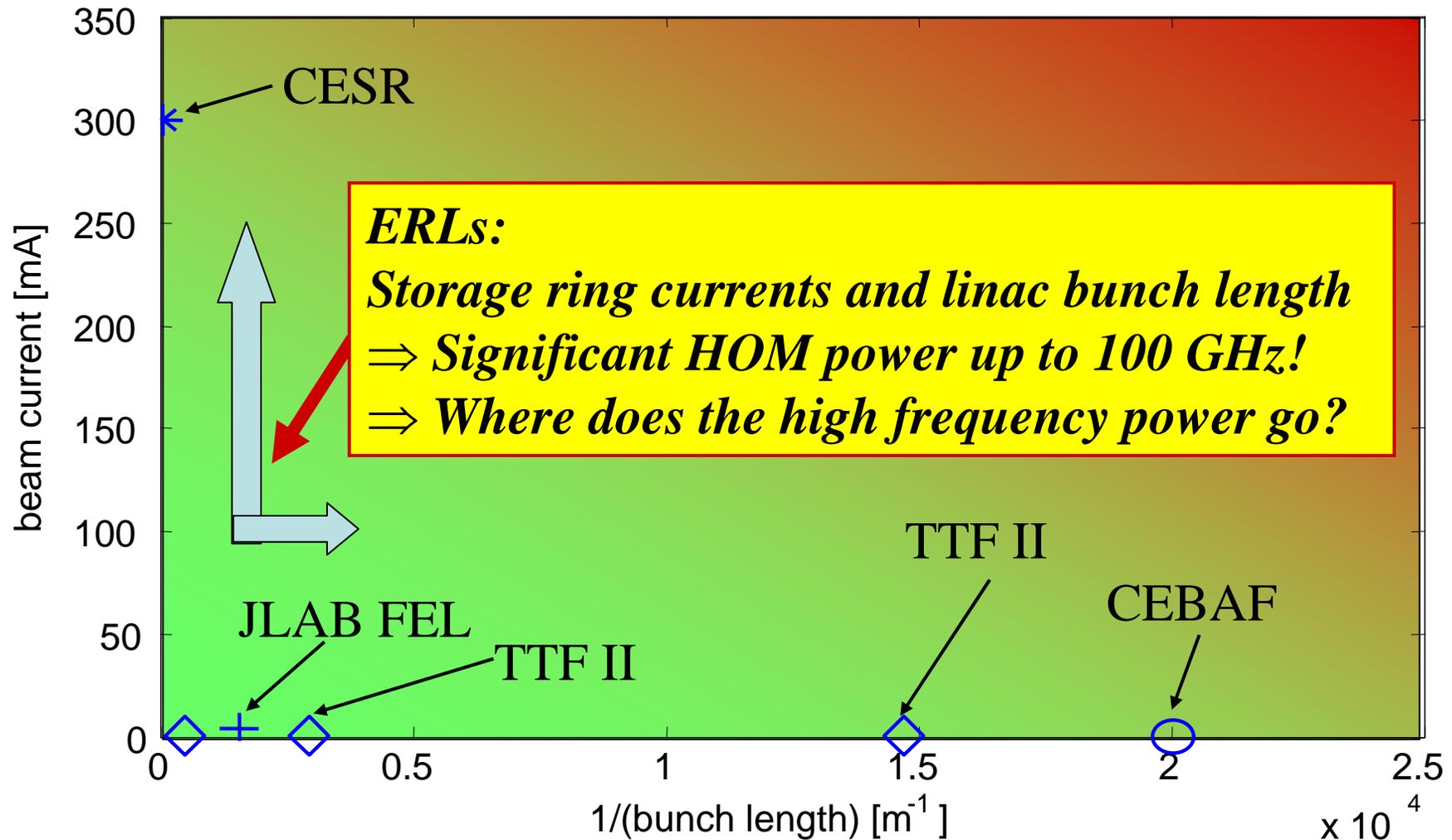
The frequency distribution of the HOM losses is determined by the bunch spectrum and the cavity impedance  $Z(\omega)$ :

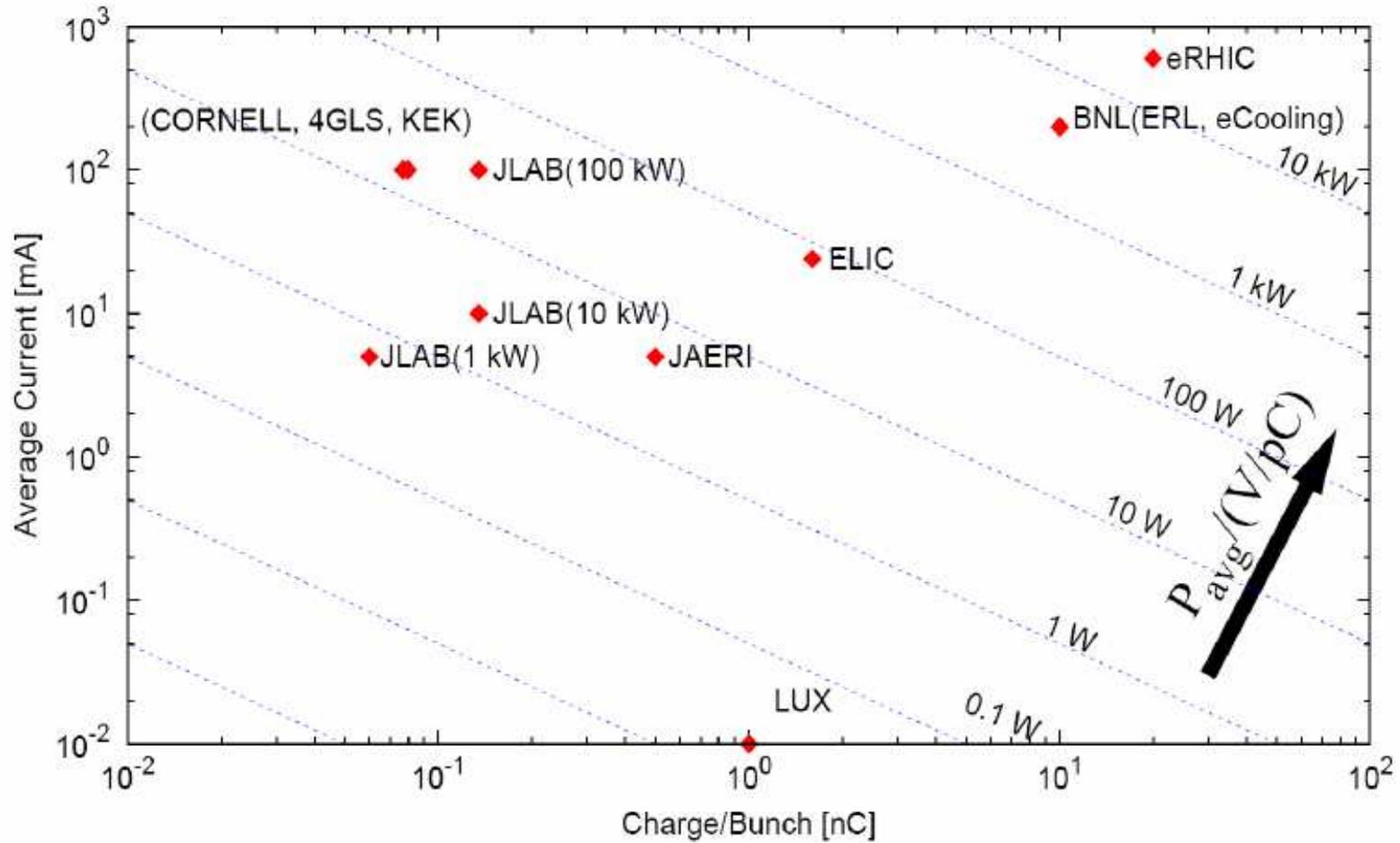
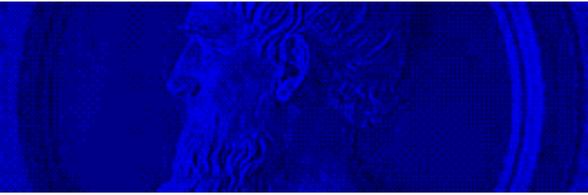
$$P(\omega) \propto Z(\omega)[\tilde{q}(\omega)]^2$$





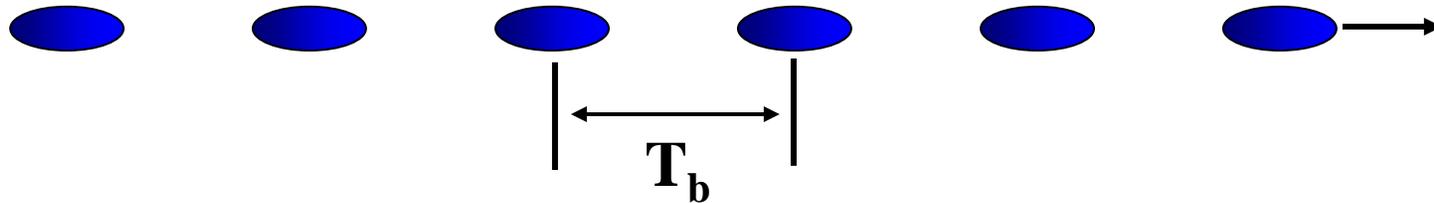
# High current and short bunches







## Bunch Trains: The more Complex Picture



- The HOMs excited by a bunch are decaying due to losses,
- but: still significant field present in the cavity when the next bunch enters the cavity!
- $\Rightarrow$  Resonant excitation of a HOM, if

$$f_{HOM} \approx N \frac{1}{T_b}$$



*The excited HOM power of a bunch train depends on:*

- the HOM losses of a single bunch,
- the beam harmonic frequencies and the HOM frequencies (resonant excitation is possible!),
- the bunch charge and the beam current ( $P_{\text{HOM}} \propto QI$ ),
- and the external quality factor,  $Q_{\text{ext}}$  of the modes.  
Lower  $Q_{\text{ext}}$  means less energy deposited by the beam:

$$P_{\text{HOM}} \propto Q_{\text{ext}}$$



## Bunch Trains: The more Complex Picture

In average the total HOM losses per cavity are given by the single bunch losses (77 pC bunch charge, 2.6 GHz bunch repetition rate,  $\sigma_b = 600 \mu\text{m}$ ):

$$P_{||} = k_{||} Q_{bunch} I_{beam} = 10.4 \text{ V/pC} \cdot 77 \text{ pC} \cdot 0.2 \text{ A} = 160 \text{ W}$$

**But: If a monopole mode is excited on resonance, the loss for this mode can be much higher:**

$$P = \left( \frac{R}{Q} \right) Q I_{beam}^2$$

**⇒ To stay below 200 W:**

- **achieve  $(R/Q)Q < 5000$ ,**
- **or avoid resonant excitation of the mode.**



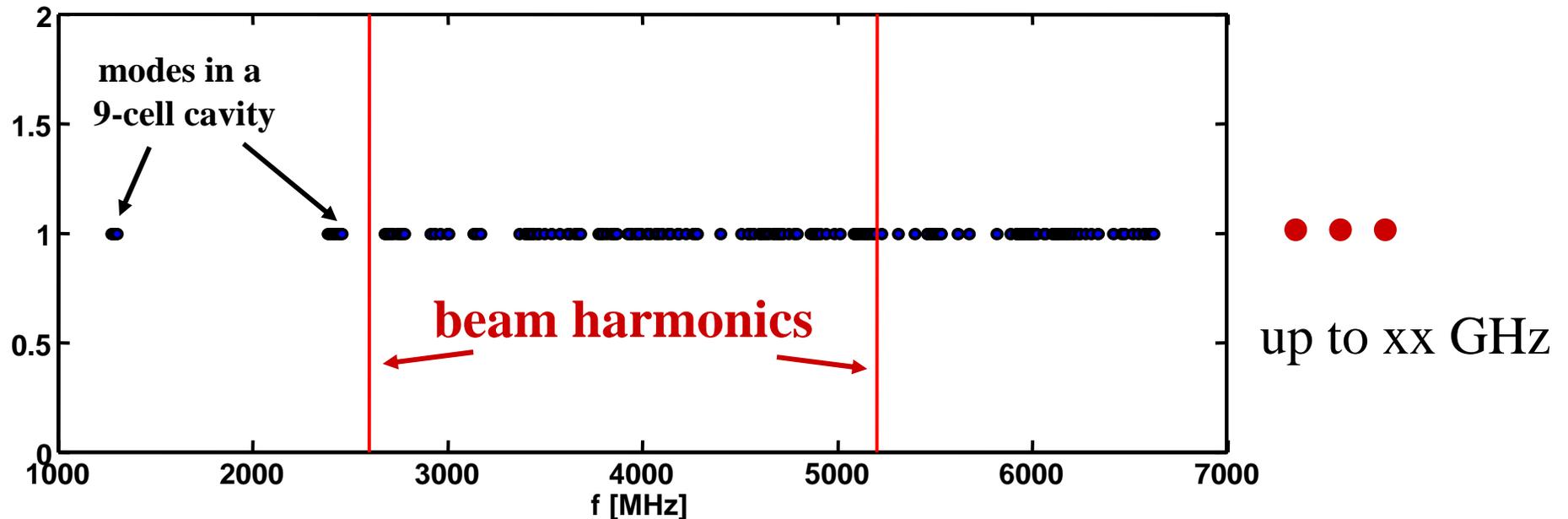
# Bunch Trains: The more Complex Picture

Example: Cornell ERL:

$$f_{HOM} = N \cdot 1.3 \text{ GHz in the injector}$$

$$f_{HOM} = N \cdot 2.6 \text{ GHz in the main linac}$$

... so most of the monopole modes in the ERL will not be excited resonantly.





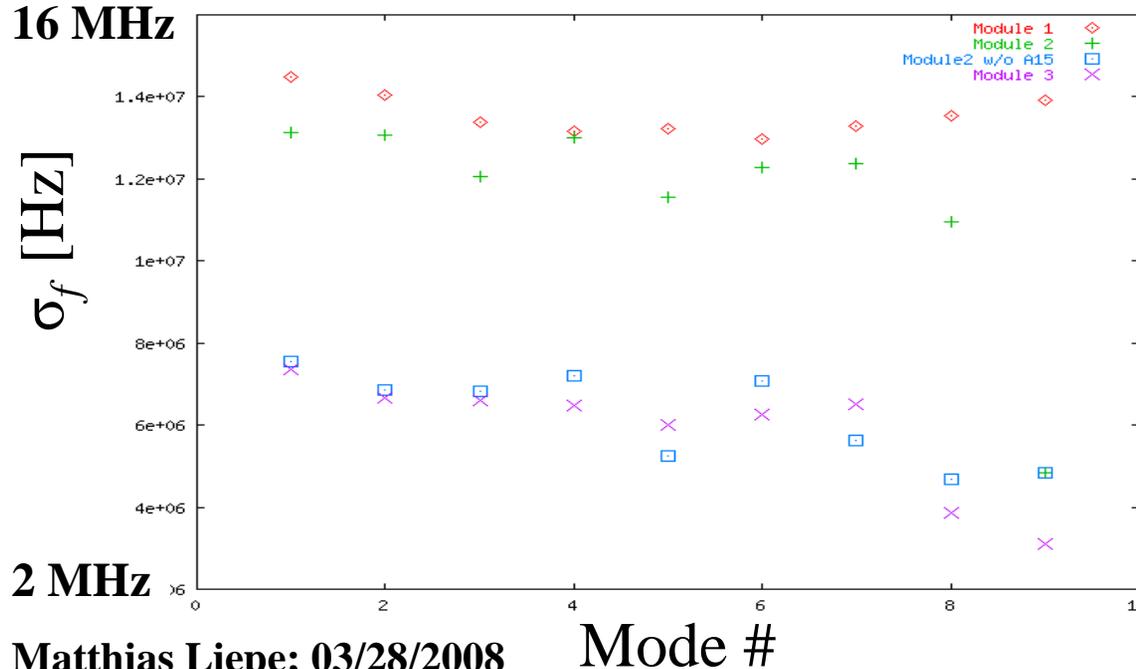
# Bunch Trains: HOM Frequencies Spread

Can one design the HOM frequencies such, that non of the modes are excited resonantly?

- The higher the frequency, the more sensitive is the frequency of a HOM to small perturbations in the cavity shape:

Simple approximation: 
$$\frac{\Delta f_{HOM}}{f_{HOM}} = const.$$

- How large is “const”? Example: 2.4 GHz modes at TTF

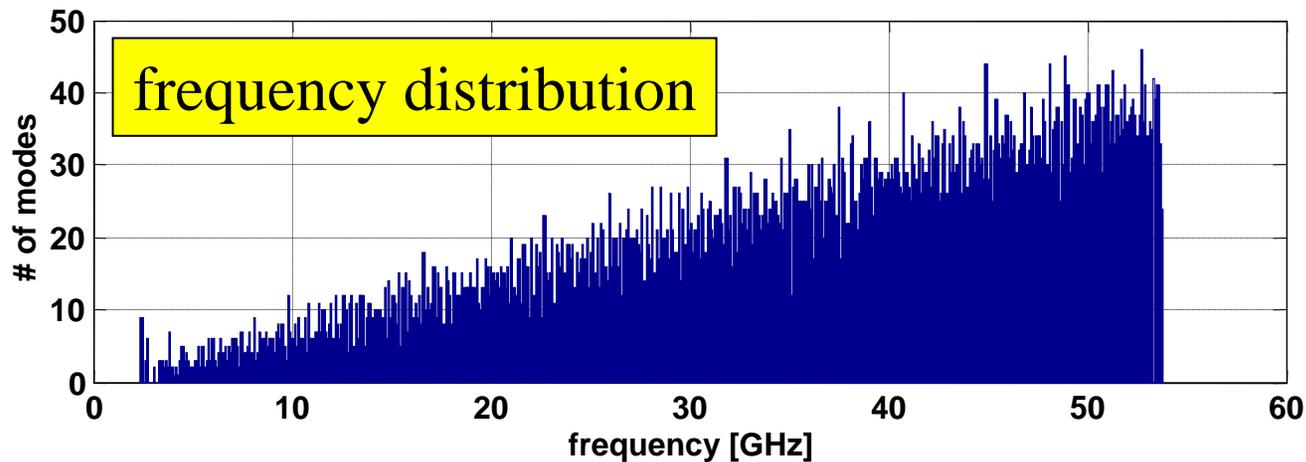
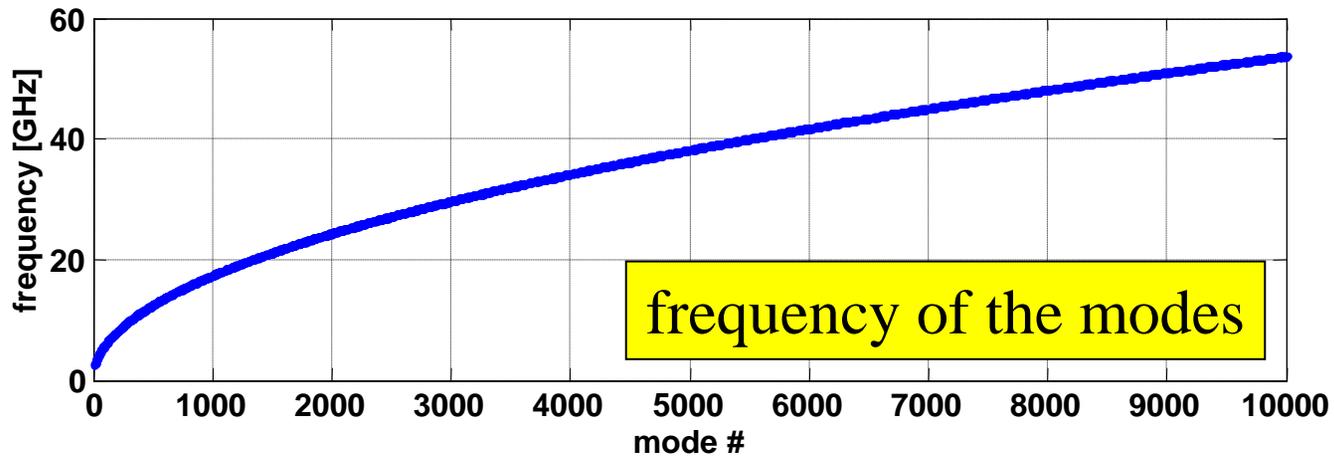


$\sigma_f = 10 \text{ MHz}$   
 $\Rightarrow const = 0.4 \%$

i.e.  $\sigma_f = 20 \text{ MHz at } 5.2 \text{ GHz}$   
 $\sigma_f = 31 \text{ MHz at } 7.8 \text{ GHz}$   
 $\sigma_f = 42 \text{ MHz at } 10.4 \text{ GHz}$   
 ...

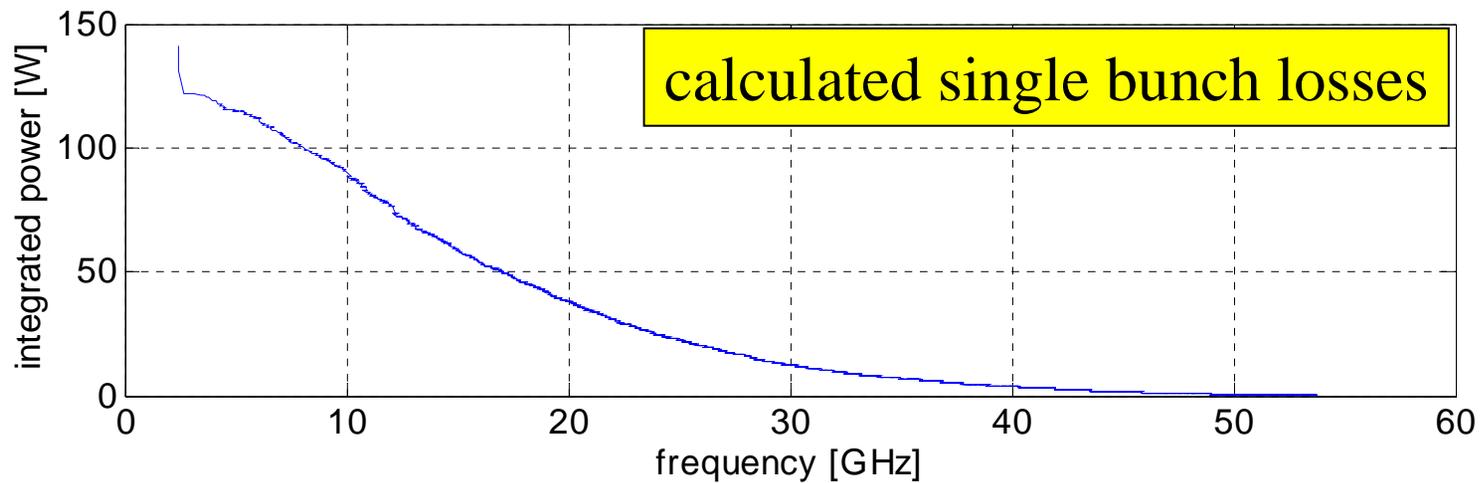
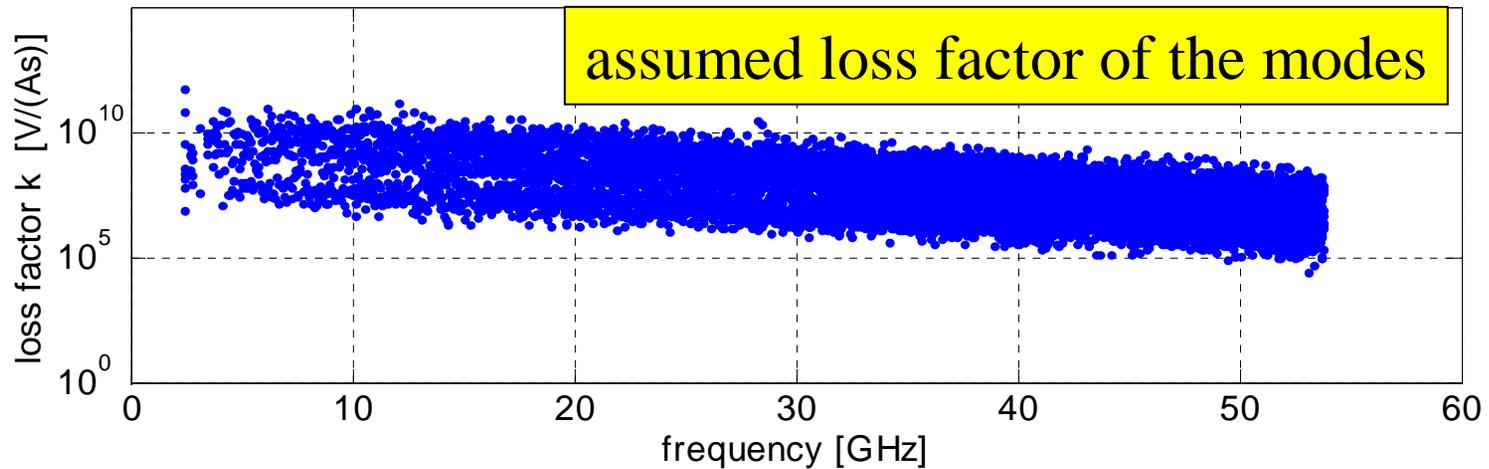


# Bunch Trains: A Simple Model: 10000 Monopoles with random $f$ 's



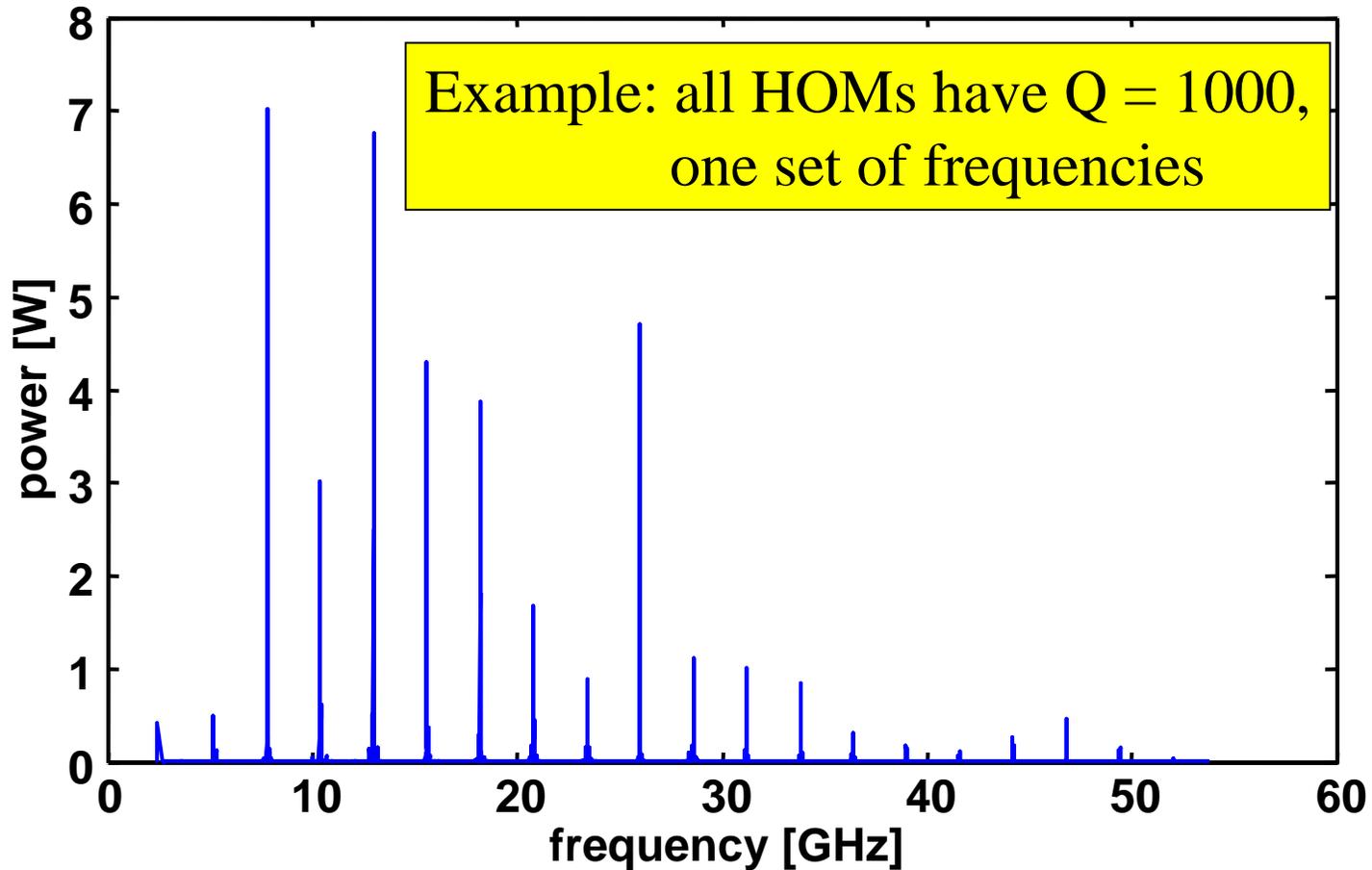


# Bunch Trains: A Simple Model: 10000 Monopoles with random $f$ 's



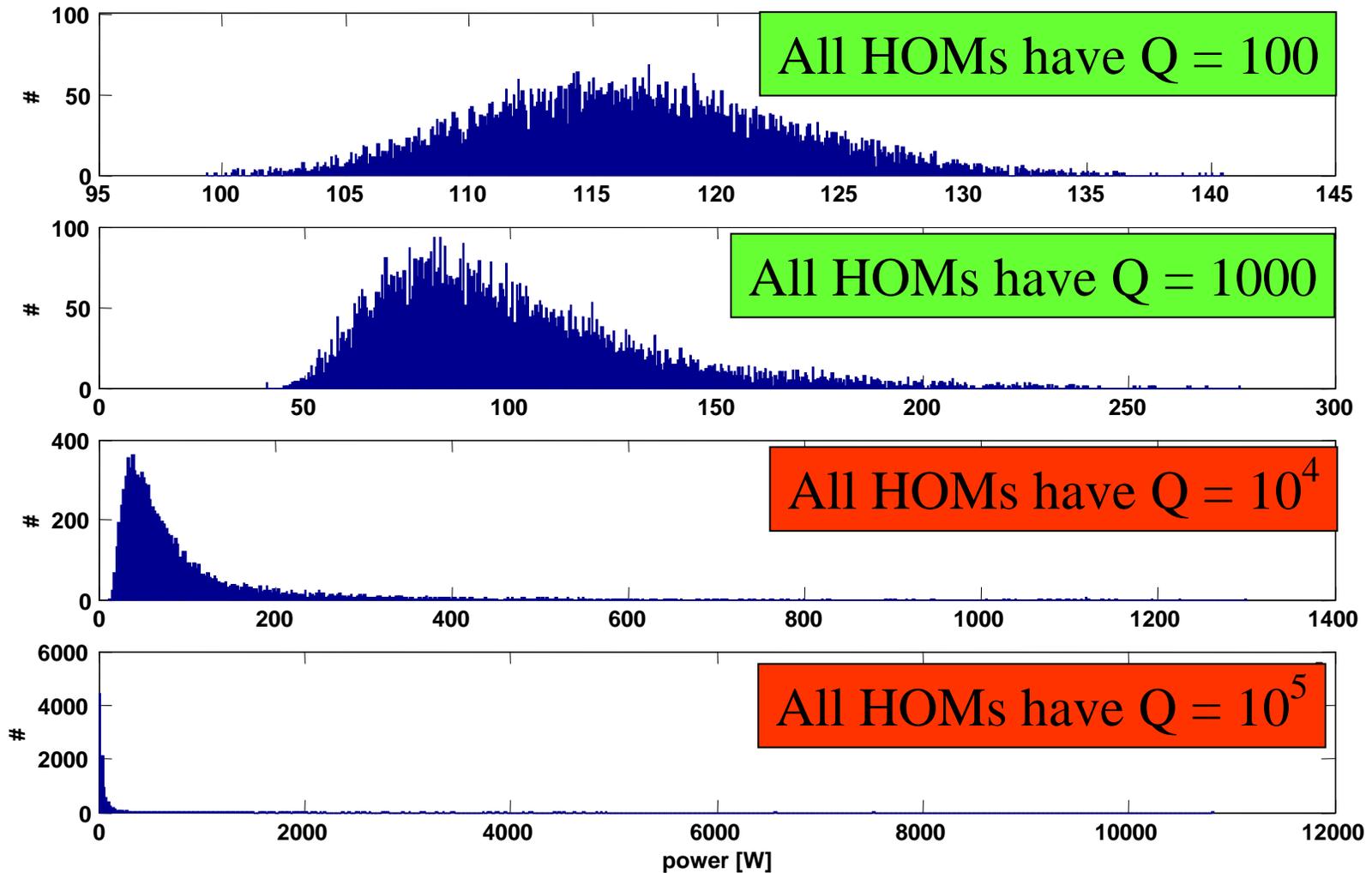


# Bunch Trains: A Simple Model: 10000 Monopoles with random $f$ 's





# A Simple Model: 1000 Monopoles with random $f$ 's Total HOM Monopole Power for random Sets of Frequencies





**Parasitic modes excited by the accelerated beam may lead to:**

- **degradation of the beam quality (transverse emittance growth due to dipole modes, BBU, energy spread),**
- **additional cryo-losses (wall losses, heating of cables and feedthroughs), mostly due to monopole modes.**

⇒ Requirements on the external quality factor,  $Q_{ext}$  of the modes.

Without additional damping the HOMs can have very high quality factors ( $Q > 10^{10}$ )!

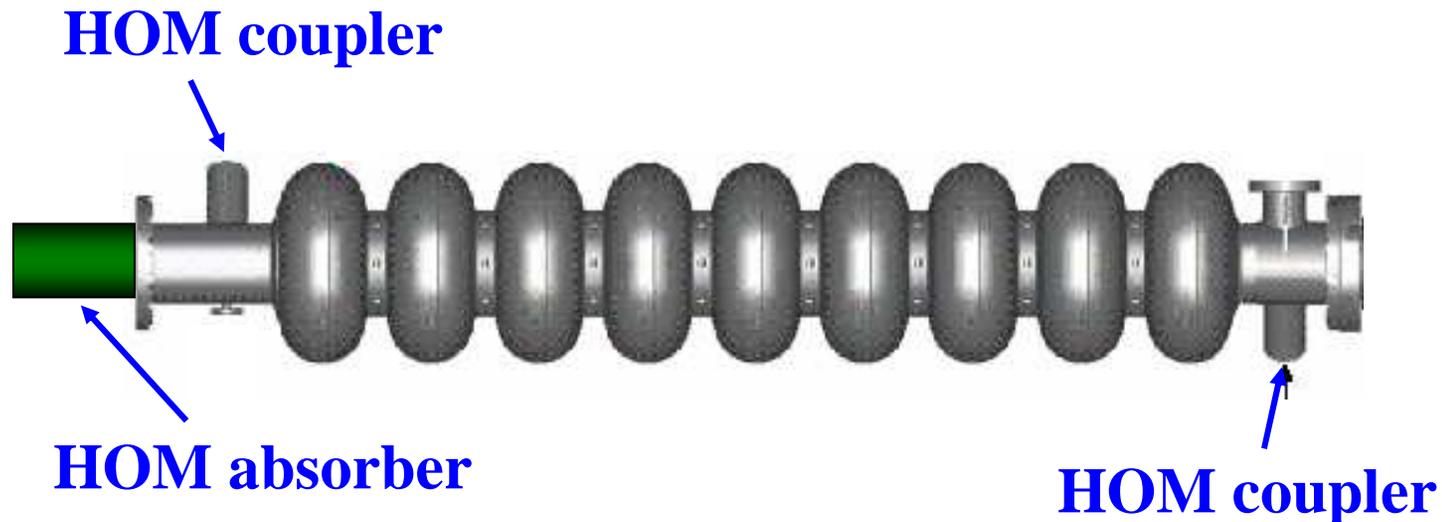


- **Higher order modes**
  - Introduction: HOMs
  - HOM excitation by a beam
  - **HOM damping schemes**
  - HOM damping examples and results



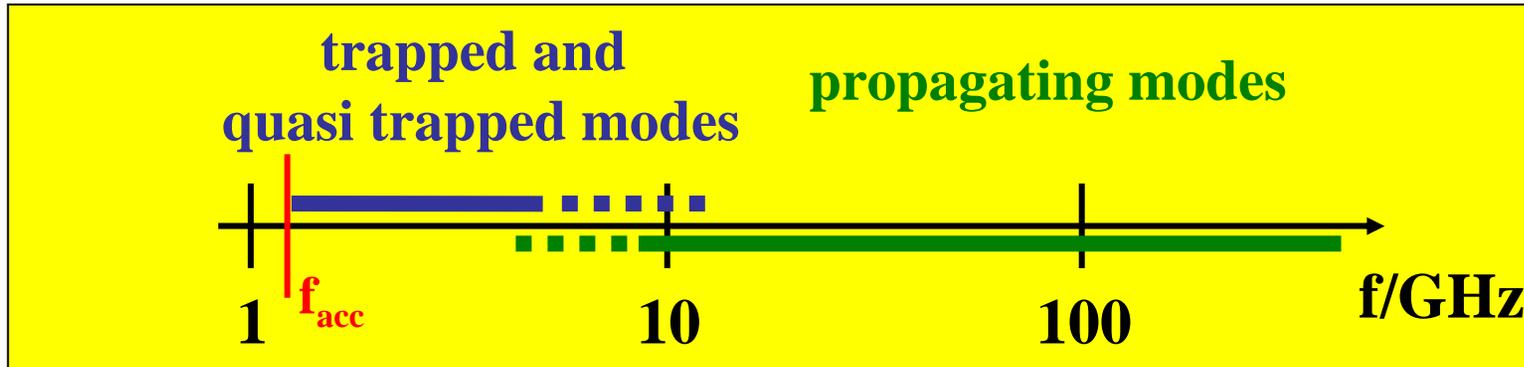
## Solution (for SC Cavities): HOM Couplers and Absorbers

The parasitic e-m fields can be kept below the threshold by means of HOM couplers and HOM absorbers, usually attached to the beam tubes of a s.c. cavity.





# Higher-Order-Mode Couplers and Absorbers

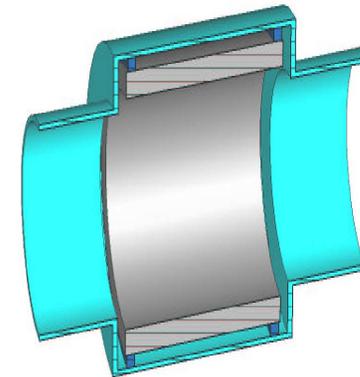
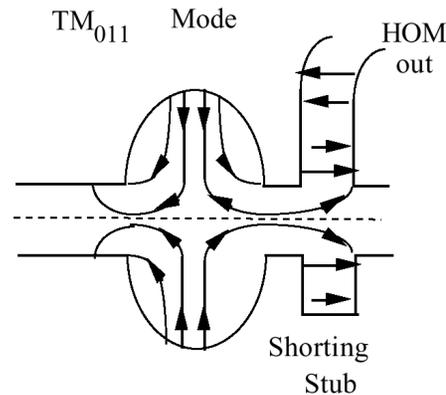
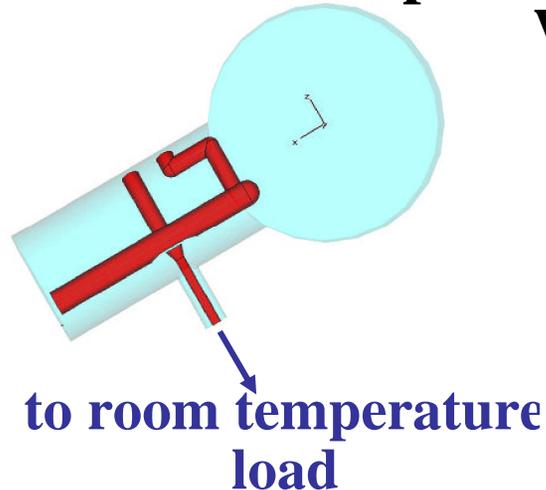


HOM couplers

HOM beam-pipe absorber

antenna couplers

waveguide couplers



absorber between cavities  
temperature level with good  
cryogenic-efficiency

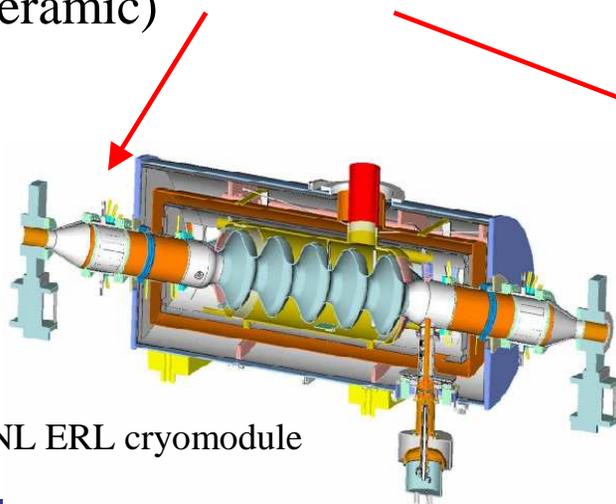
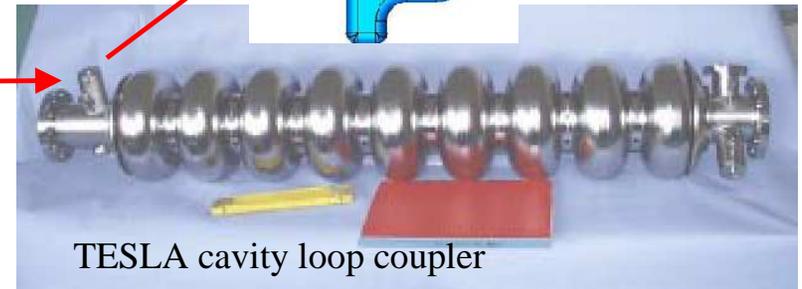
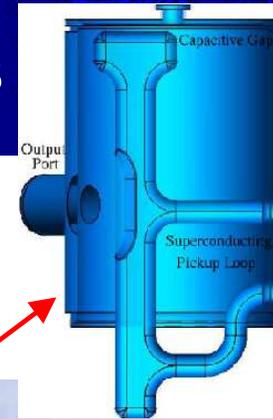
The frequency where the HOMs start to propagate depends on the beam tube diameter:  $\omega_c \propto 1/\text{diameter!}$



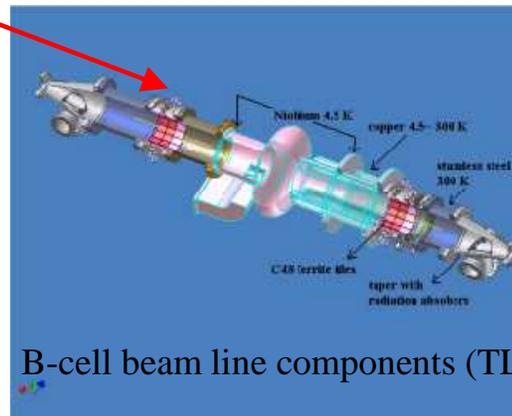
# HOM Extraction/Damping Schemes

## Several approaches are used:

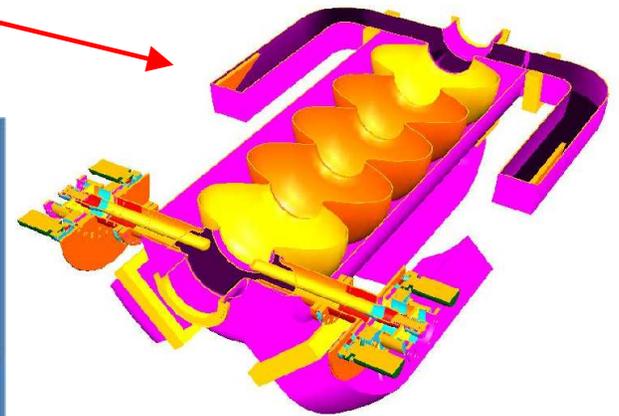
- Loop couplers (several per cavity for different modes/orientations)
- Waveguide dampers
- Beam pipe absorbers (ferrite or ceramic)



BNL ERL cryomodule



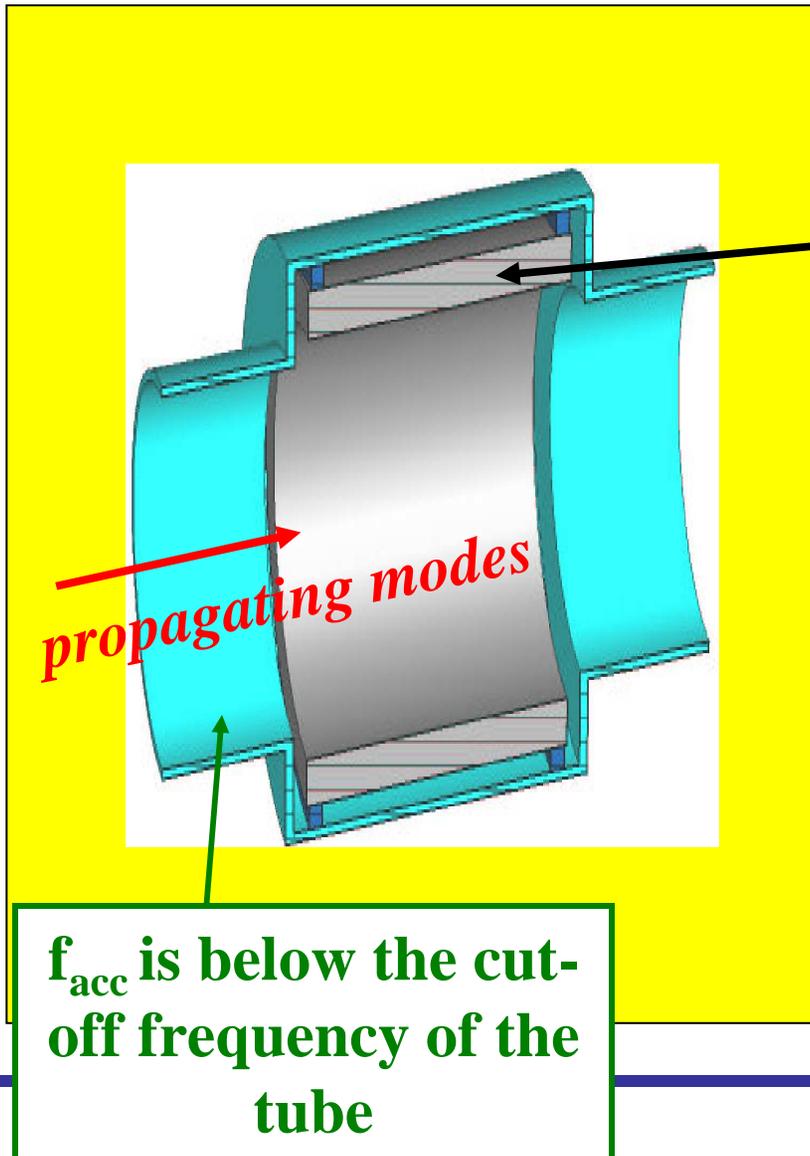
B-cell beam line components (TLS)



JLab proposal



# Broadband Beam Pipe RF Absorber

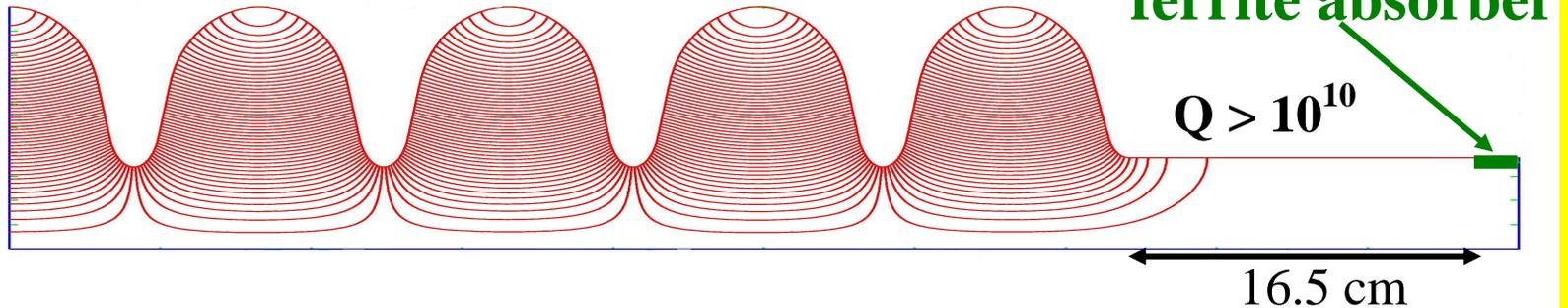


- High frequency modes propagate out the beam pipe.
- RF absorbing material can damp these modes.
- Dissipated power will be intercepted by cooling (water, GHe, LN<sub>2</sub>).
- **Candidate absorber materials:**
  - ferrites (used in CESR HOM load)
  - Zr<sub>10</sub>CB<sub>5</sub> CERADYNE (used for CEBAF HOM load)
  - Mo in AL<sub>2</sub>O<sub>3</sub>
  - ...



# Broadband RF Absorber

*Fundamental mode:  $f=1.300$  GHz*



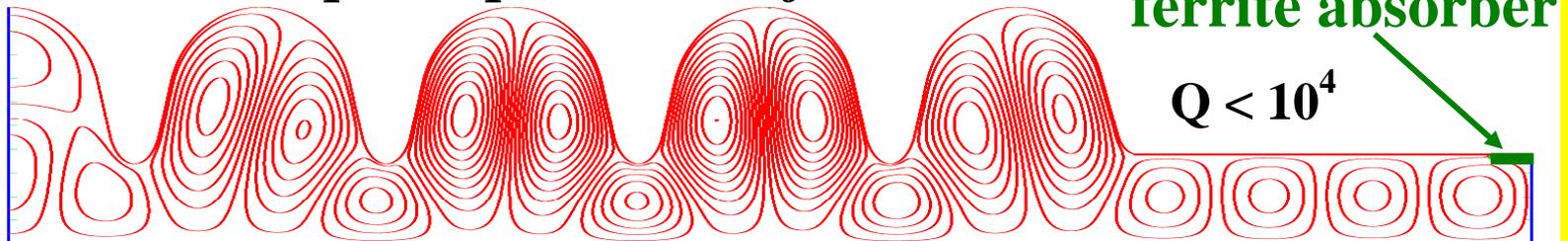
• **Low field at absorber**

⇒ **no significant damping of the fundamental mode**

*but:*

- **Propagating modes have higher fields at the absorber**  
⇒ **damping and power extraction!**

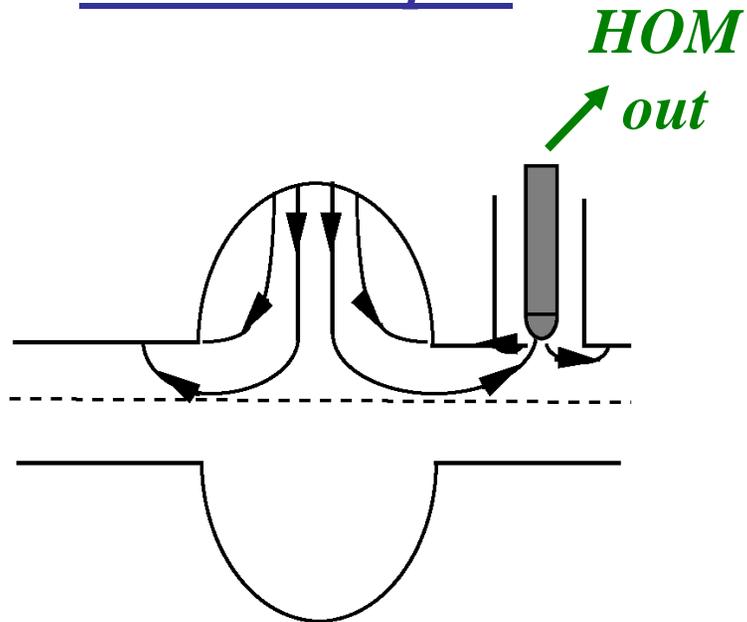
*Example: dipole mode:  $f=3.9$  GHz*





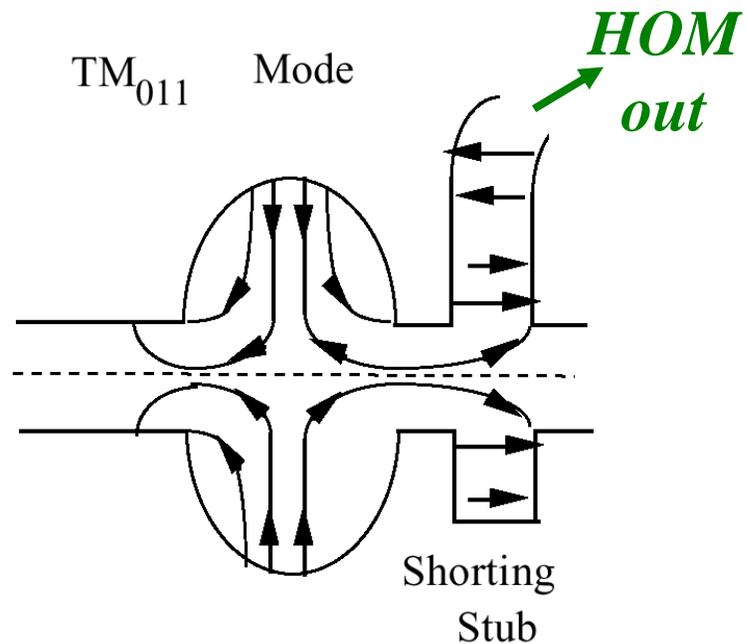
# Higher-Order-Mode Couplers

## Coaxial Coupler



**Rejection filter  
suppresses coupling to  
the accelerating mode.**

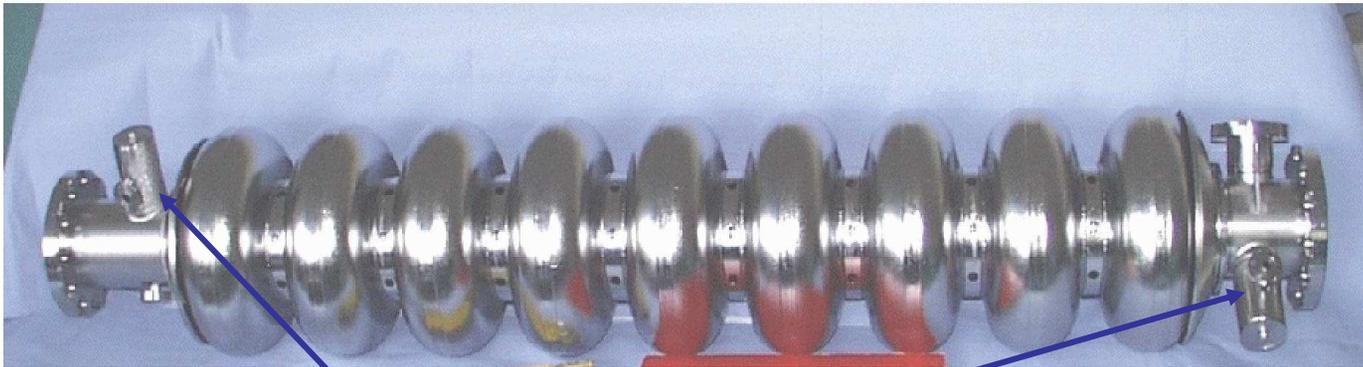
## Waveguide Coupler



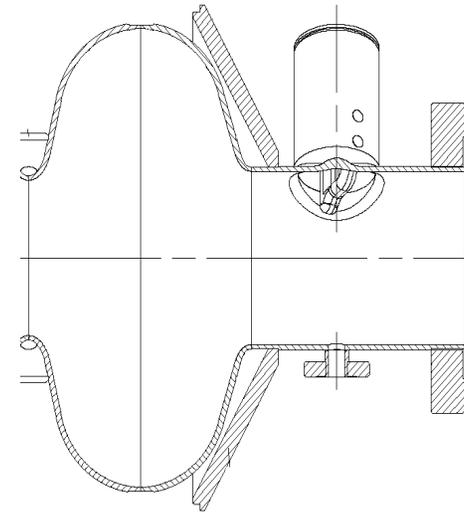
**Waveguide cutoff  
suppresses coupling to  
the accelerating mode.**



## TTF HOM Loop Coupler (1)



*HOM coupler at each side  
of the cavity close to end cell  
to damp HOMs*



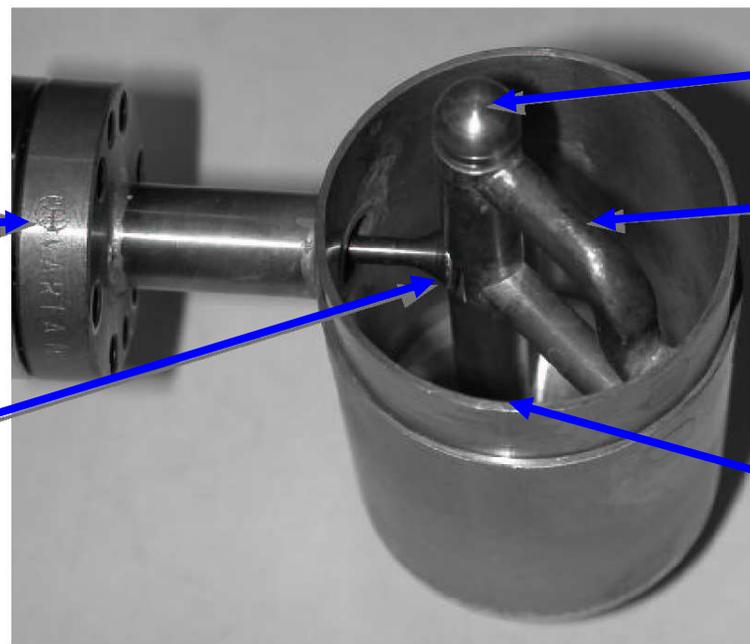


## HOM Loop-Couplers

### Coupler model:

*output to  
room temp.  
load*

*capacitive  
coupling*



*superconducting  
pick-up antenna  
superconducting  
pick-up loop*

*capacitor of the  
1.3 GHz notch  
filter*

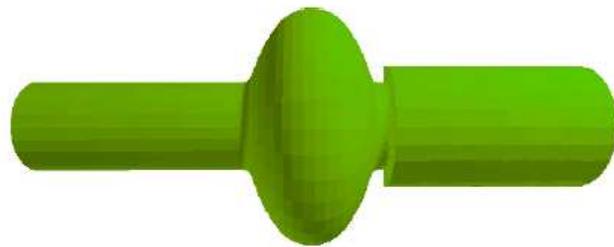
- Important to reduce  $Q$  of non-propagating dipole modes.
- Can only handle a few 10 W.
- Will work up to a few GHz but not above.
- Cooling / heating from fundamental mode issue in cw cavity operation.



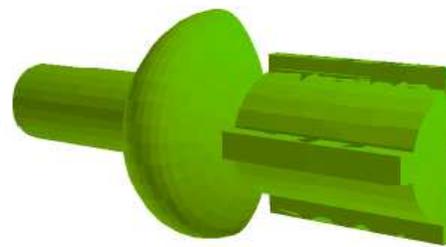
# Methods for HOM Damping

Methods of broad-band HOM damping:

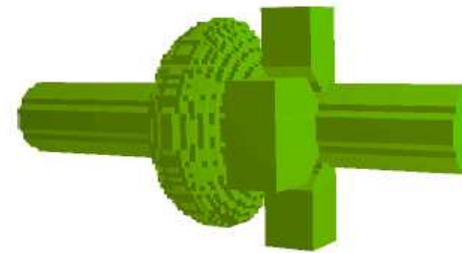
Strong HOM damping has been shown in single-cell cavities, e.g. Cornell and B-factory storage rings. Studies show these methods can be applied to multi-cell cavities. Options include multiple coaxial antennas, beam pipe loads, waveguide loads.



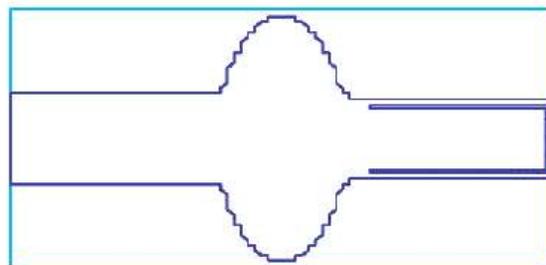
Enlarged beam pipe.  
(KEK, BNL, Cornell ERL)



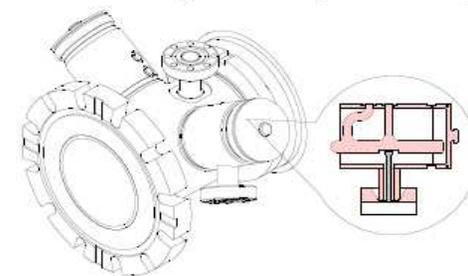
Fluted beam pipe.  
(Cornell, CESR)



Waveguide dampers  
(CEBAF, PEP-II)



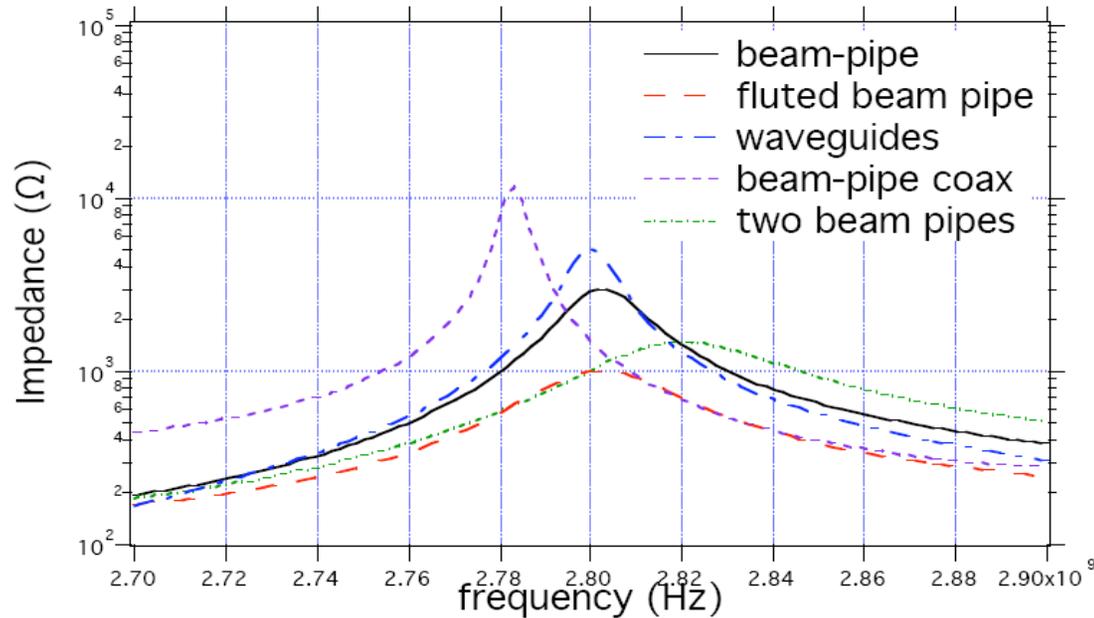
Coaxial/radial beam pipe  
(KEK, JAERI)



Multiple coaxial loops  
(DESY, CERN)



# Methods for HOM Damping: Effectiveness



TM<sub>011</sub> mode with various damping schemes.

	Freq. MHz	Q <sub>ext</sub>	R* ( )	R/Q ( )
b-pipe	2803	252	3001	11.9
flutes	2803	137	1010	7.3
w-guide	2800	353	5040	14.3
bp-coax	2783	725	11879	16.4
2xbp	2822	121	1481	12.2

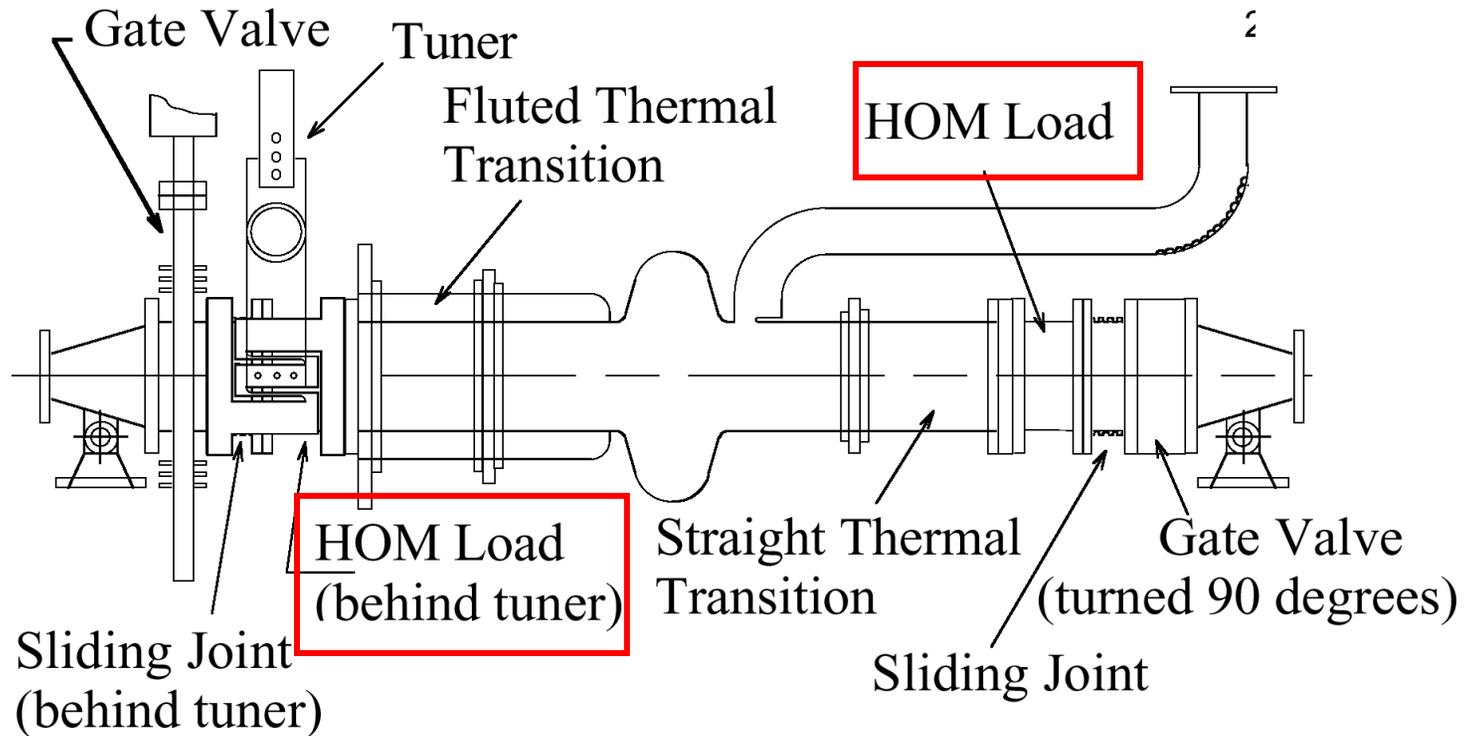
\*R=V<sup>2</sup>/2P



- **Higher order modes**
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  - **HOM damping examples and results**



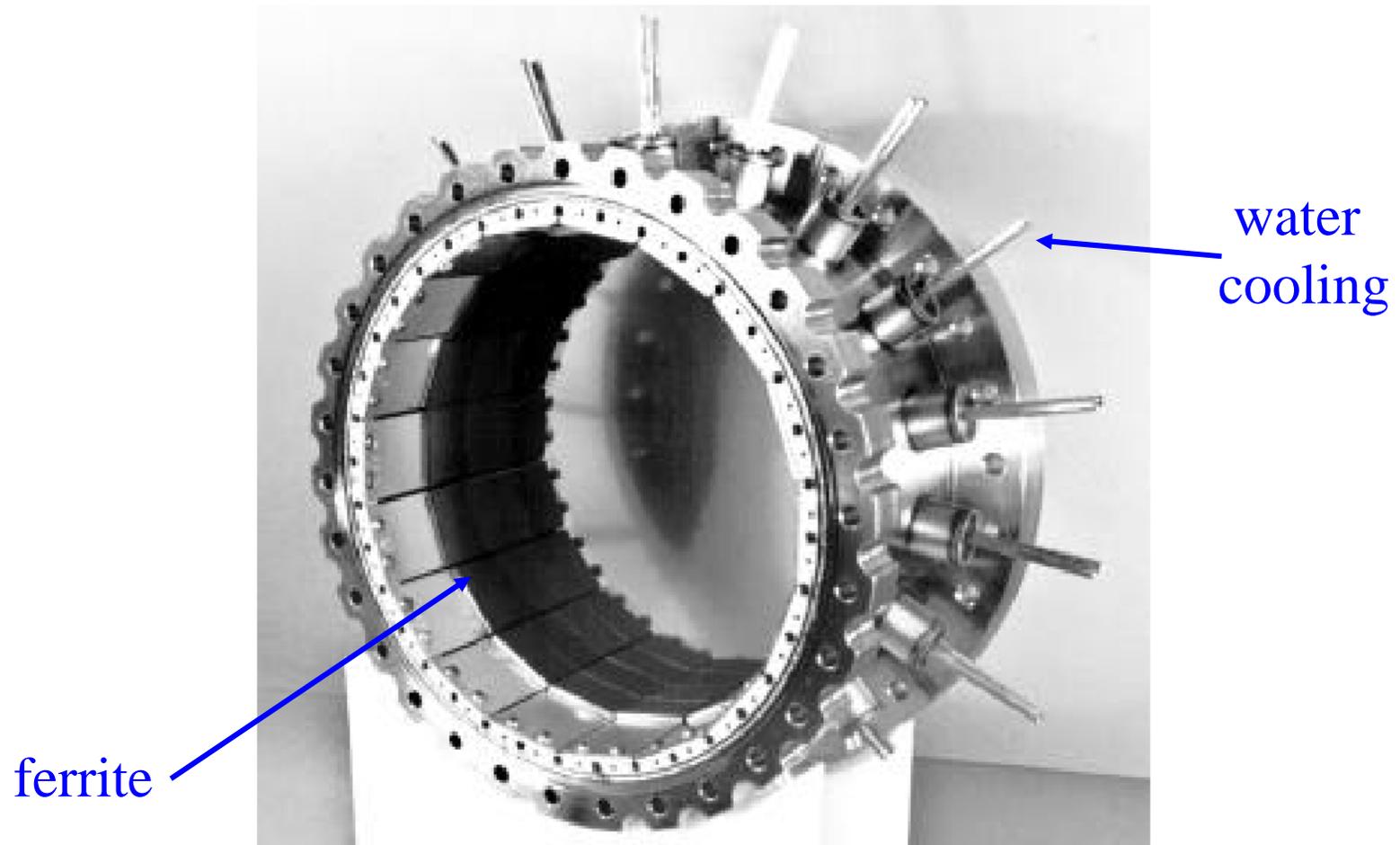
## Example 1: CESR HOM Ferrite Absorber (1)



- Flute beam pipe  $\Rightarrow$  guide out the first two defecting modes.
- Total HOM power: **several kW!**
- $Q_{\text{ext}} < 10^3$



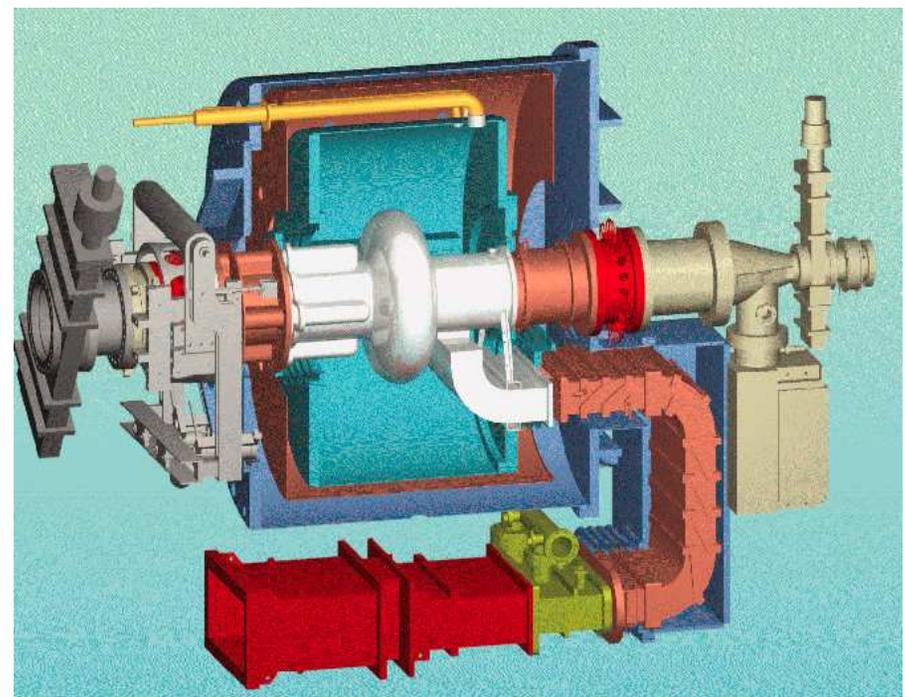
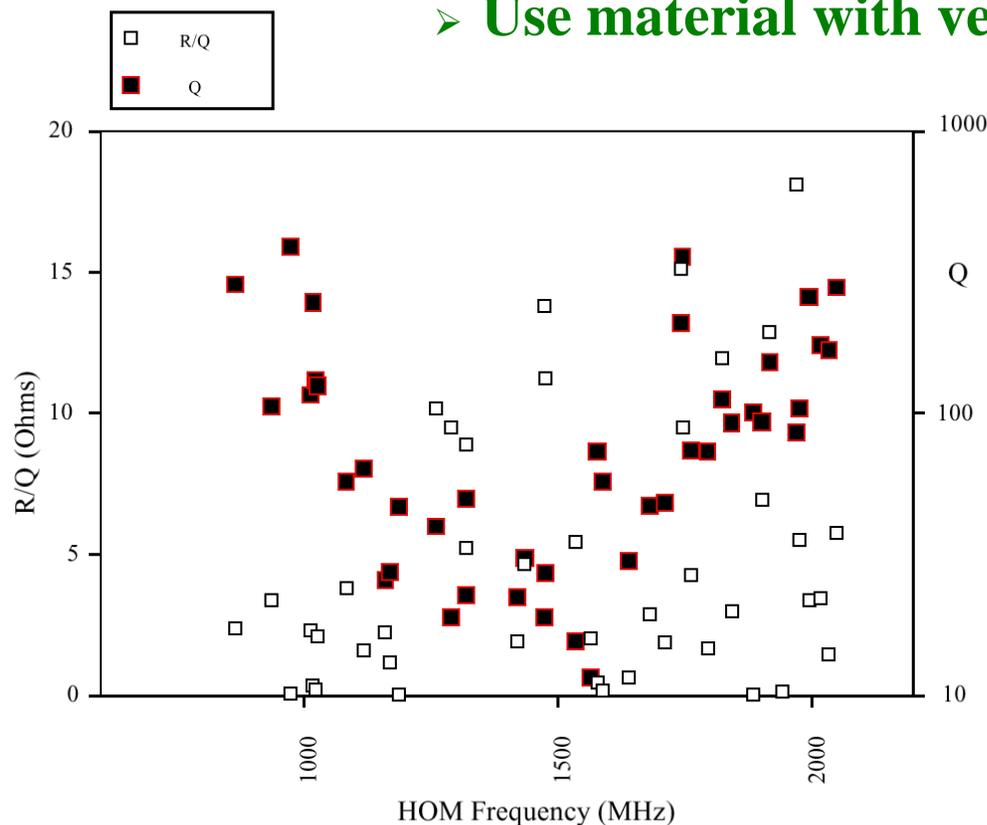
## CESR HOM Ferrite Absorber (2)





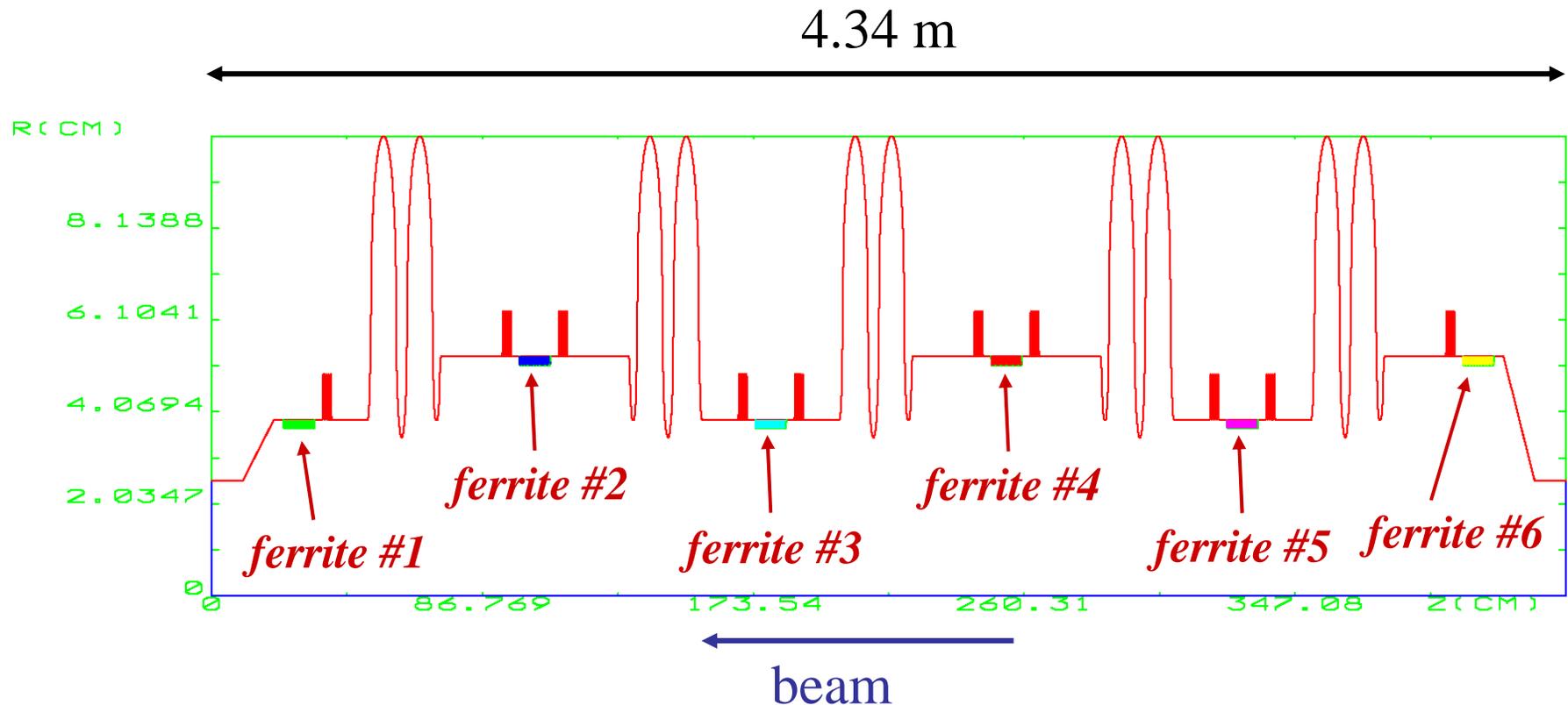
## CESR HOM Ferrite Absorber (3)

- Use a single cell (no reflection by irises between cells)
- Open beam tubes so that all modes propagate out the beam tubes!
- Use material with very high RF losses.





## Example 2: The Cornell ERL Injector

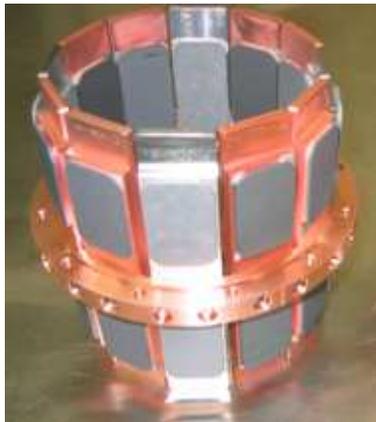
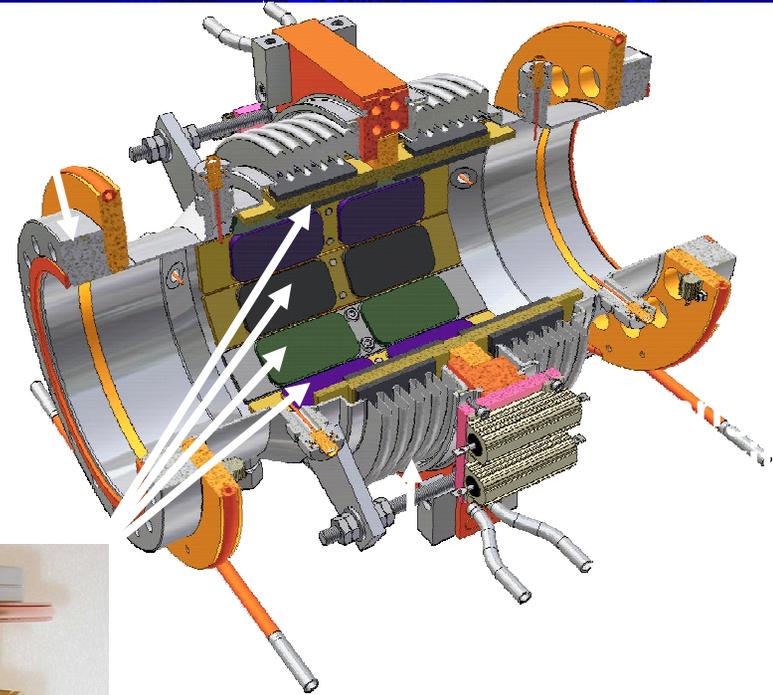


**HOM damping concept: Make all TM monopole and all dipole modes propagating by increasing the beam tube diameter (as in CESR).**



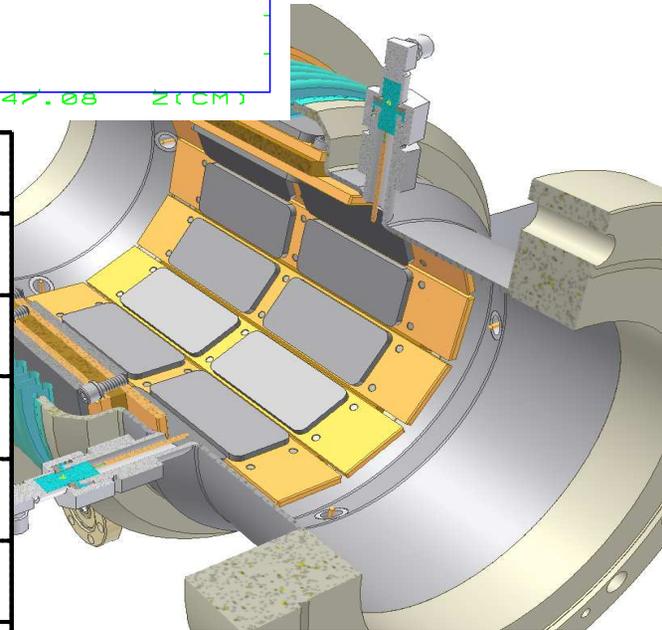
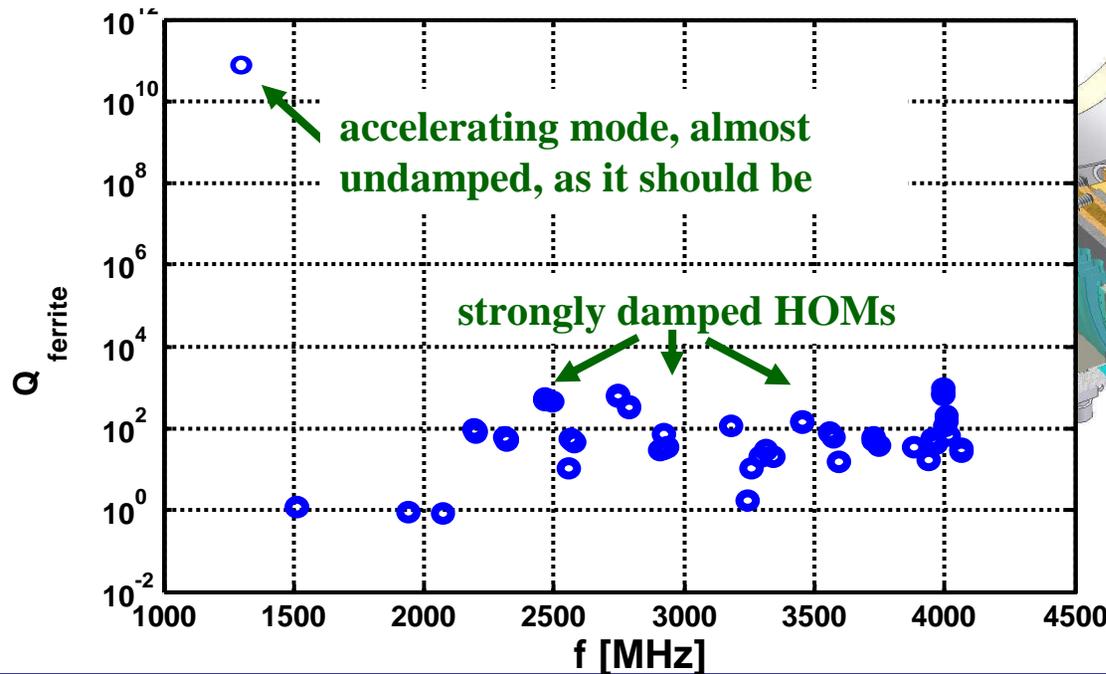
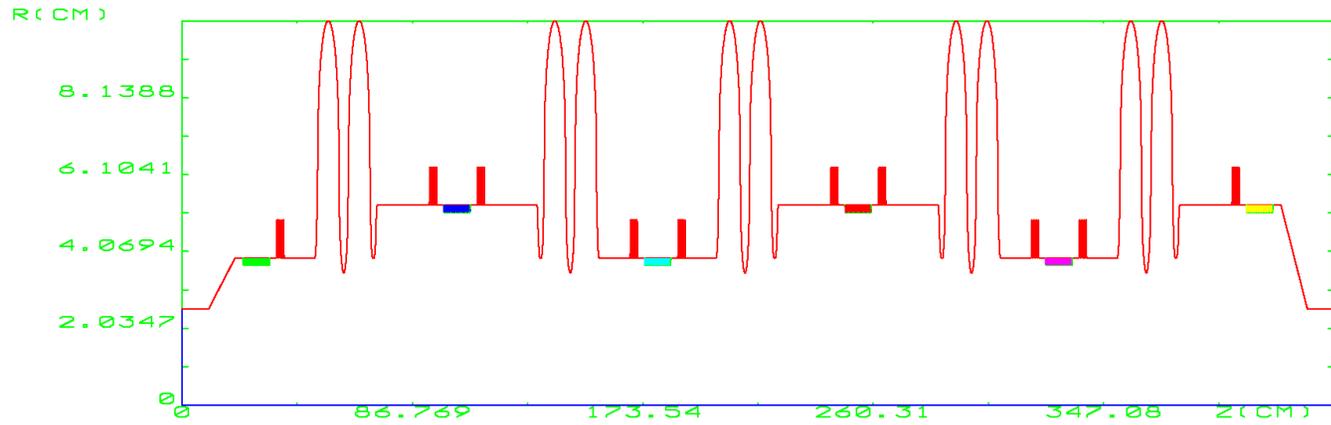
# Cornell ERL Beam Line HOM Loads

Power per load	26 W (200 W max)
HOM frequencies	1.4 – 100 GHz
Operating temp.	80 K
Coolant	He Gas
RF absorbing tiles	TT2, Co2Z, Ceralloy





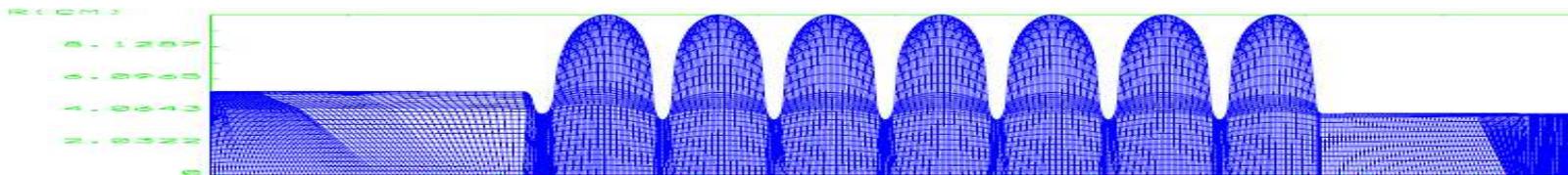
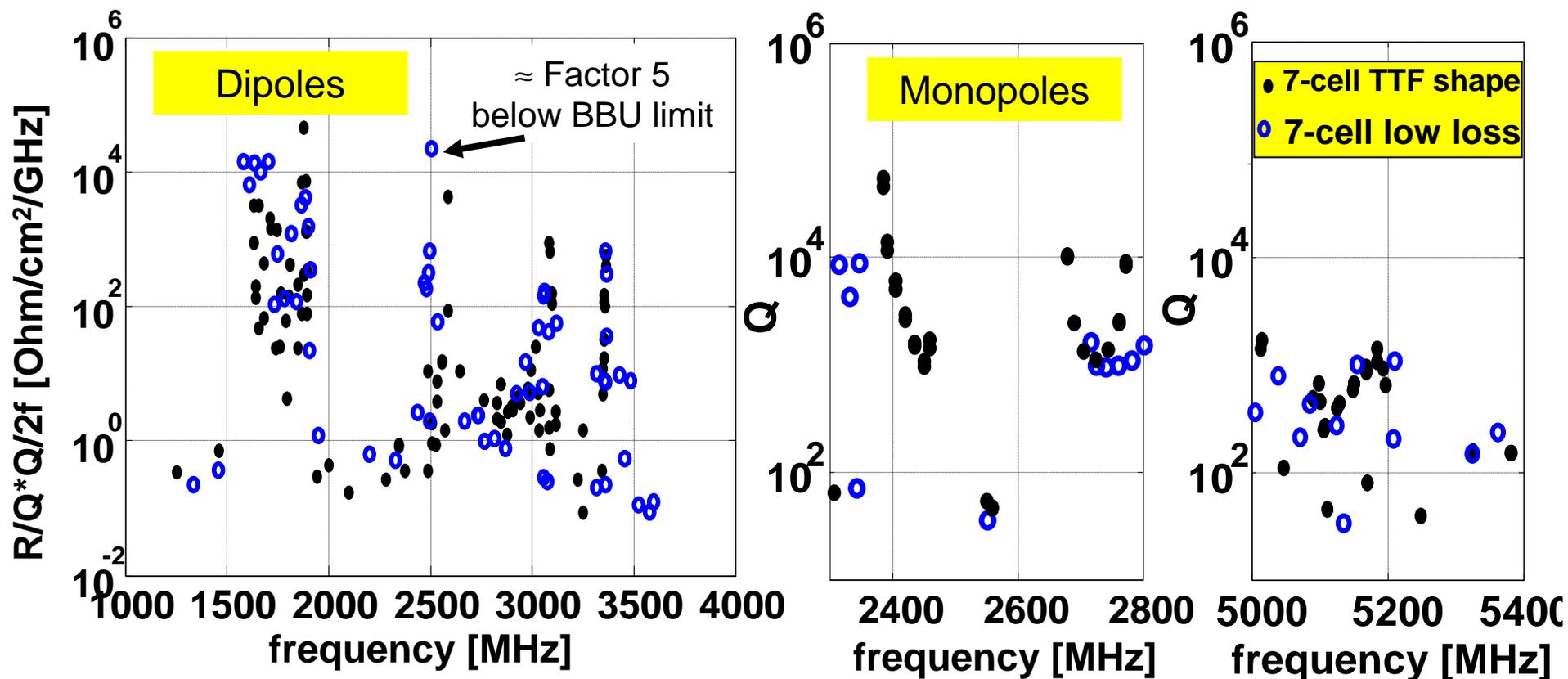
# Cornell ERL Beam Line HOM Loads: Damping Calculations





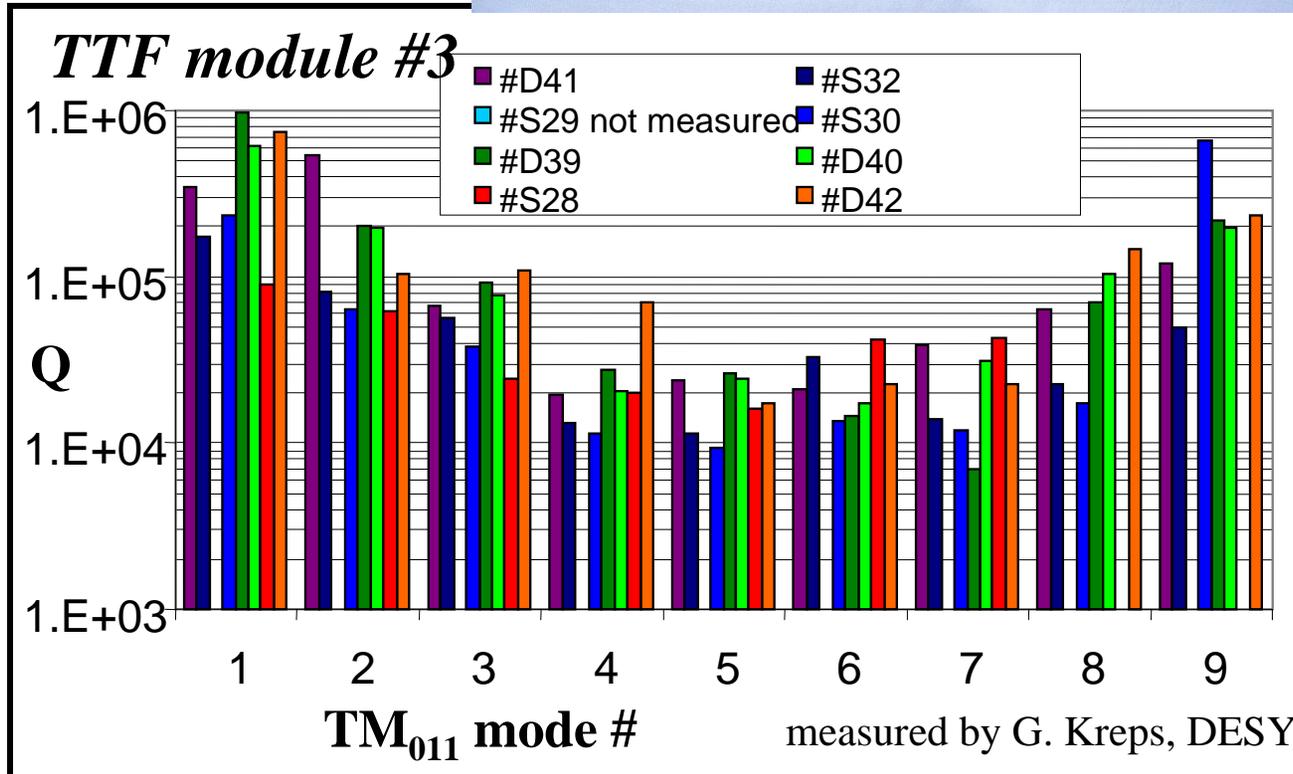
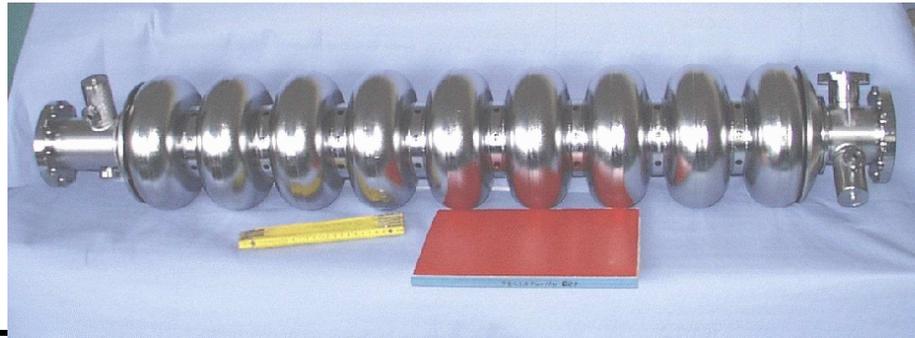
# ERL Main Linac HOM Damping Simulations

- CLANS calculations (started 3D Microwave Studio models)
- Modes are sufficiently damped for 100 mA operation



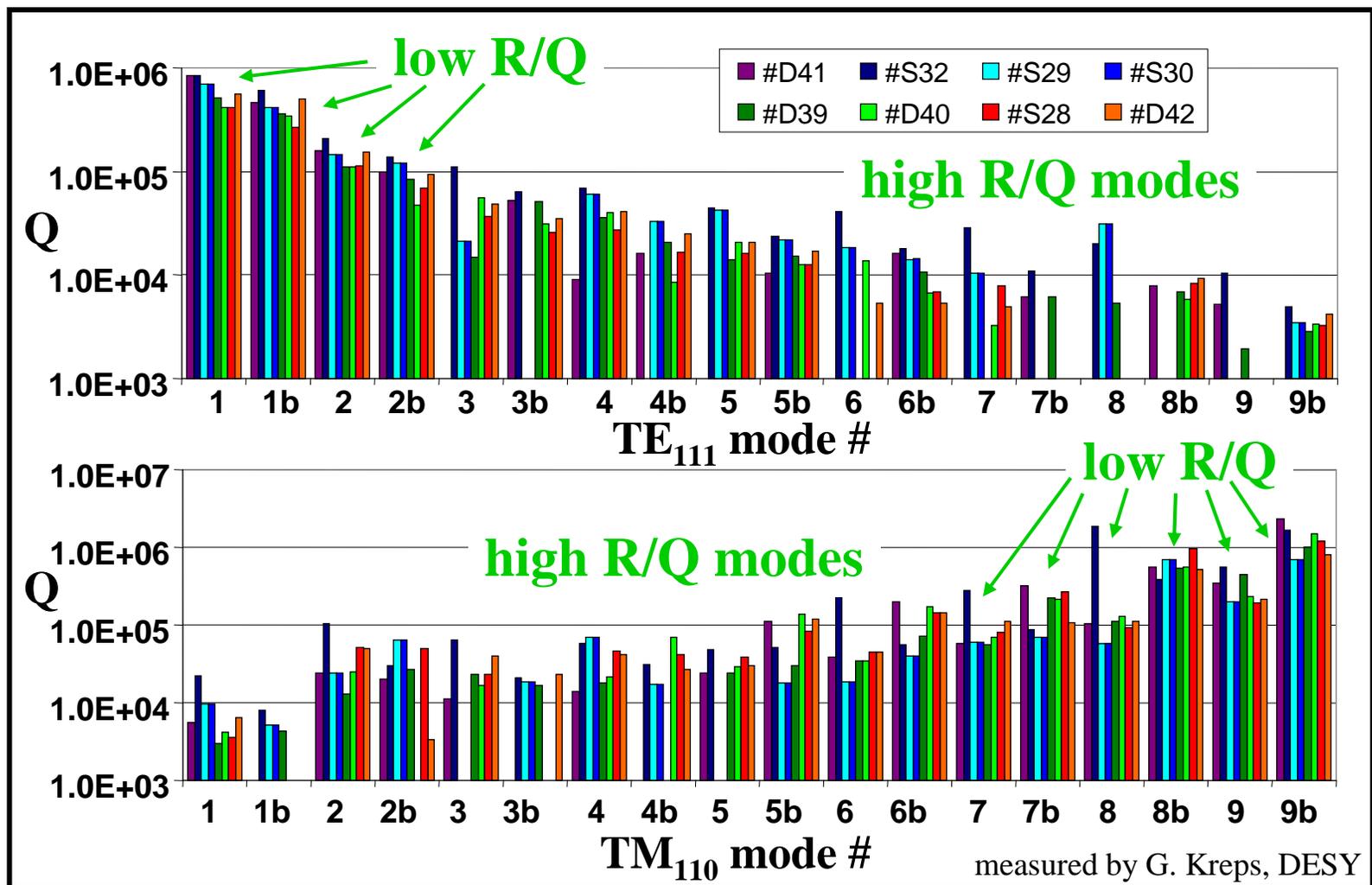


# Example 4: ILC Cavity with HOM Loop Couplers





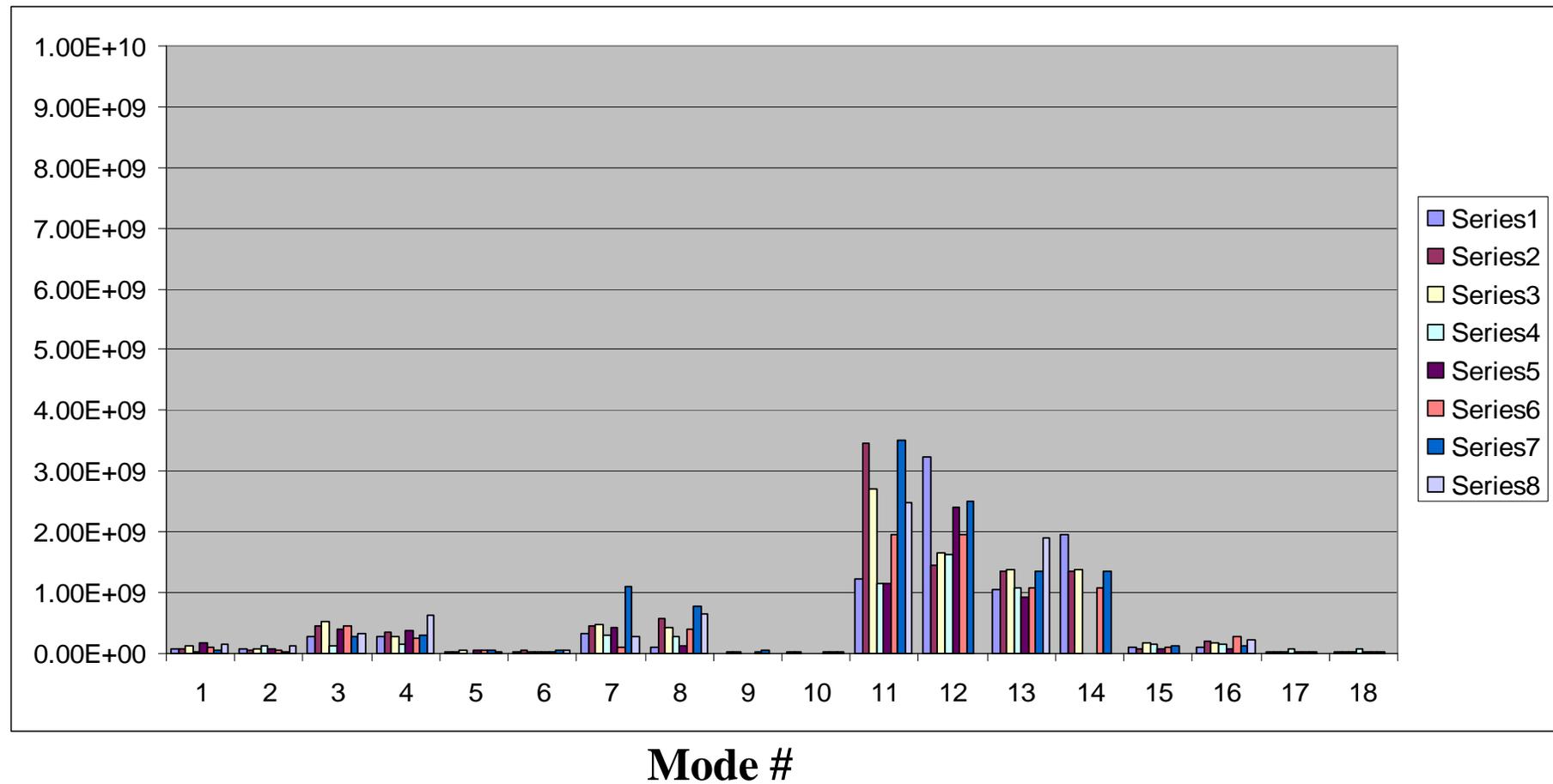
# TTF HOM Coupler: Measured Damping of Dipole Modes





# 9-cell Cavities TE111 Dipole Modes: TTF Module 2

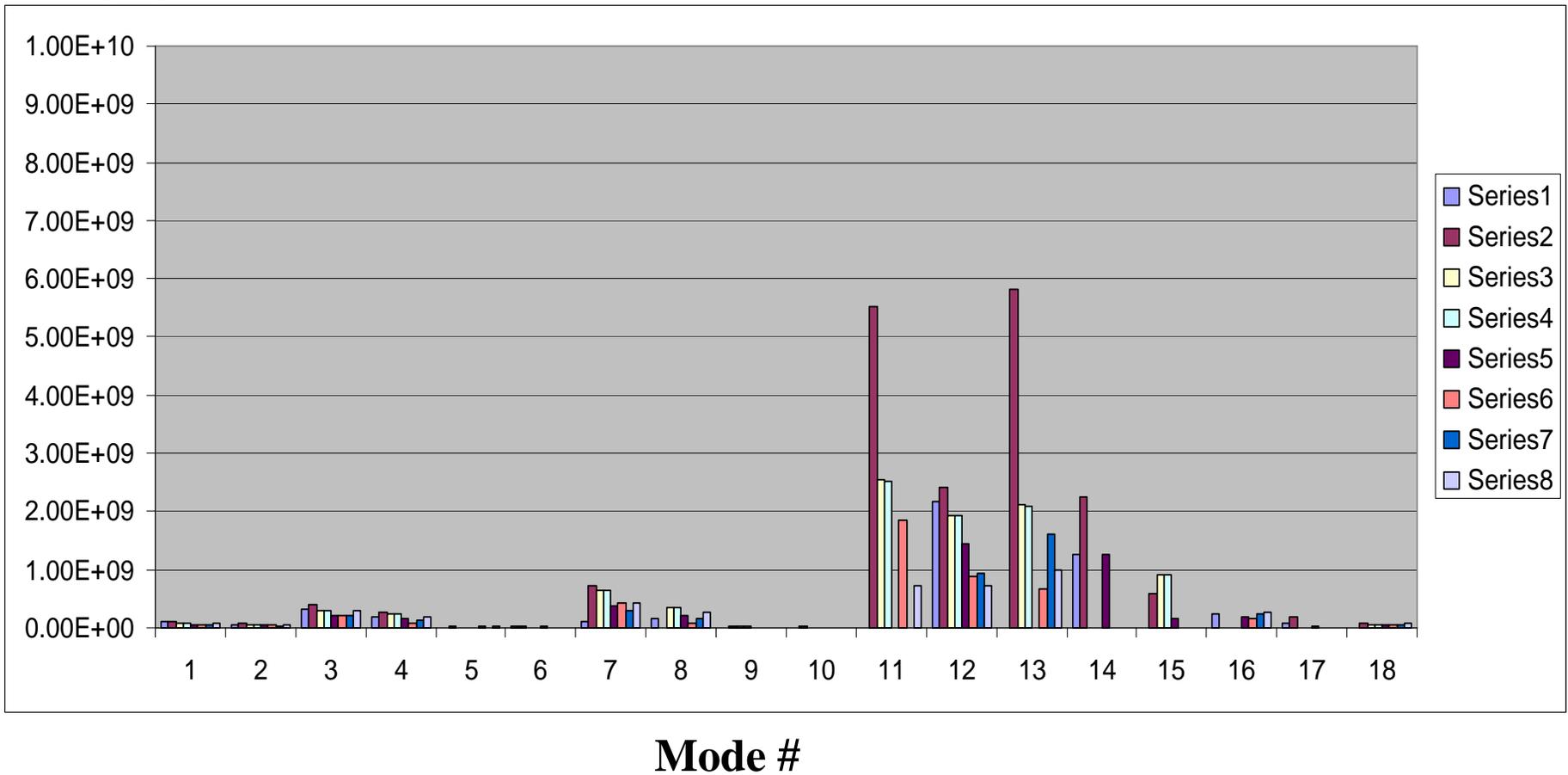
$(R/Q)Q_f$  [ $\Omega$ MHz]





# 9-cell Cavities TE111 Dipole Modes: TTF Module 3

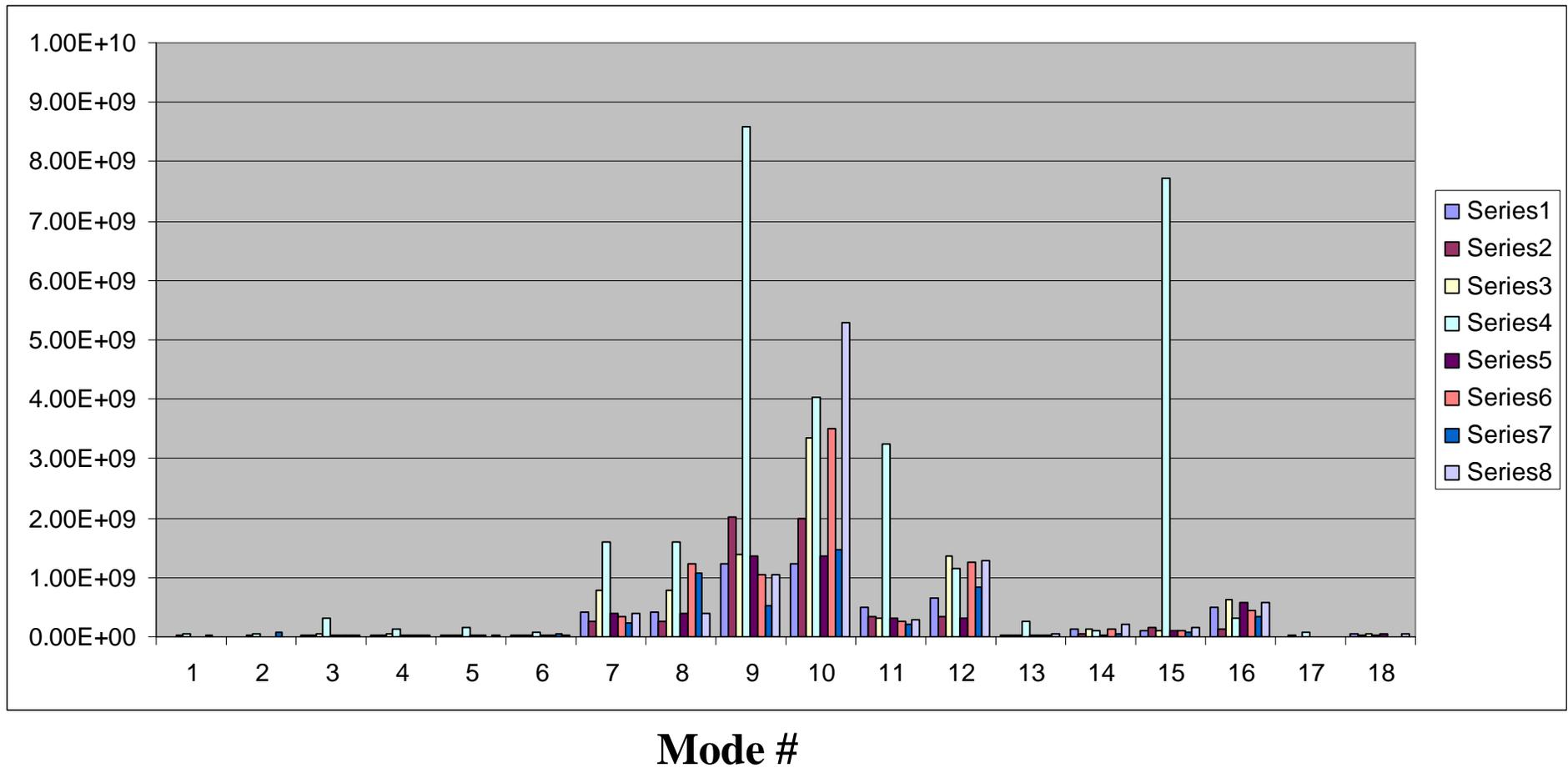
$(R/Q)Q_f$  [ $\Omega\text{MHz}$ ]





# 9-cell Cavities TM110 Dipole Modes: TTF Module 2

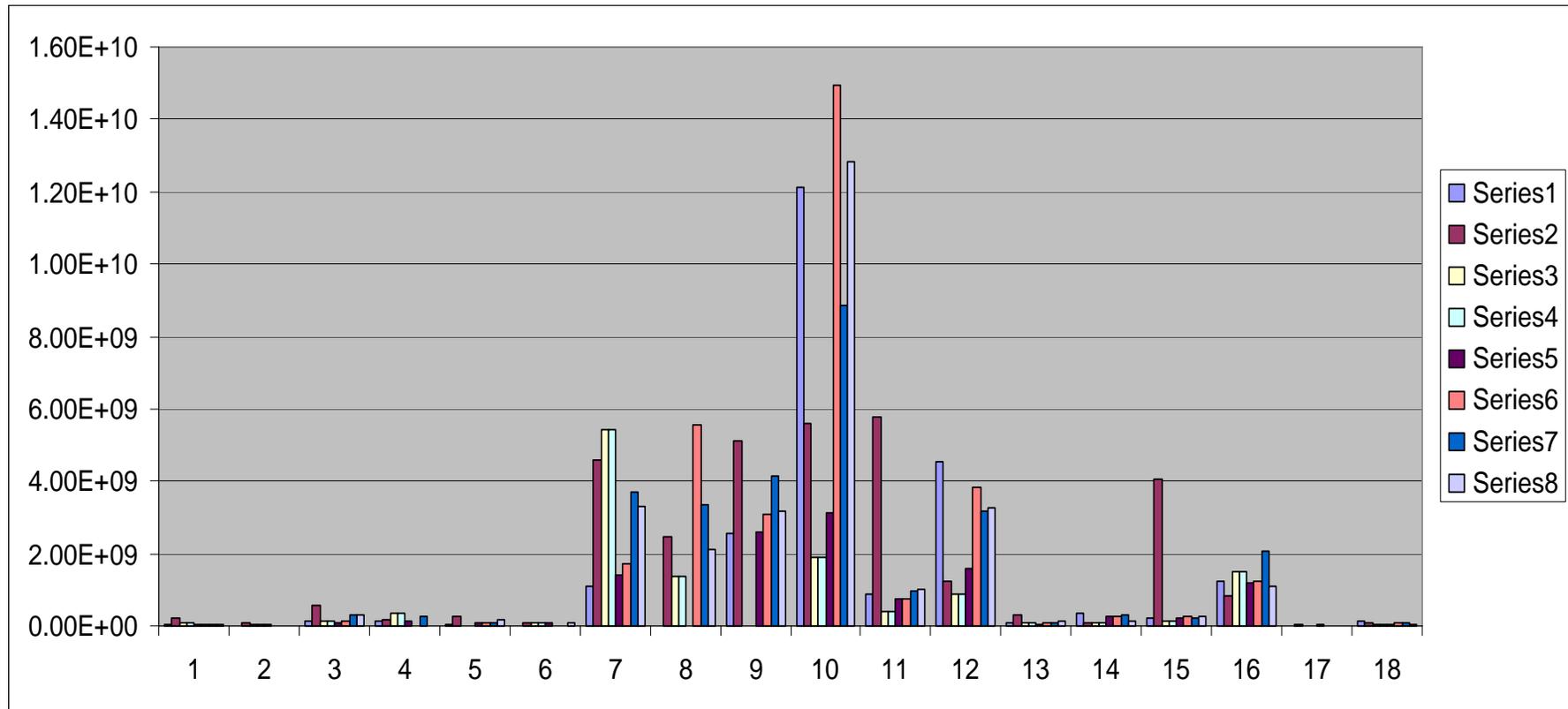
$(R/Q)Q_f$  [ $\Omega\text{MHz}$ ]





# 9-cell Cavities TM110 Dipole Modes: TTF Module 3

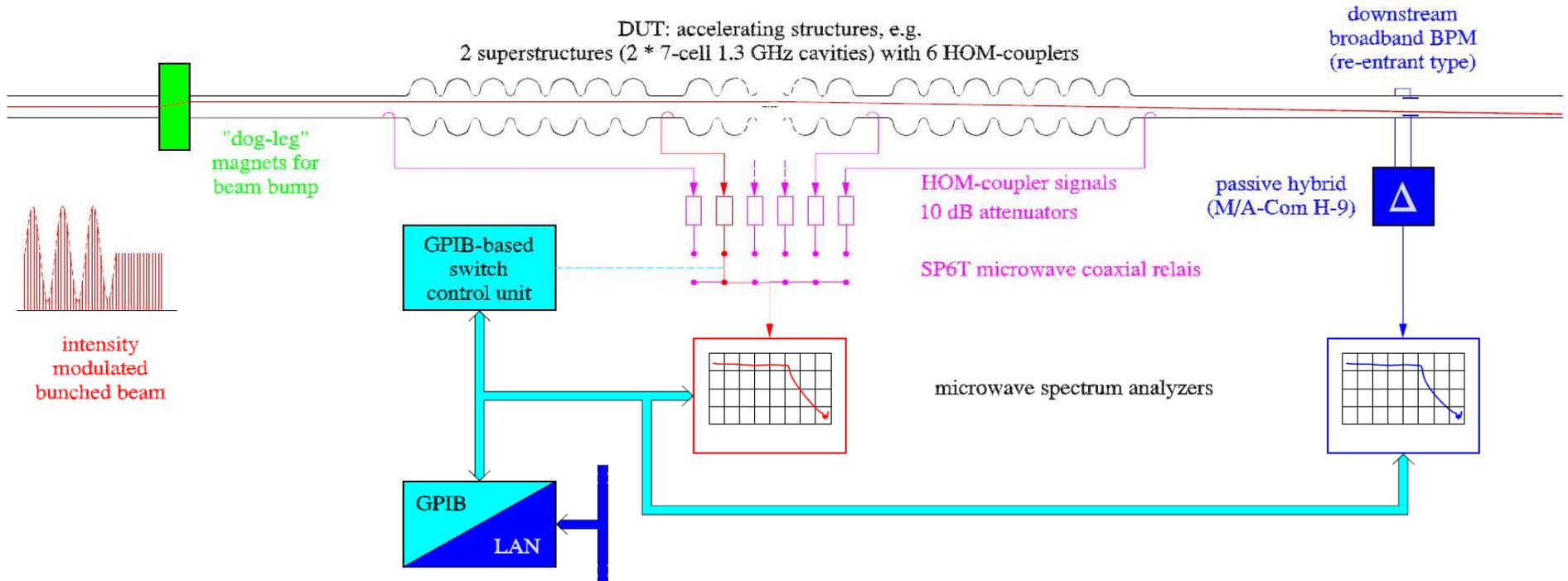
$(R/Q)Q_f$  [ $\Omega\text{MHz}$ ]



Mode #



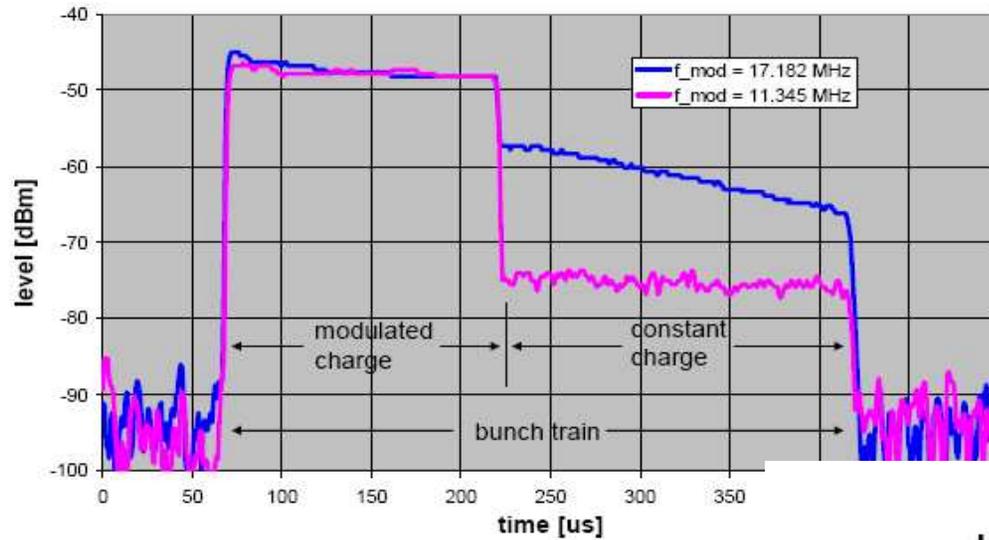
# Experimental Setup for Beam Based HOM Measurements at TTF/FLASH



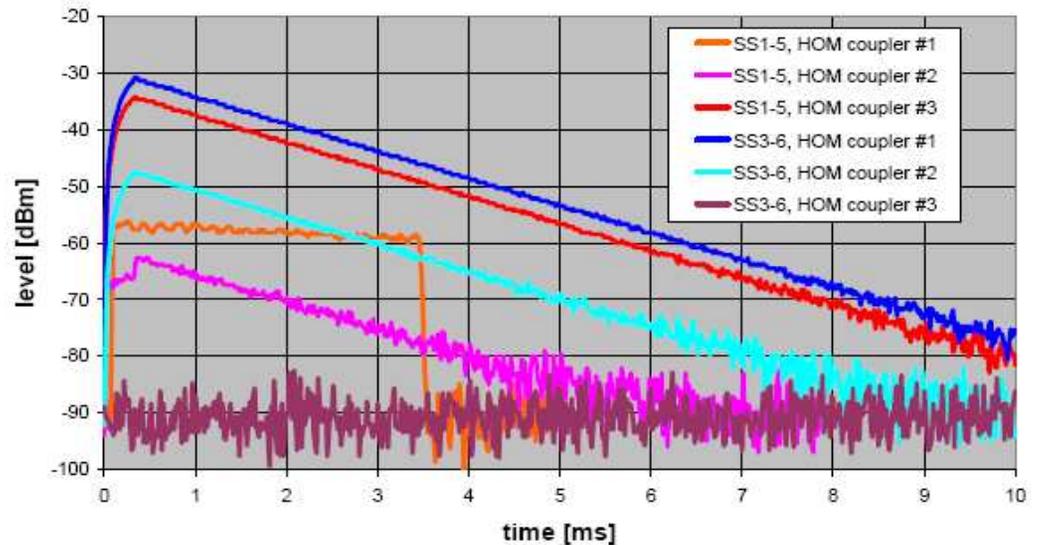


# Beam Based HOM Measurements at TTF/FLASH

## HOM Measurements: BPM Signals

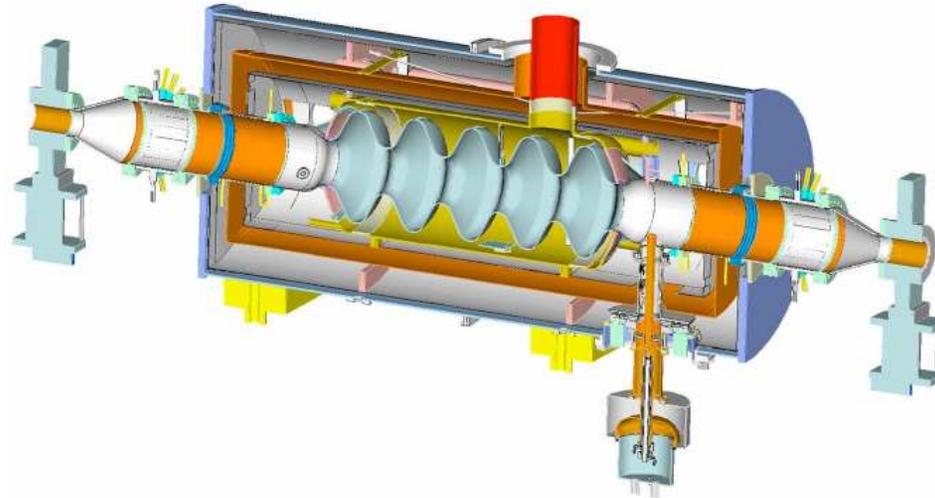


## HOM Measurements: HOM Coupler Signals at $f_{HOM} = 3076$ MHz

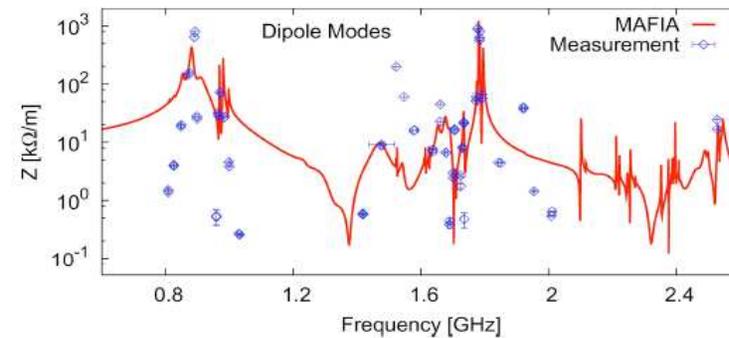
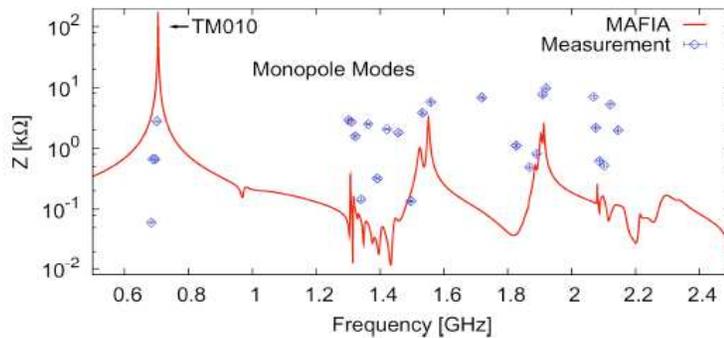




# Example 5: BNL ERL Cavity



BNL high current ERL cryomodule concept for electron cooling



Calculated and Measured HOM spectra. (See Rama Calaga's talk, this working group)



# Example 6: TJNAF 1A Cryomodule Design

FEL Ampere-class module draft specs.

Voltage	100-120 MV
Length	~10m
Frequency	750 MHz
Beam Aperture	>3"
BBU Threshold	>1A
HOM Q's	<10 <sup>4</sup>

JLab FEL proposal:



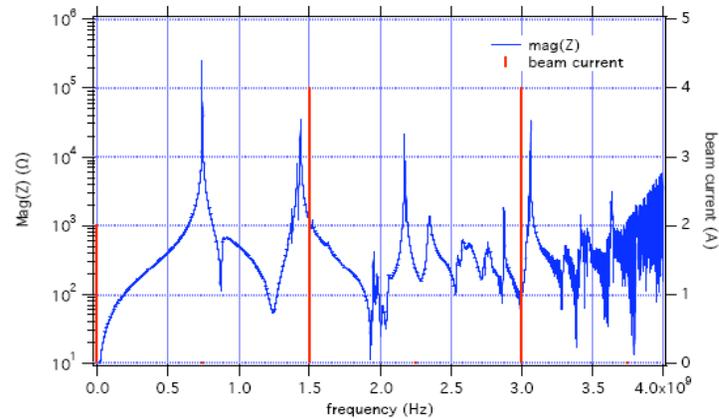
5-cell waveguide damped cavity



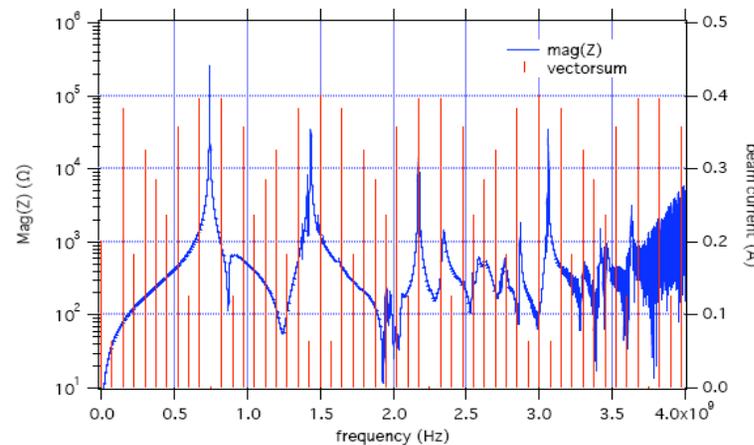
CEBAF cavity



# TJNAF 1A Cryomodule Design



Beam spectrum, 750 MHz, 1A 2 pass, 50.2m path length (~22 kW below cutoff)



Beam spectrum, 75 MHz, 100mA 2 pass, 50.2m path length (>5 kW below cutoff?)