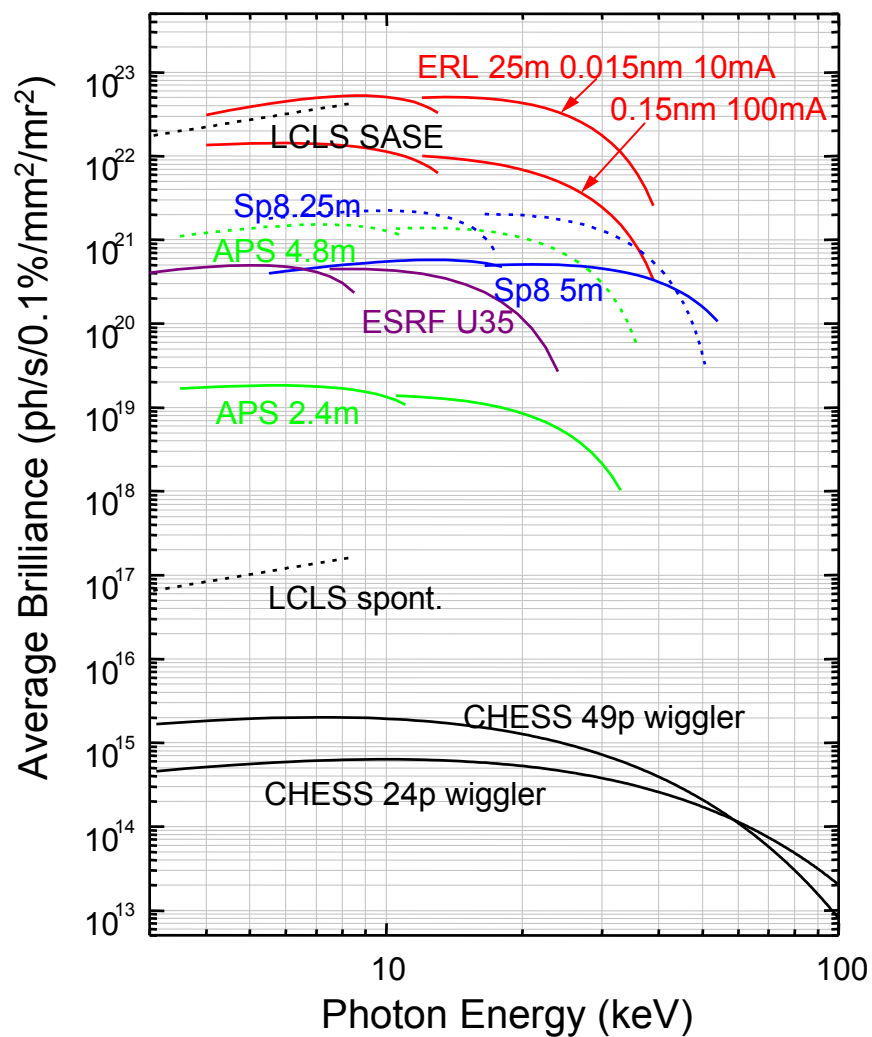
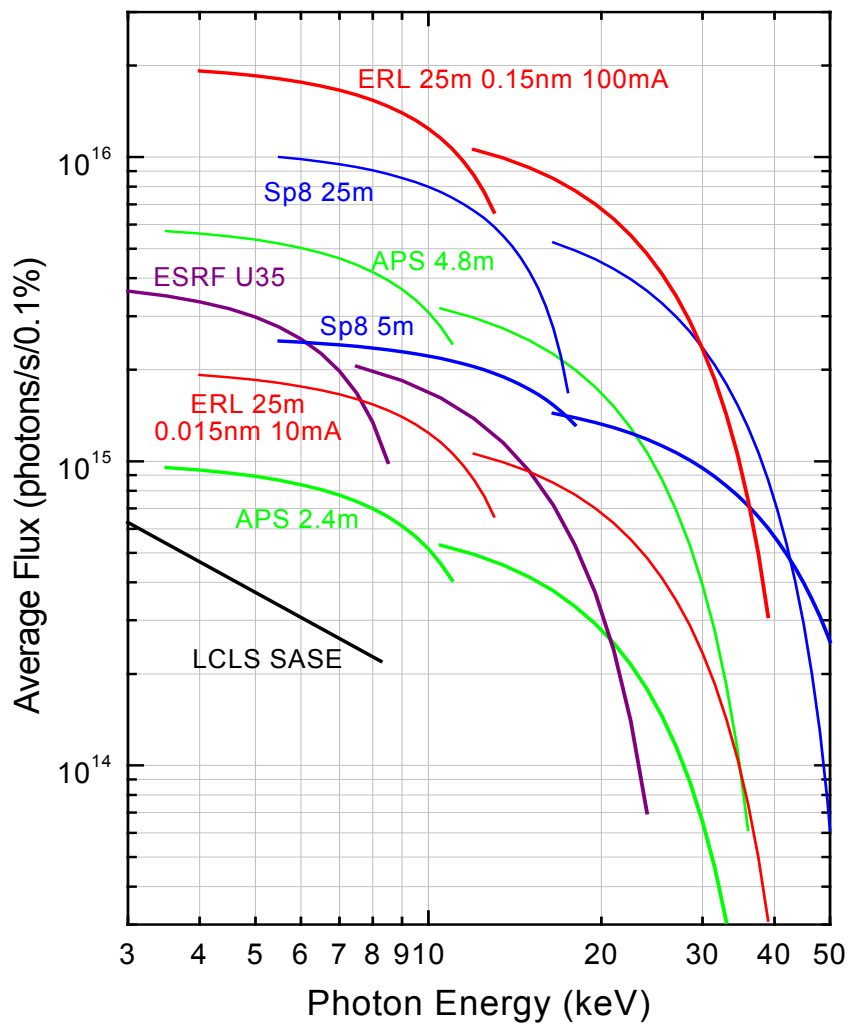


# Considering an ERL x-ray source based on double acceleration

# Considering an ERL x-ray source

# Outline

- Power crisis for ERL
- Optimizing for flux, brightness, brilliance
- Injector performance
- Layout of ERL x-ray source



# POWER BILL

## 20 MIW

# Estimates of ERL power

Refrigeration	.....	8.6 MW
Main linac rf power	.....	7.5 MW
Injector rf power	.....	2 MW
Magnet power supplies	.....	< 1 MW
<hr/>		
	Total:	19 MW

# Estimates of ERL power

Refrigeration	.....	8.6 MW	16 MW
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Magnet power supplies	.....	< 1 MW	
<hr/>			
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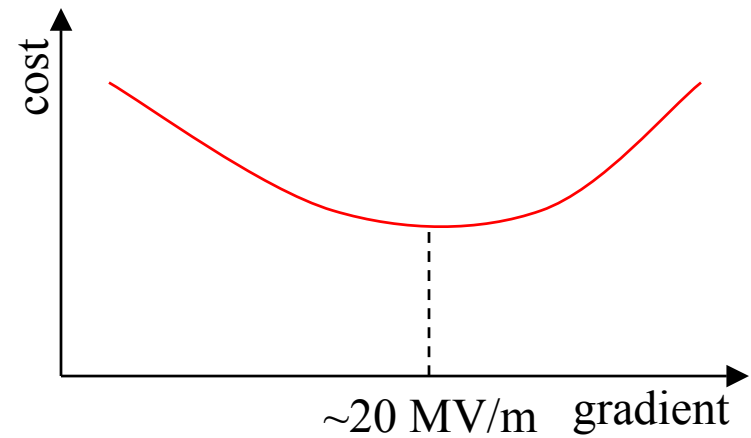
Note: this is not a pessimistic number



# Big ticket item: 5 GeV linac

Reduce the power by

a) lowering the gradient (works if cavities are cheap)



b) going multipass

# Going multipass

# Going multipass

- Need half the linac
  - ✓ linac cost
  - ✓ power ( $\sim 9$  MW)

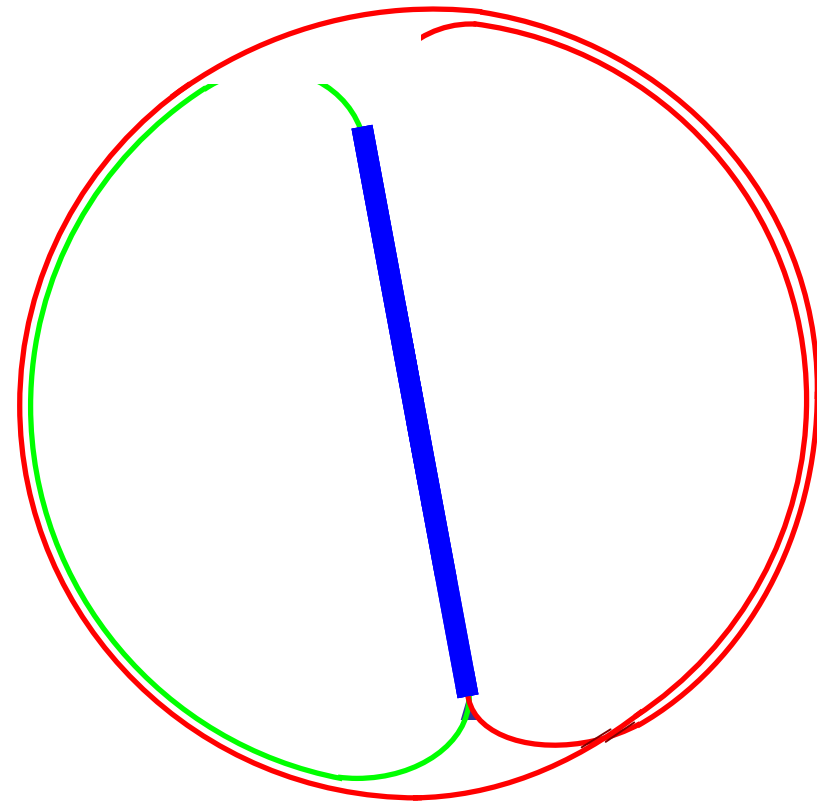
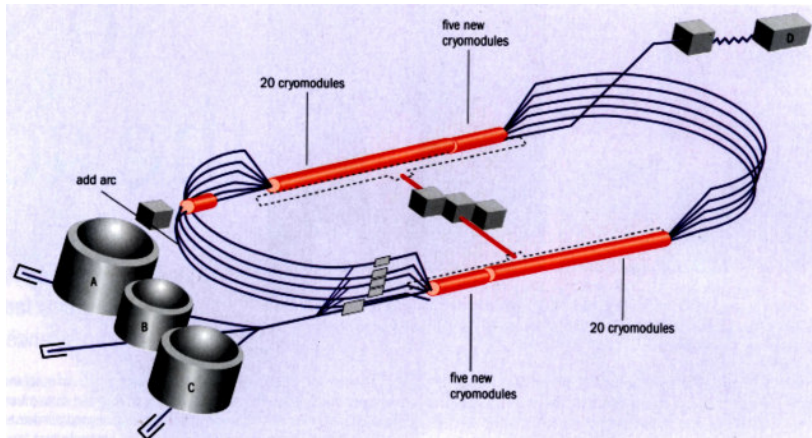
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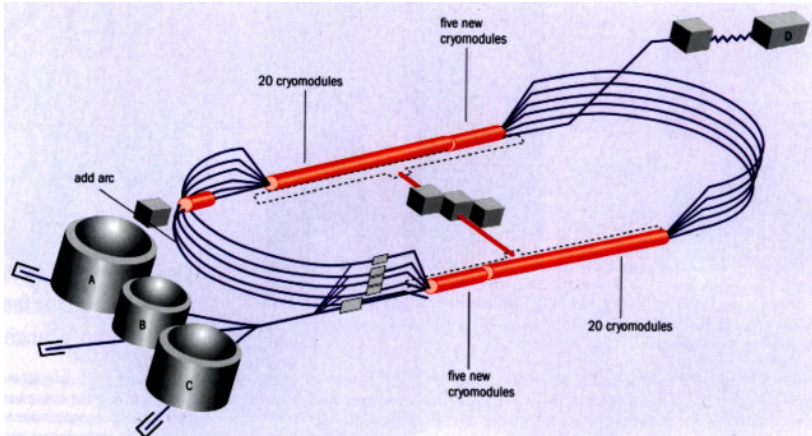
# Going multipass

- Need half the linac
  - ✓ linac cost
  - ✓ power ( $\sim 9$  MW)
- BBU is currently limited to  $\sim 20$  mA
- Beam current in linac would be 400 mA (difficult even for storage rings), e.g. beam induced losses would go up by a factor of 4

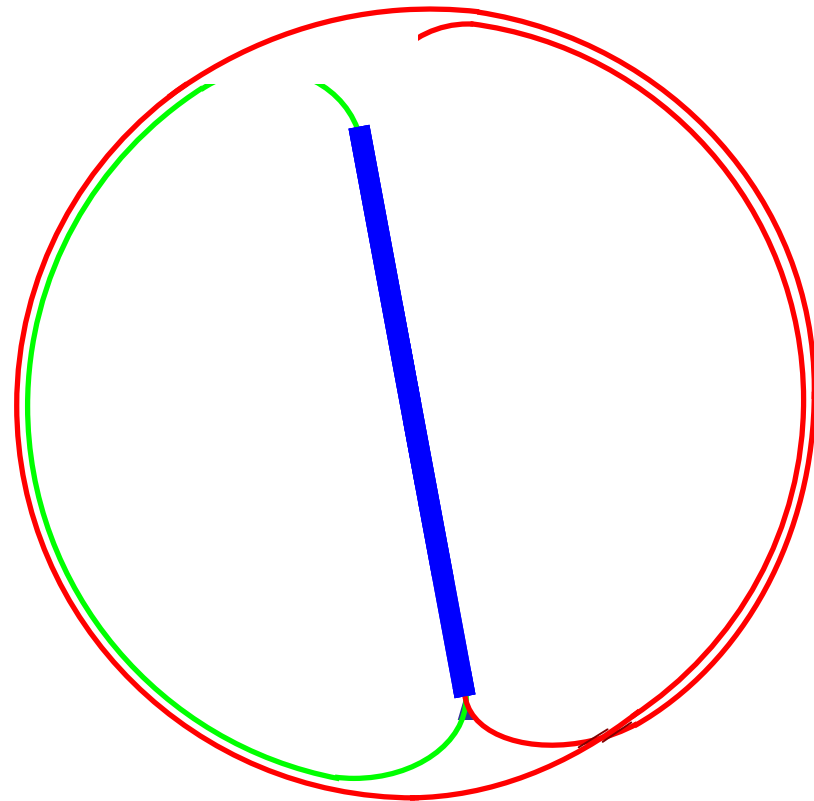
# Multipass configuration



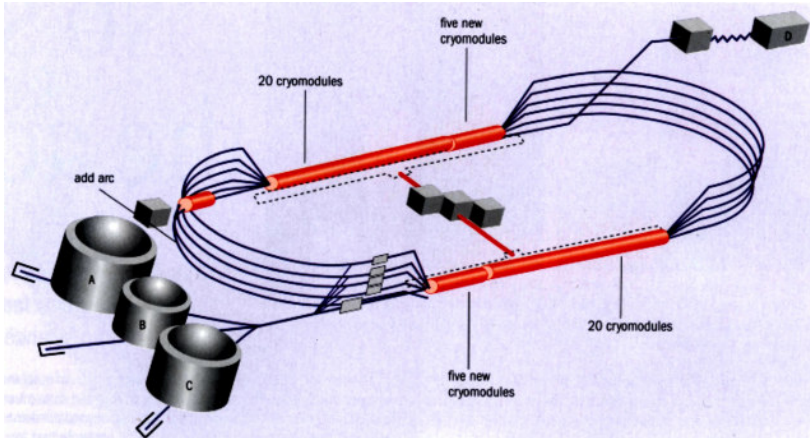
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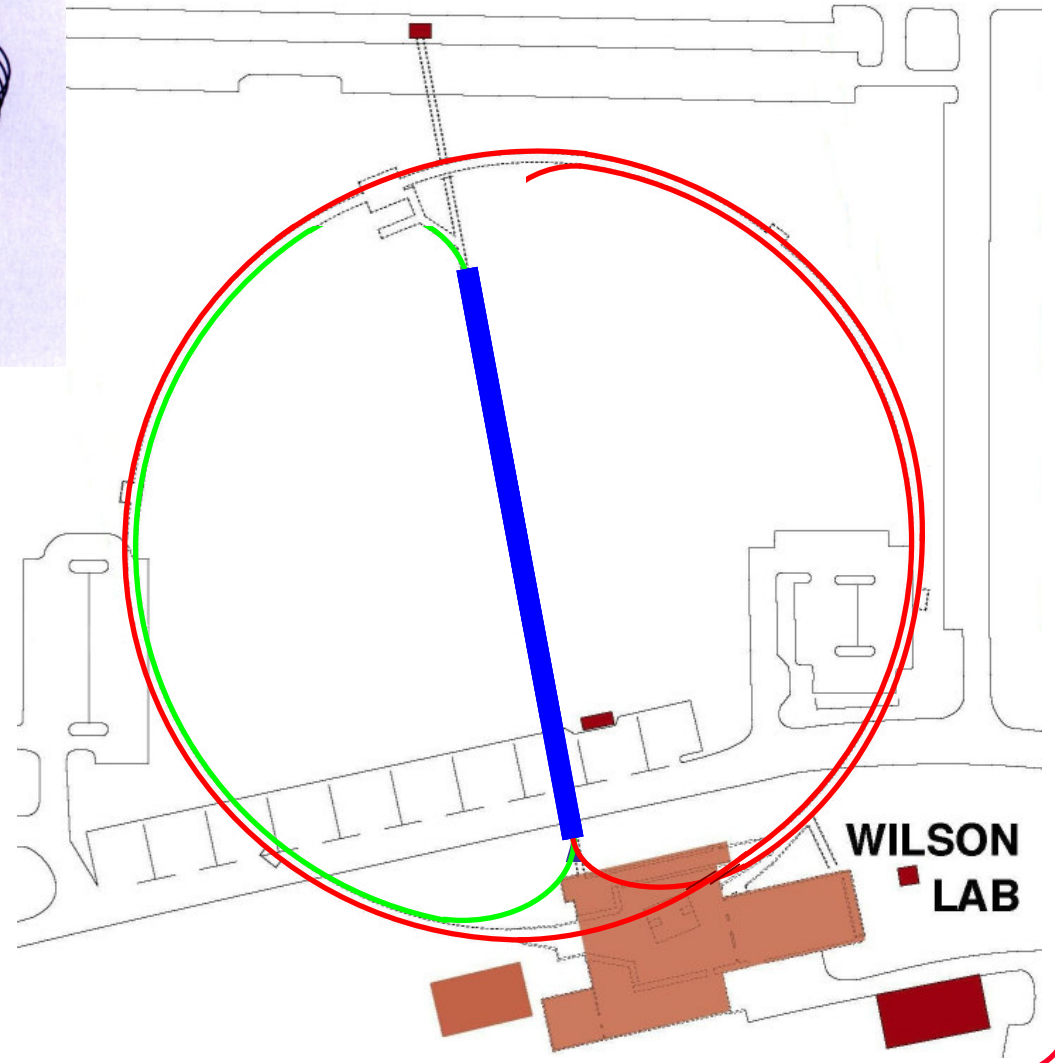
200  $\mu$ A only. Each energy has its own arc.



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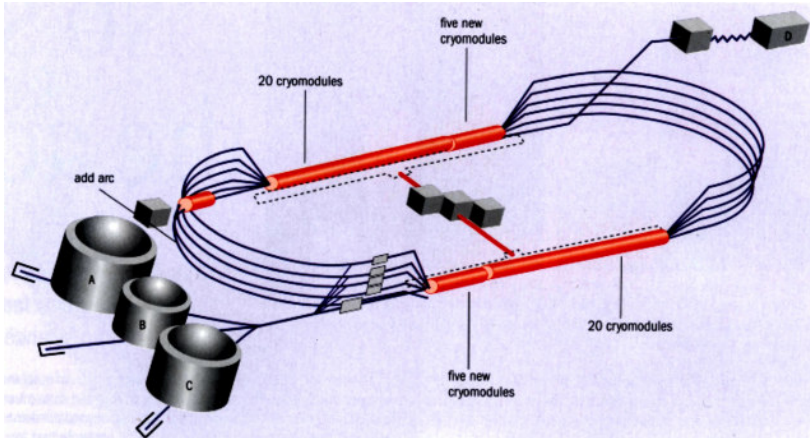


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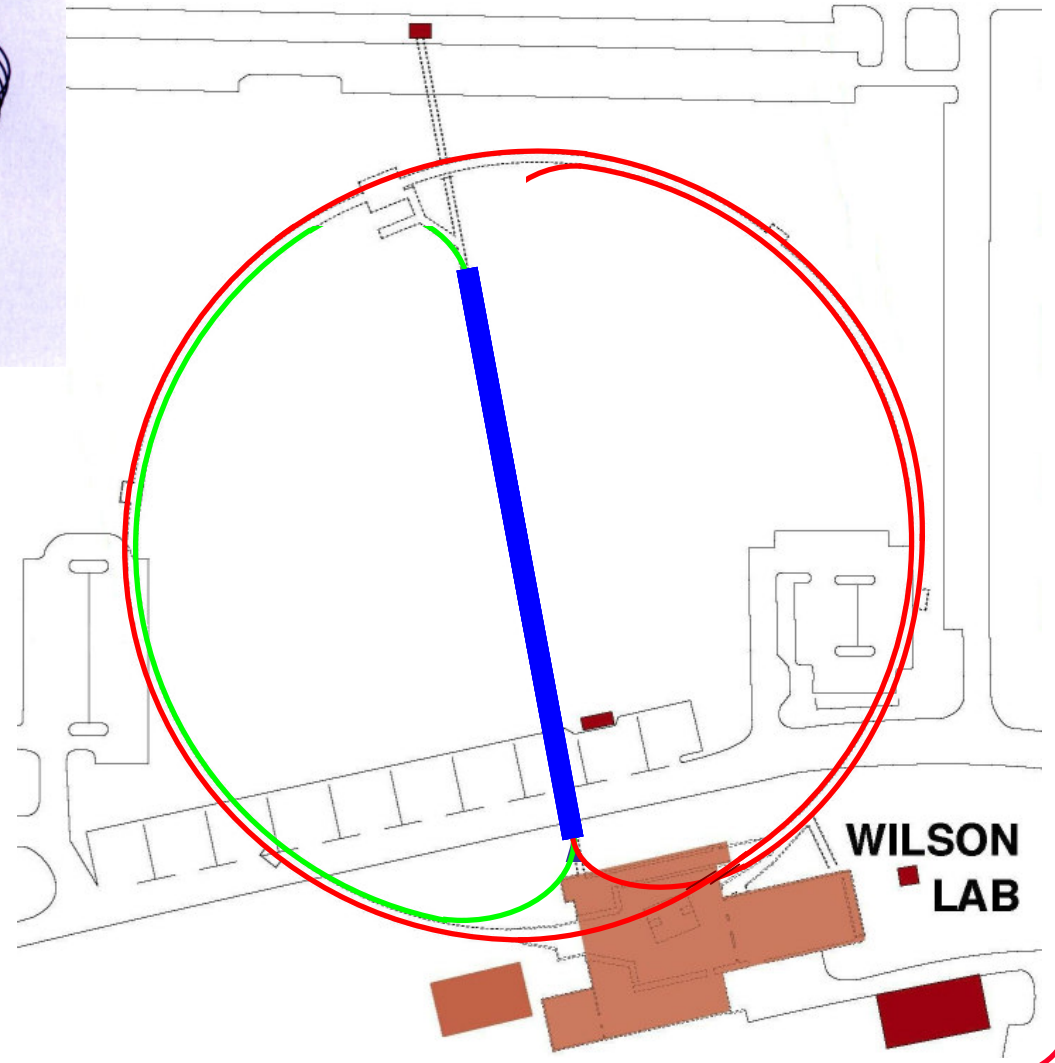




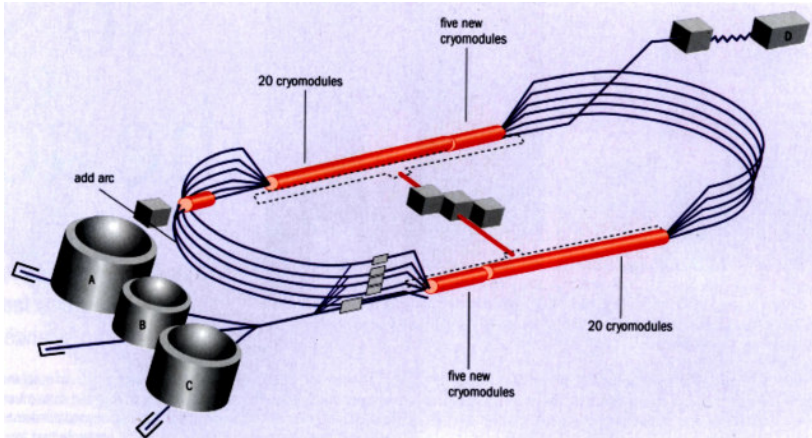
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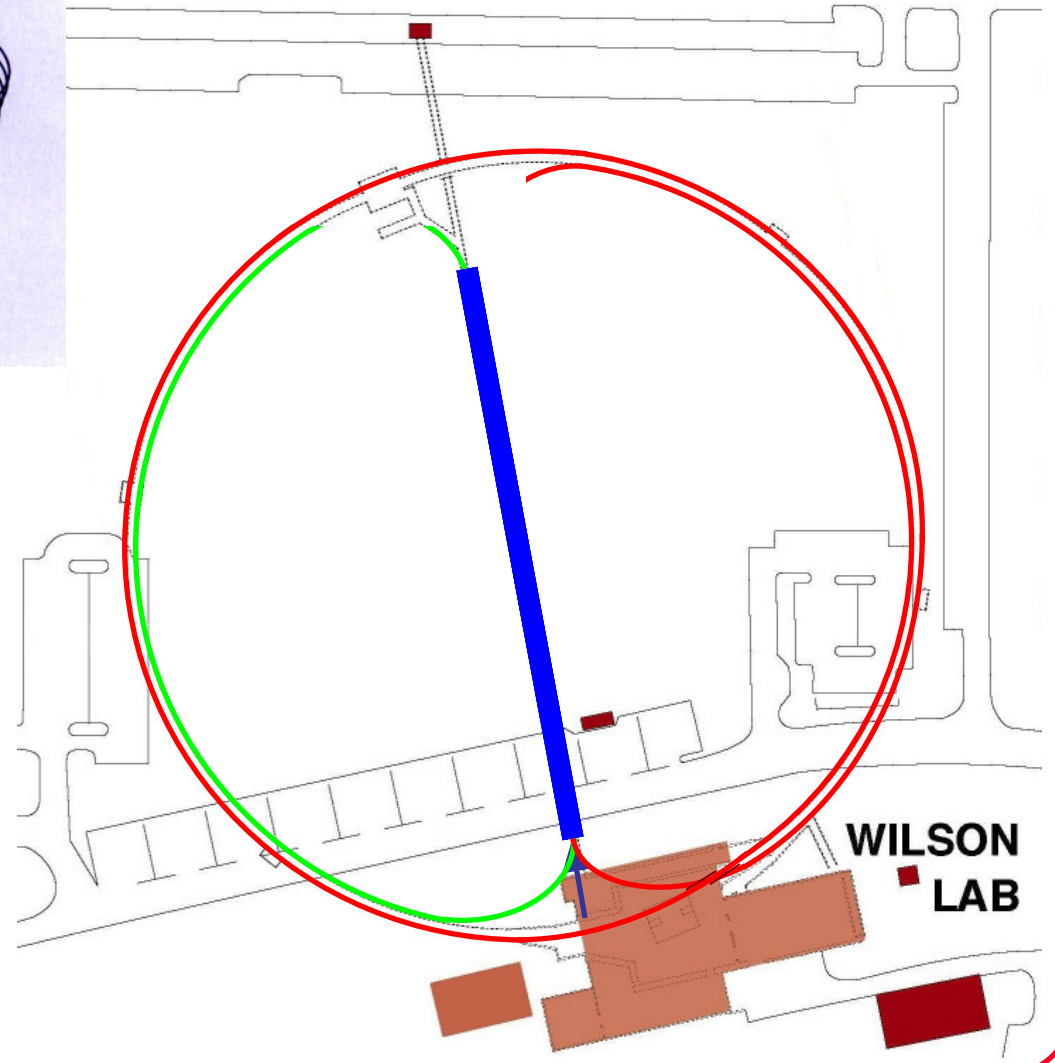
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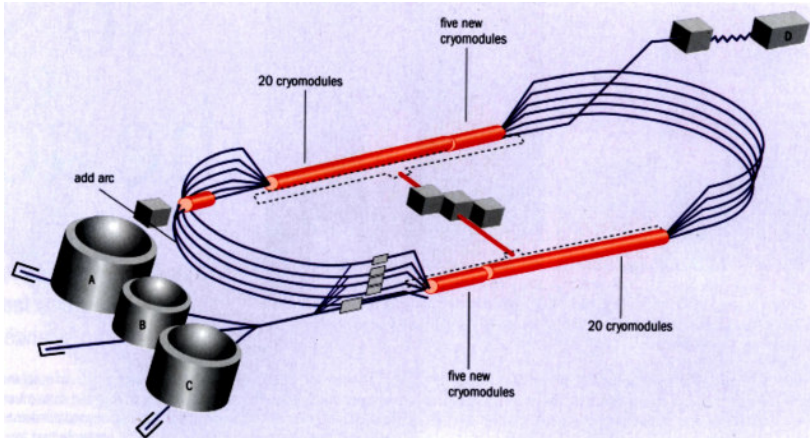
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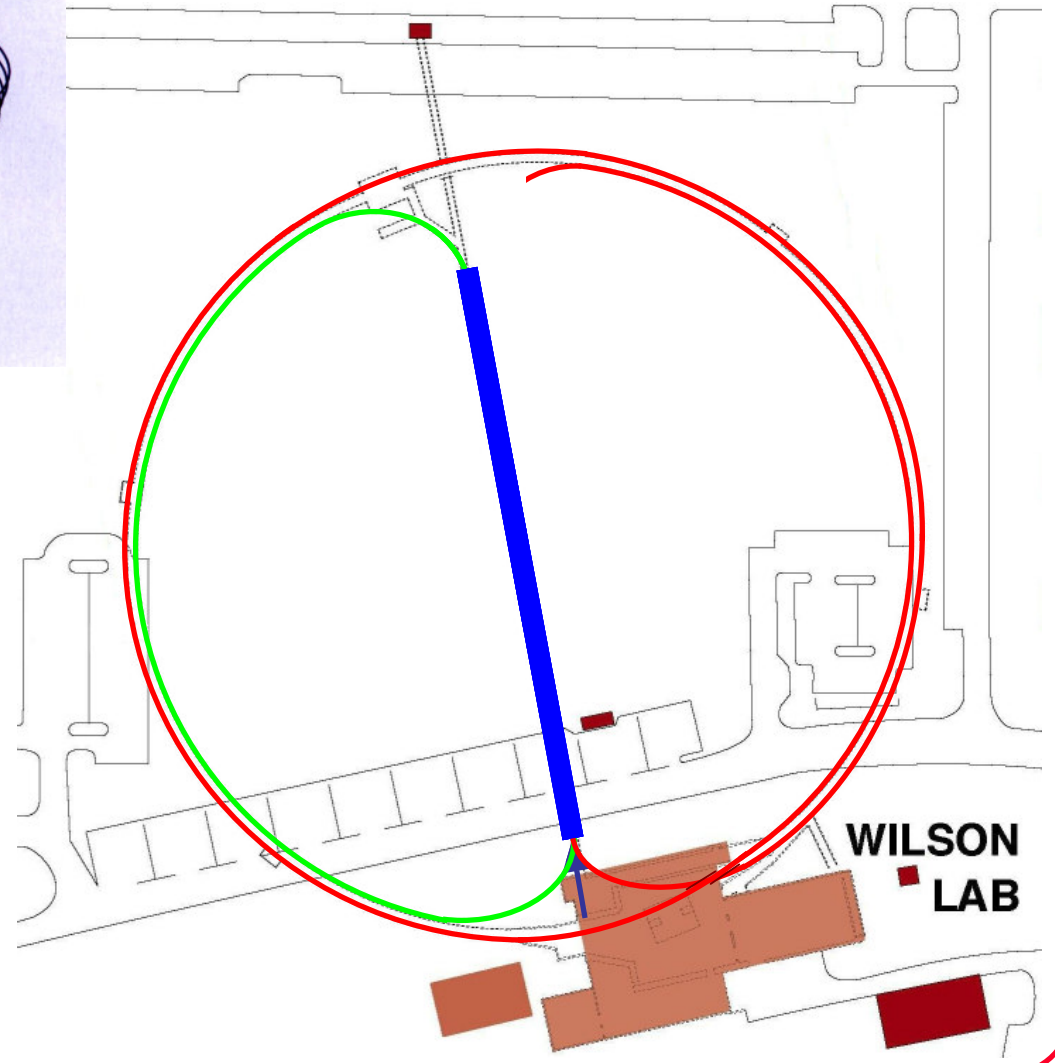
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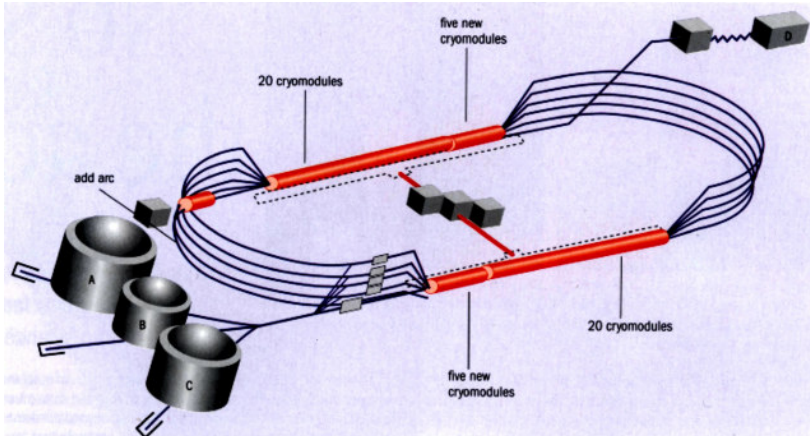
# Multipass configuration



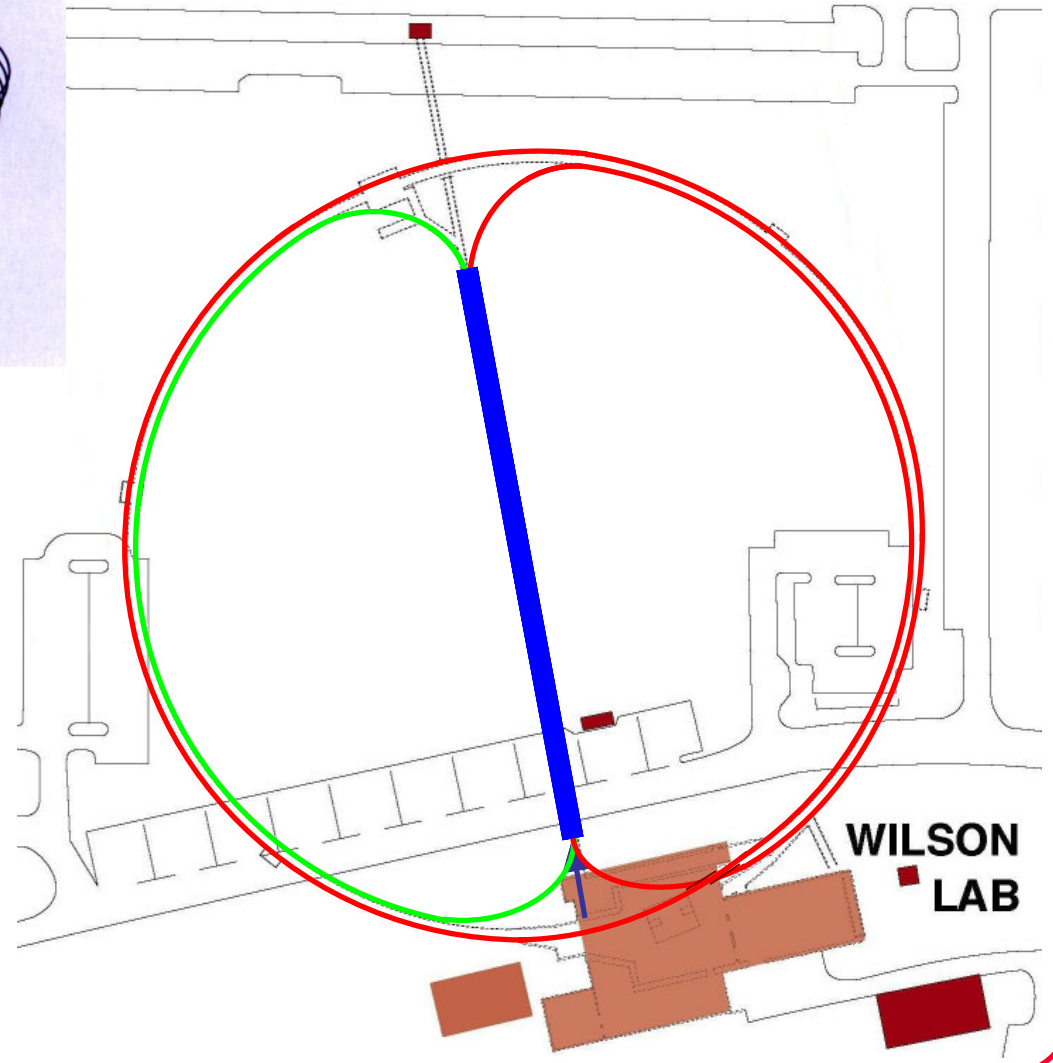
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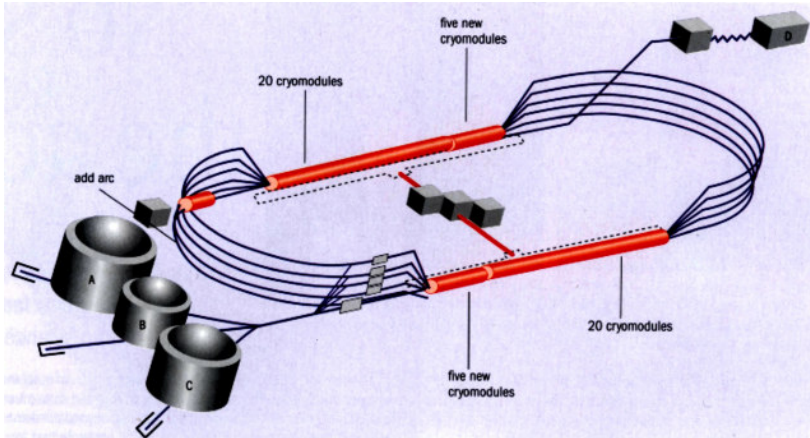
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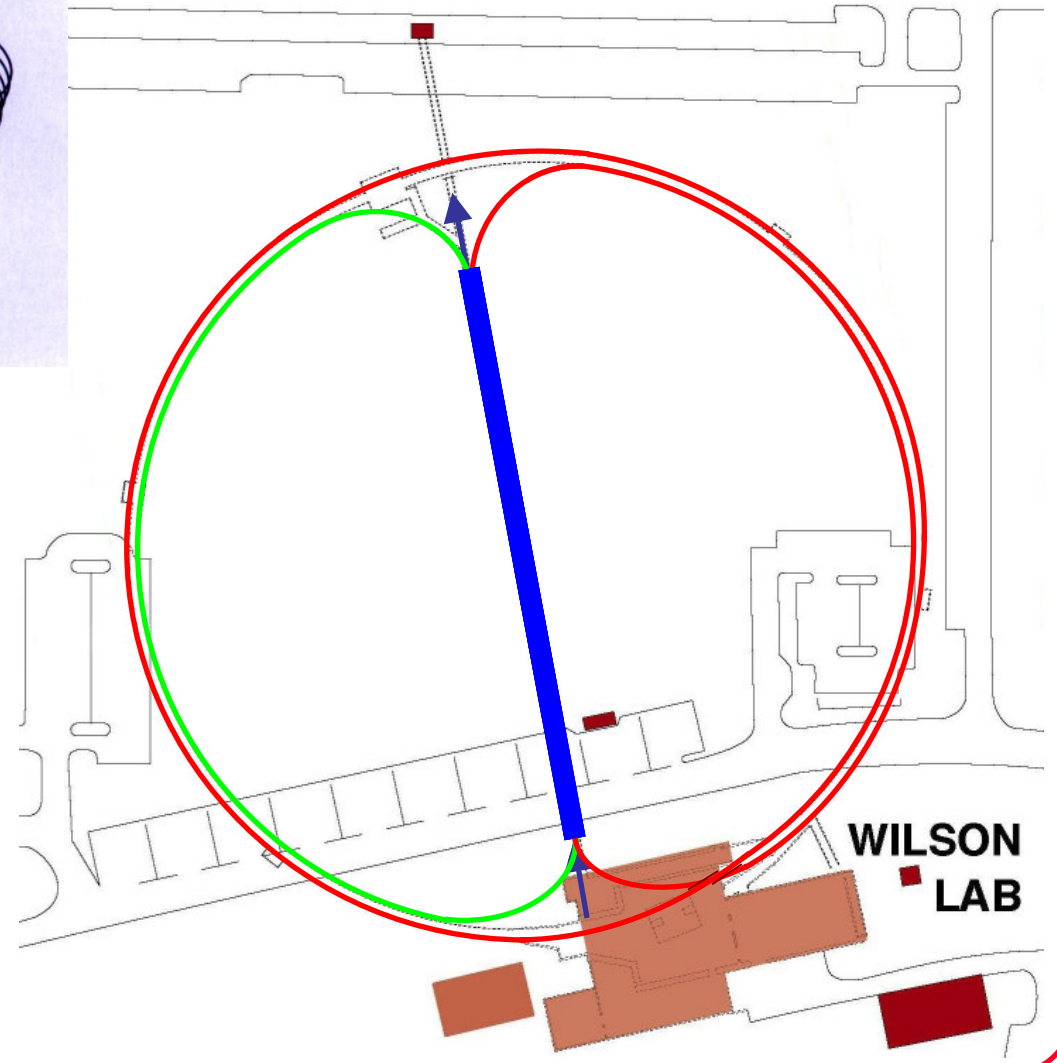
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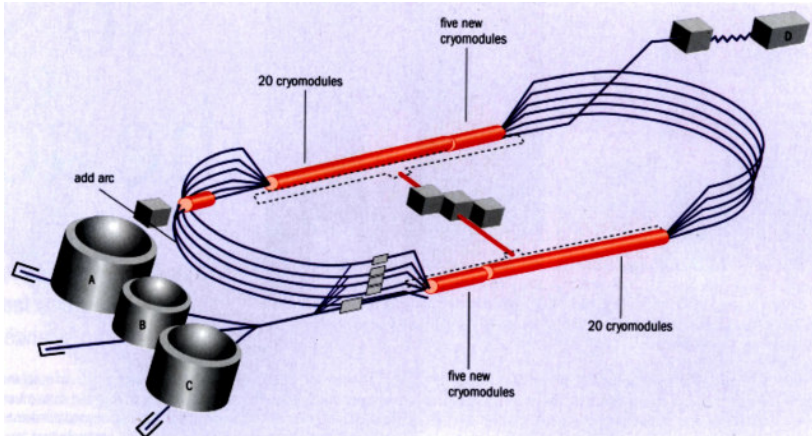
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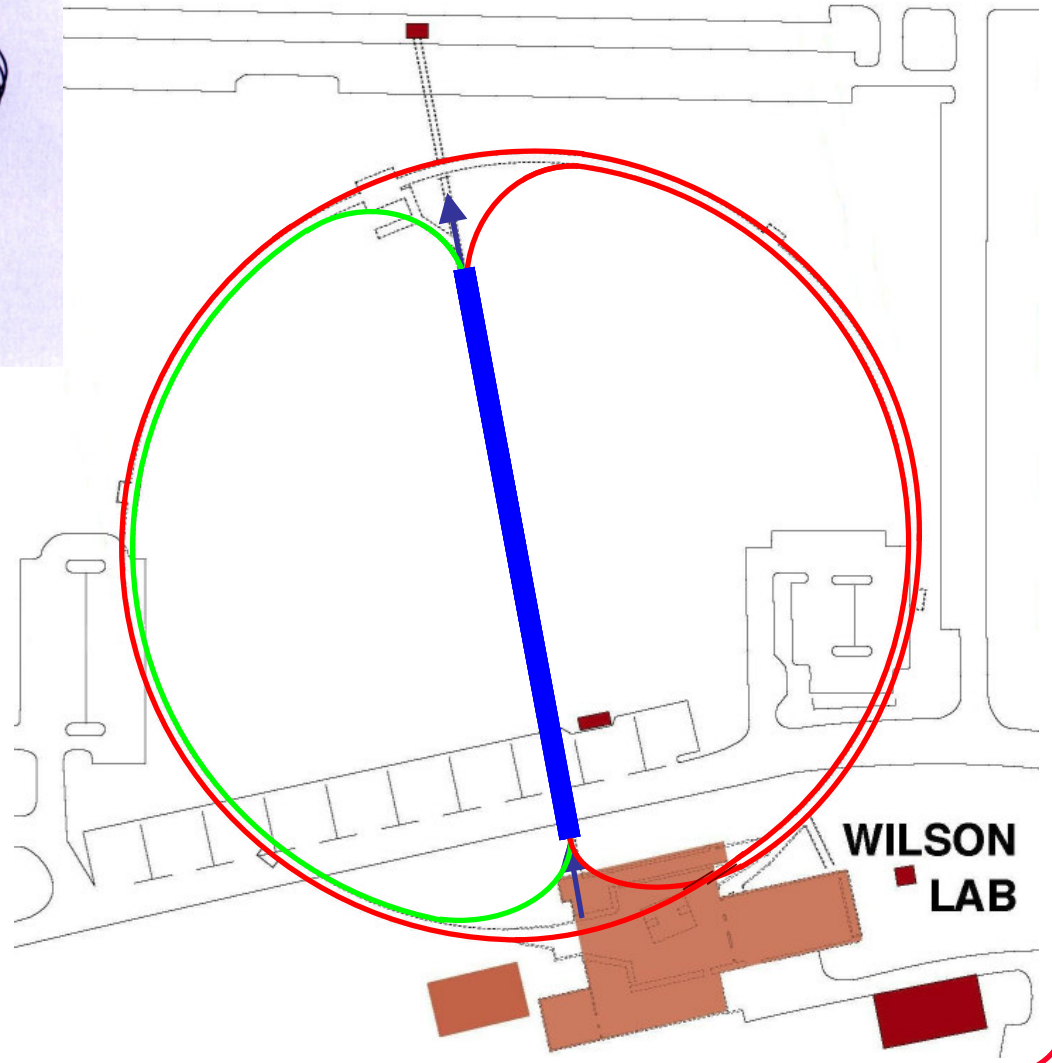


# Multipass configuration



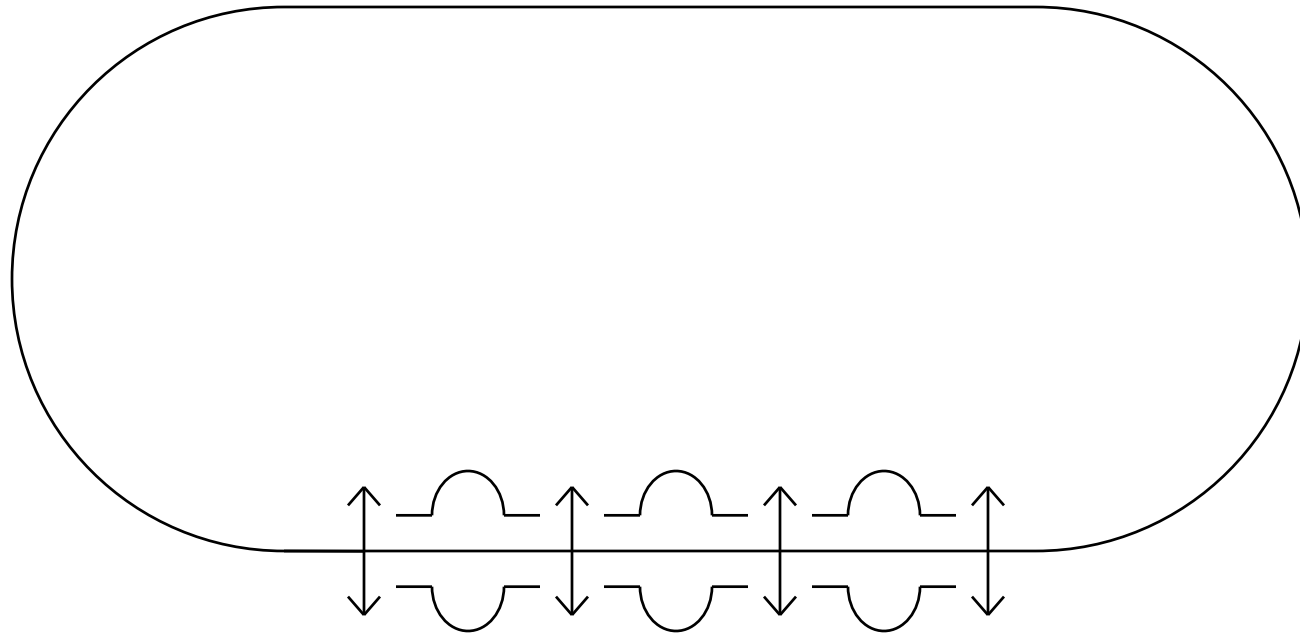
200  $\mu$ A only. Each energy has its own arc.

With 400 mA in linac, such machine is more vulnerable to **BBU**



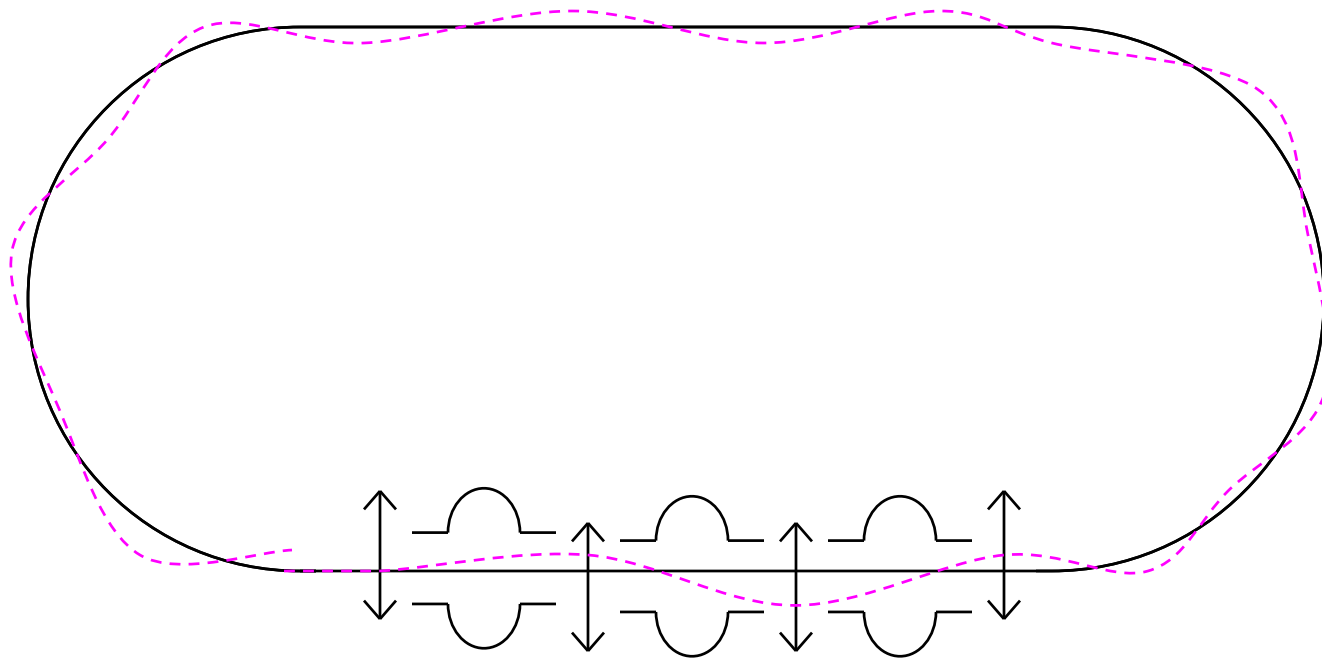
# Multipass beam breakup

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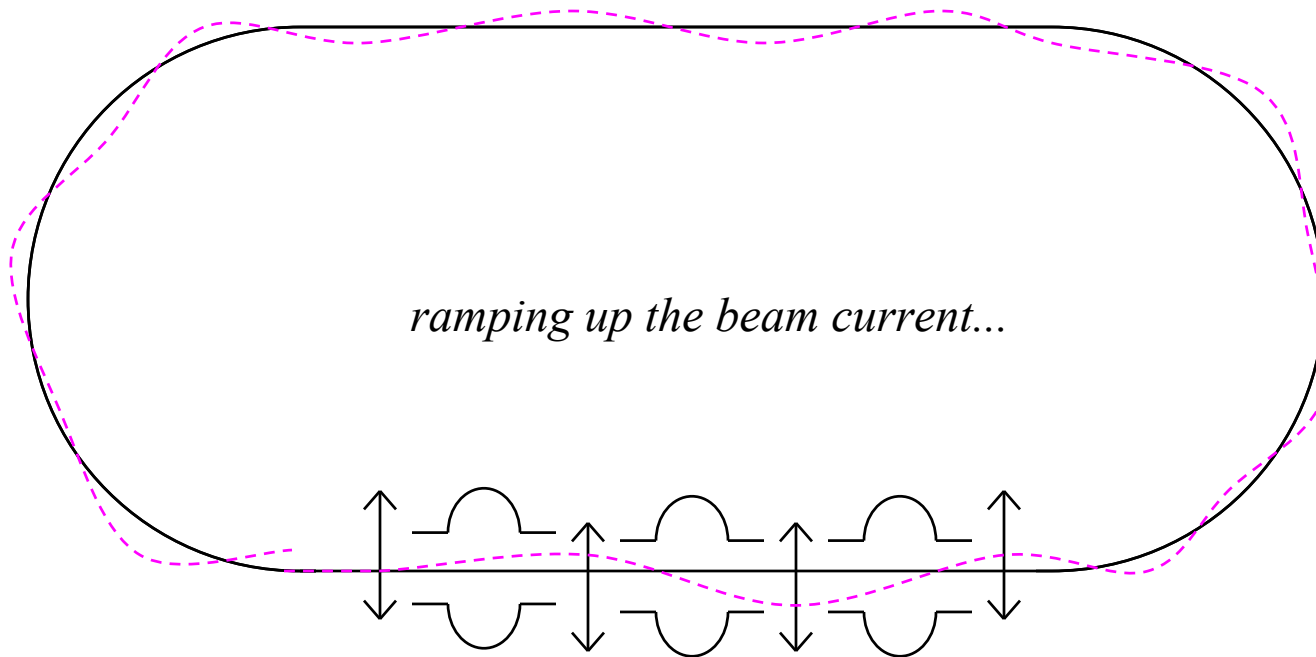




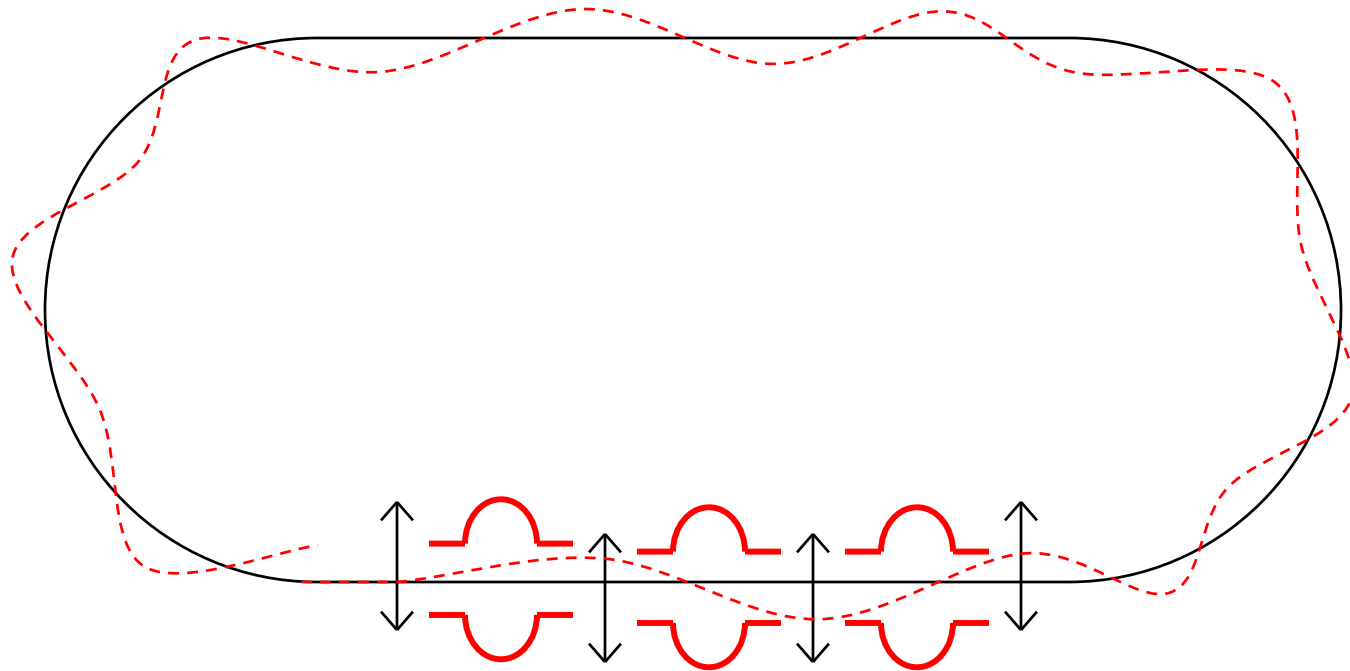
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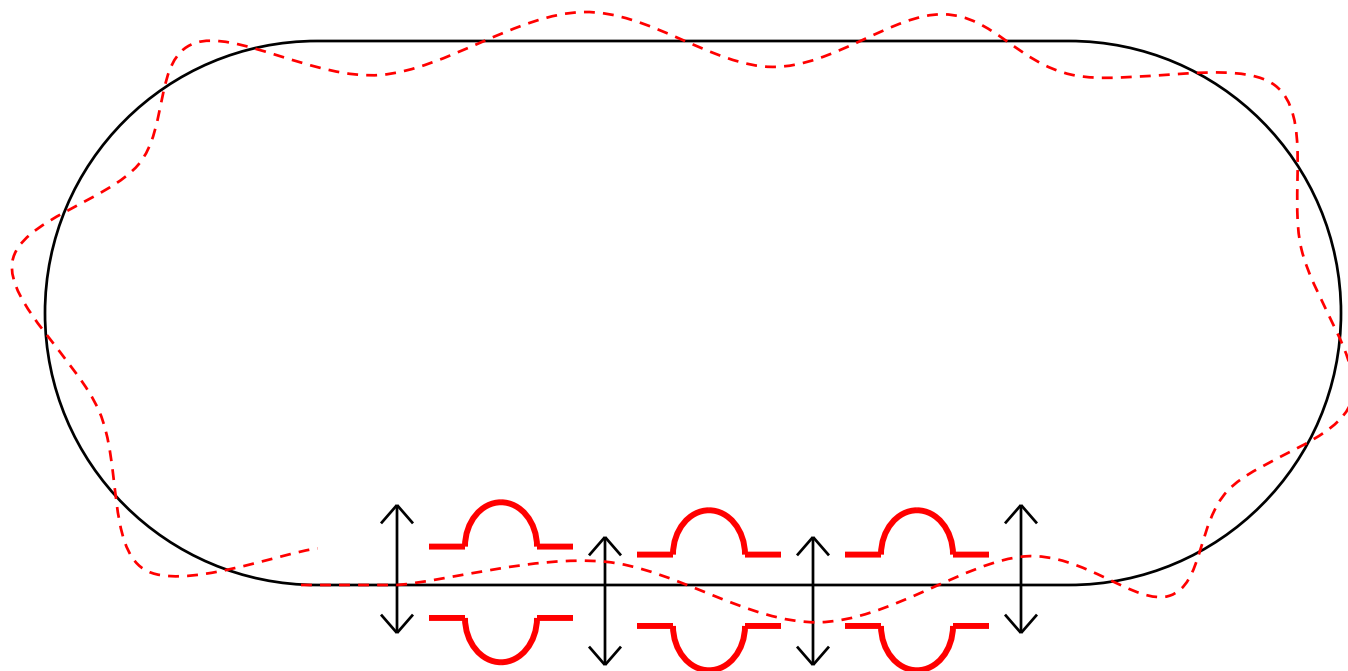
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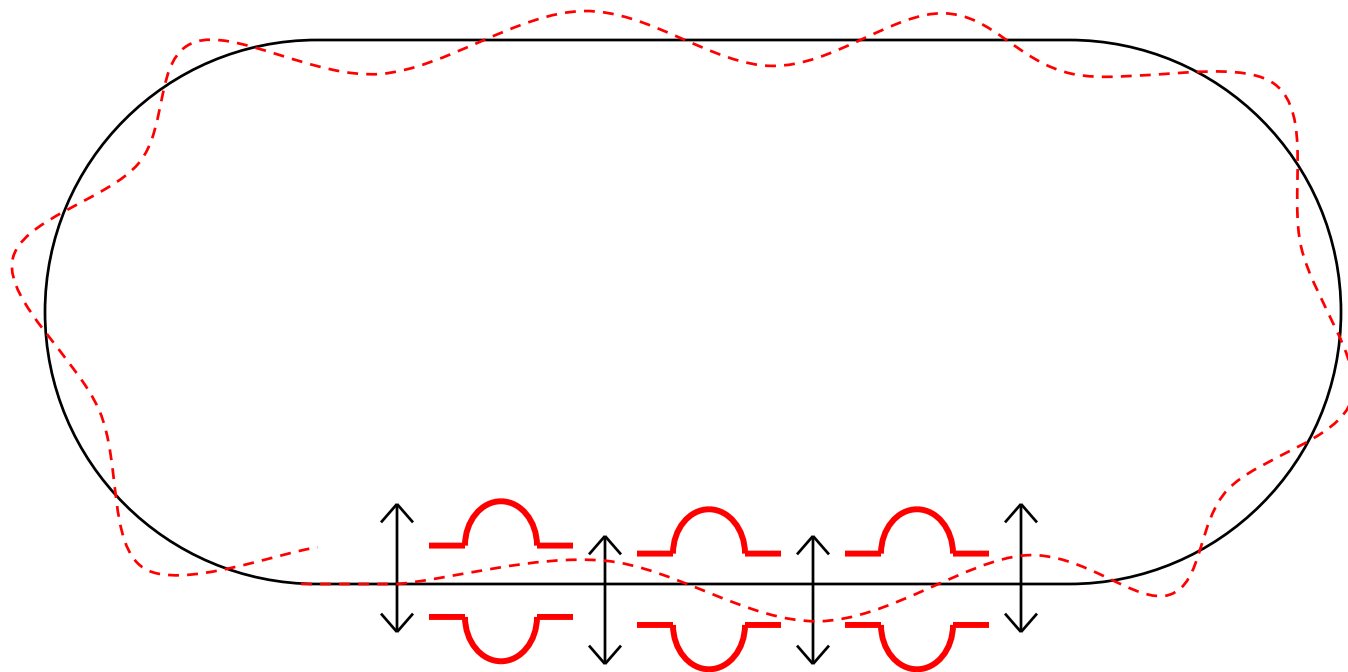


# Multipass beam breakup



- higher order mode damping
- recirculating optics
- injection energy

# Multipass beam breakup



threshold  
current



- higher order mode damping
- recirculating optics
- injection energy

# BBU in two-pass ERL: gruesome look

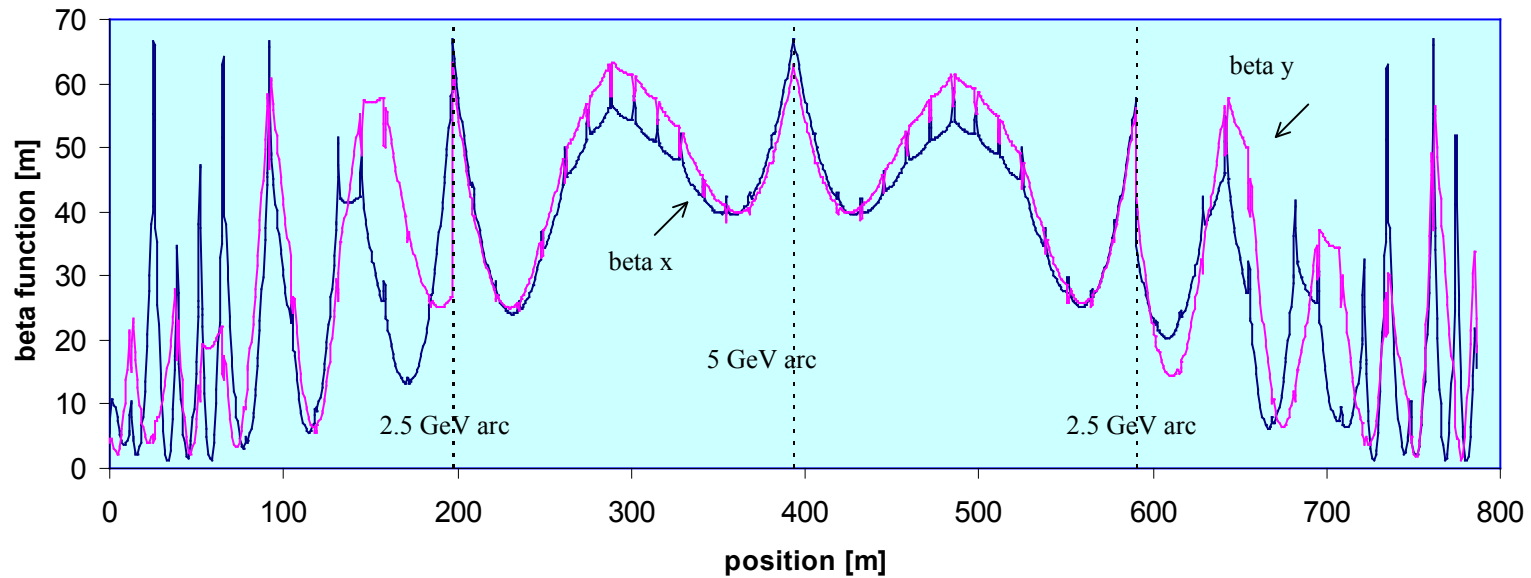


Table 1.  
Results of TDBBU runs for 1-pass and 2-pass 5 GeV ERL.  
HOM table (TESLA TDR 03/2001)

f (MHz)	R/Q (Ohm)	Q	(R/Q)*Q	1-pass 5 GeV ERL BBU (mA)	2-pass 5 GeV ERL BBU (mA) Q*	Improved by a factor of
1699	88.40	5.00E+04	4.42E+06	160	20 8.00E+02	62.5
1873	56.39	7.00E+04	3.95E+06	190	25 1.30E+03	53.8
2575	51.50	5.00E+04	2.57E+06	115	15 9.00E+02	55.6
1725	118.64	2.00E+04	2.37E+06	135	15 5.00E+02	40.0
1864	42.84	5.00E+04	2.14E+06	> 200	40 2.00E+03	25.0
1880	11.08	1.00E+05	1.11E+06	> 200	90 8.00E+04	1.3
...	...	...	...	> 200	> 100	

\* BBU th  $\geq$  100 mA

Trapped in  $\sim 20$  MW ERL?

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**Suggestion: drop the average current ( $\sim 30$  mA)  
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Cons: lower flux per meter of insertion device

Maxim time

**Never trade flux for brilliance**

Maxim time

**Never say “never”**

# Flux: how many bulbs does it take?





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**FLUX**

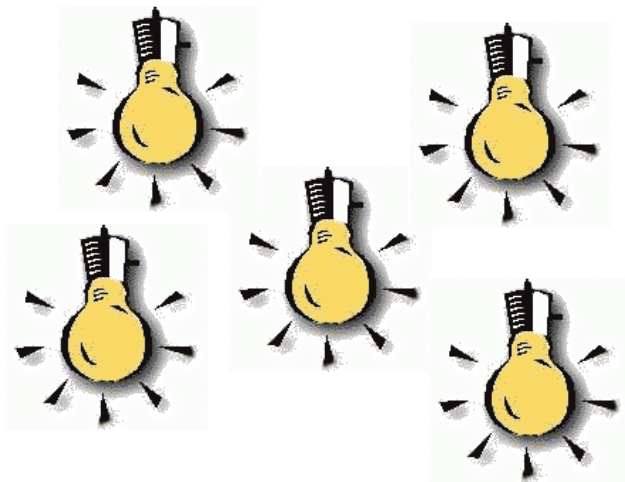


**BRILLIANCE**

# Flux: how many bulbs does it take?



**$N \times \text{FLUX}$**



**BRILLIANCE**

# Naïve scaling for ERL x-ray source

If source is completely dominated by e<sup>-</sup>-beam

Flux	ph/s/0.1%bw	$\propto I$
Brightness	ph/s/mrad <sup>2</sup> /0.1%bw	$\propto I / \epsilon$
Brilliance	ph/s/mm <sup>2</sup> /mrad <sup>2</sup> /0.1%bw	$\propto I / \epsilon^2$

*assuming*  $\epsilon \propto q$

$$F \propto I \quad dF / d\Omega \propto \text{const} \quad B \propto 1 / I$$

If near the diffraction limit, it's current that matters

# Beam matching & energy spread effect

$$\frac{dF_n}{d\Omega} = \frac{F_n}{2\pi\sqrt{\sigma_{cen}'^2 + \sigma_{x'}^2}\sqrt{\sigma_{cen}'^2 + \sigma_{y'}^2}}$$

*optimizing brilliance*

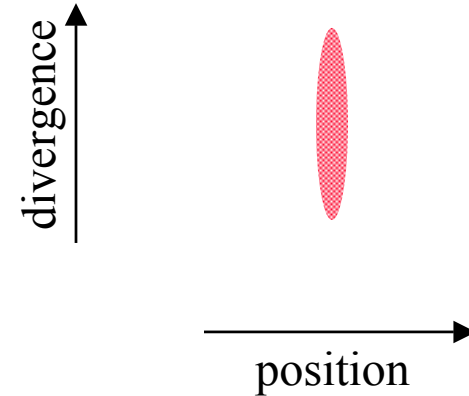
divergence ↑

→ position

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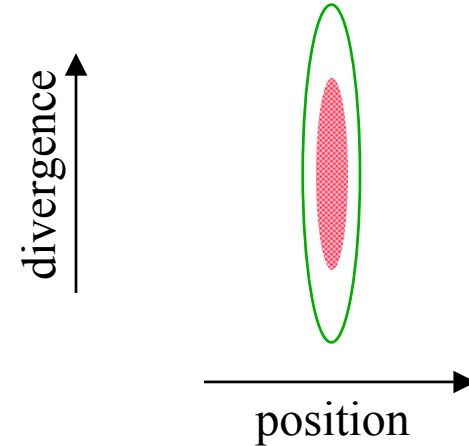
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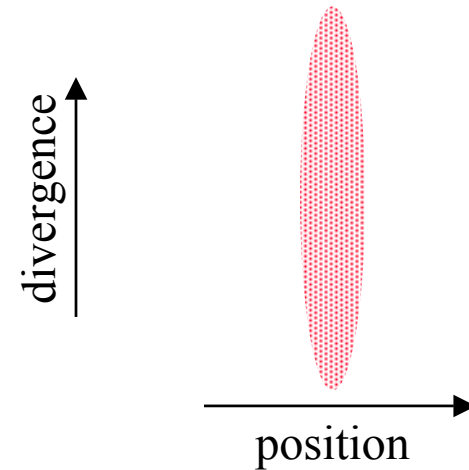
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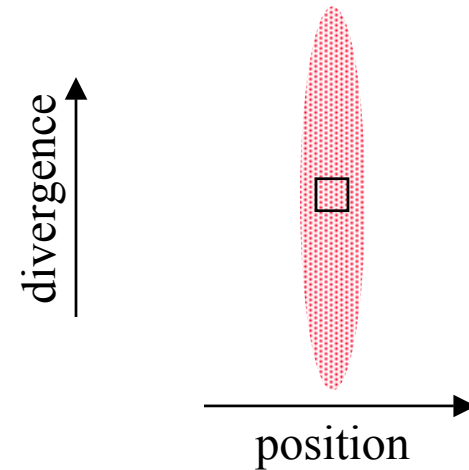
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*optimizing brightness*

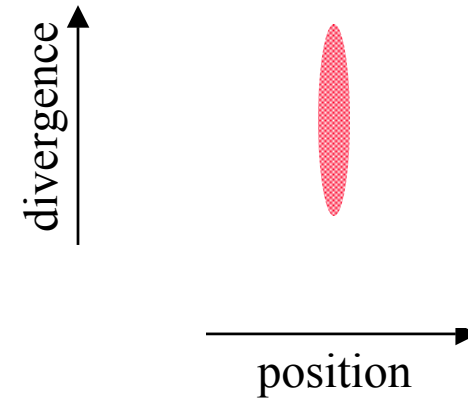
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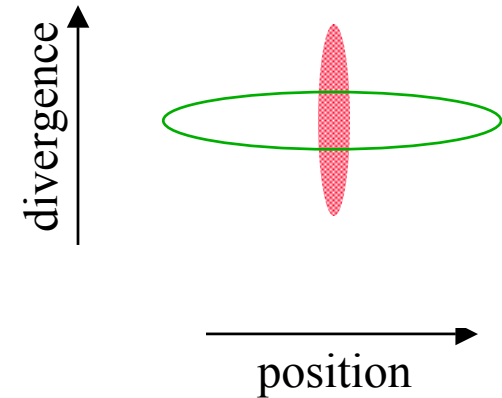
*optimizing brightness*



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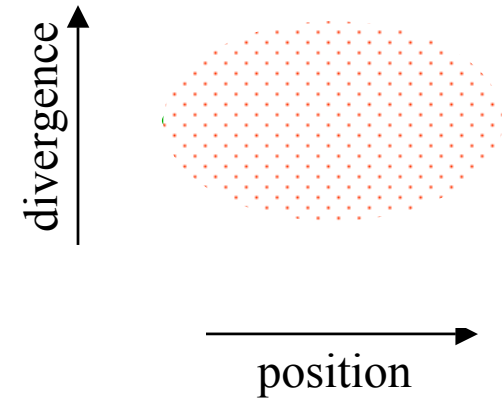
*optimizing brightness*



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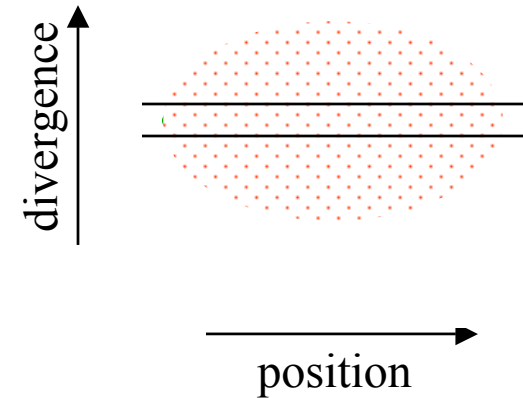
*optimizing brightness*



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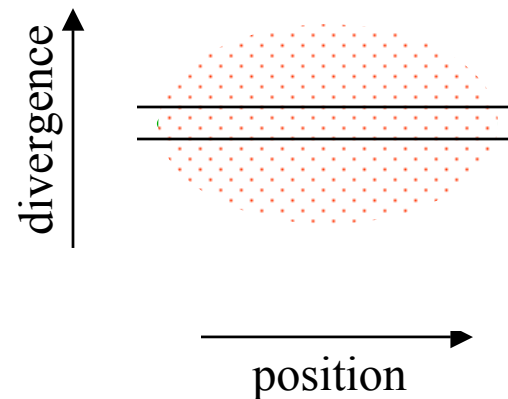
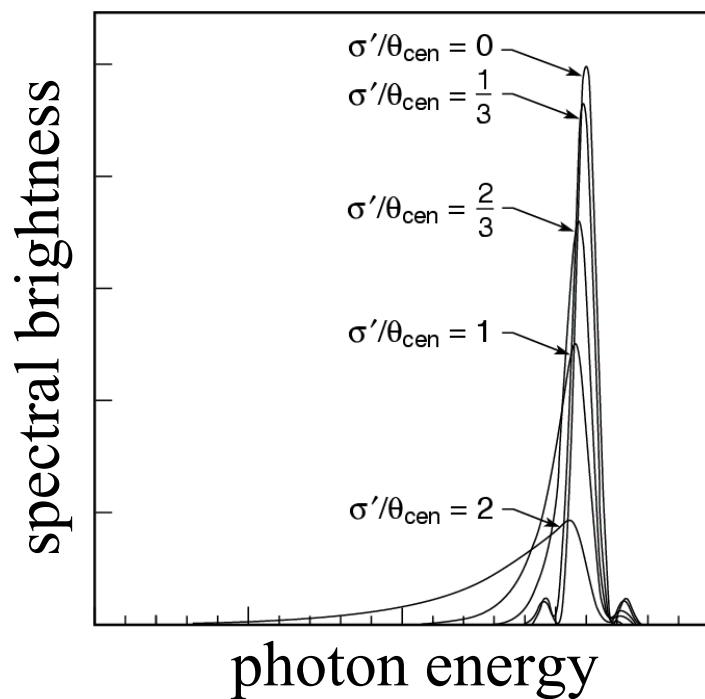
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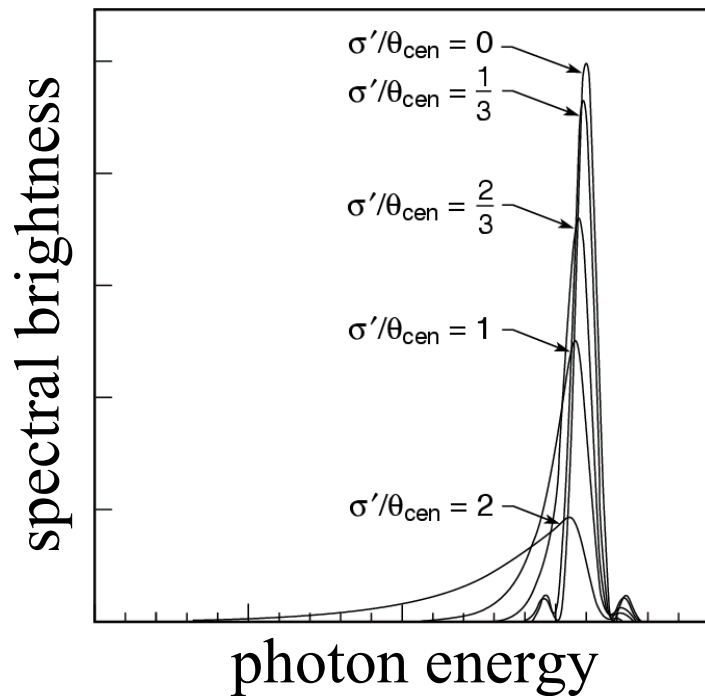
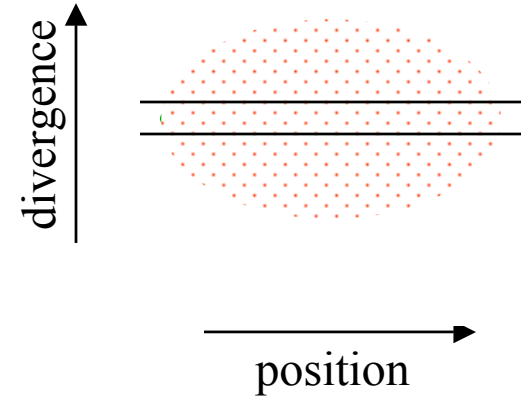
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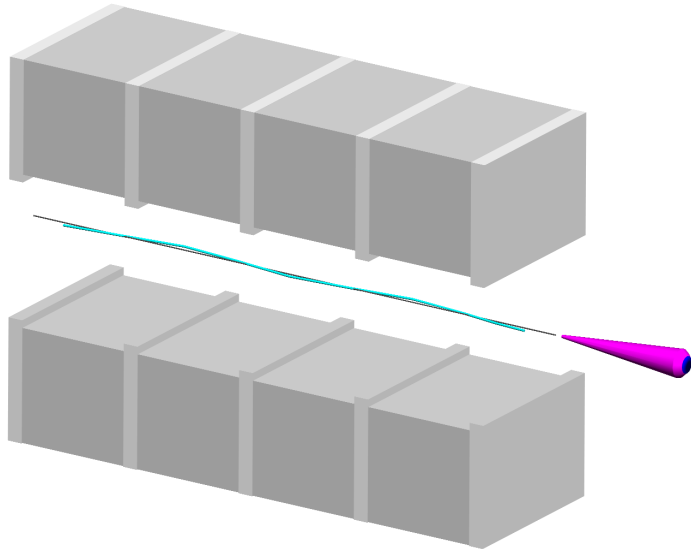
optimizing brightness



$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{1}{2}K^2 + \gamma^2\theta^2\right)$$

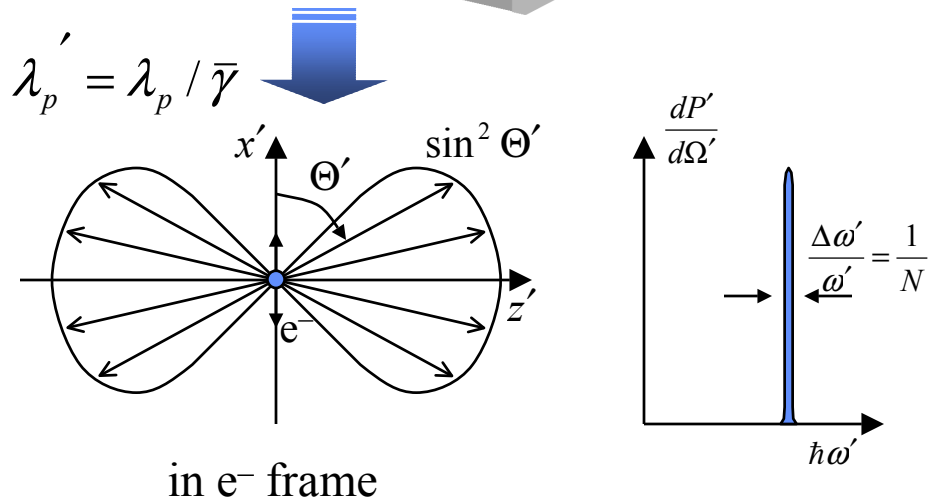
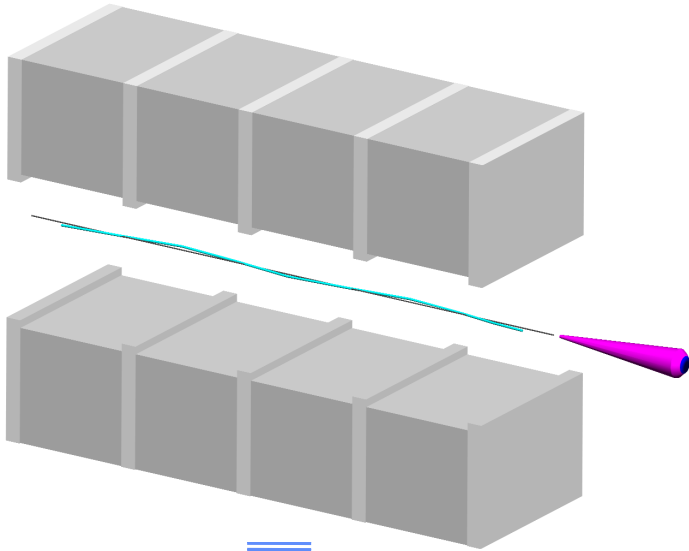
$$\frac{\Delta\lambda}{\lambda} = \frac{\lambda_u}{2} \theta^2 \Rightarrow \left. \frac{\Delta\lambda}{\lambda} \right|_{FWHM} \approx \frac{1}{N} \frac{\sigma_T'^2}{\sigma_{cen}'^2}$$

# Intuitive picture of undulator radiation

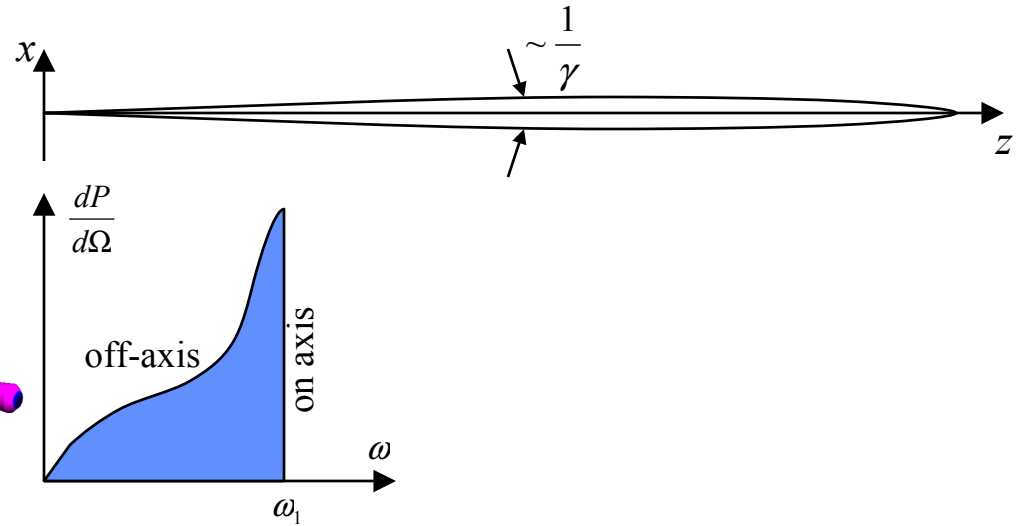
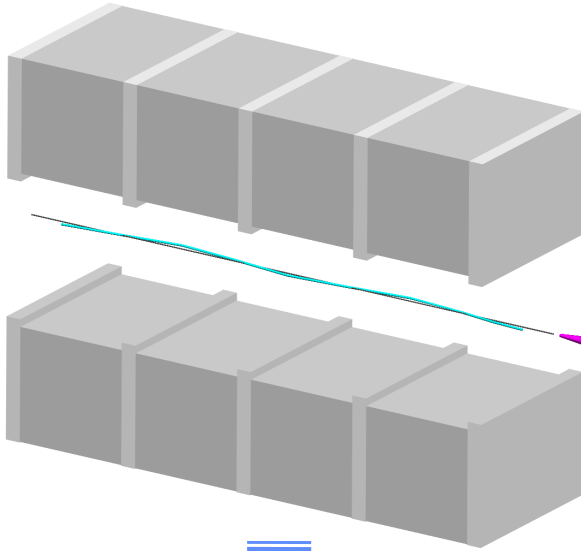




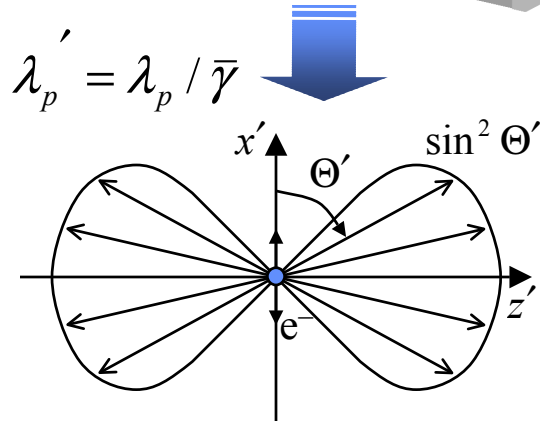
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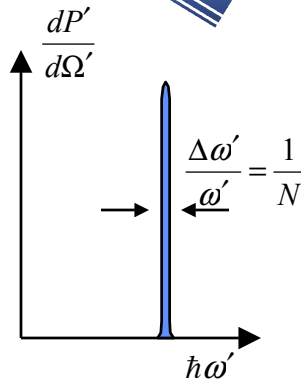
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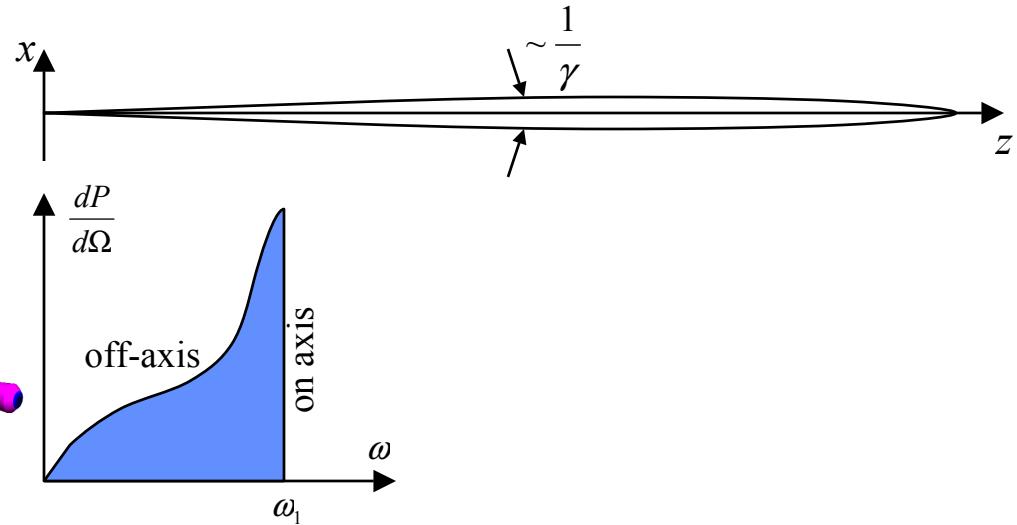
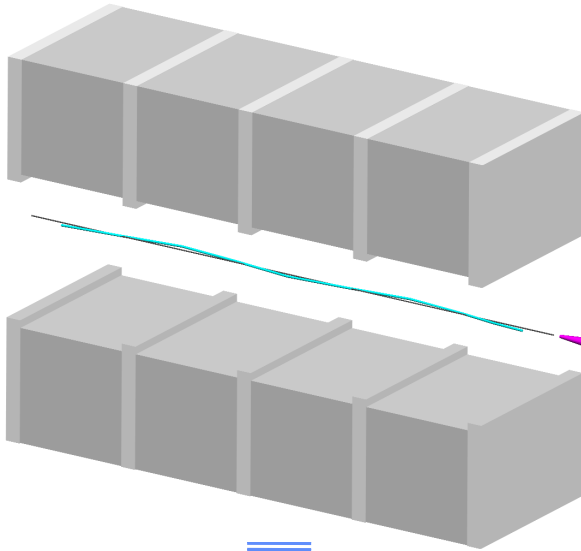
back to lab frame



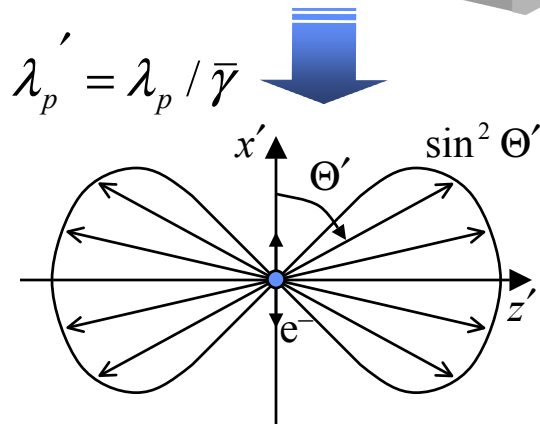
in  $e^-$  frame



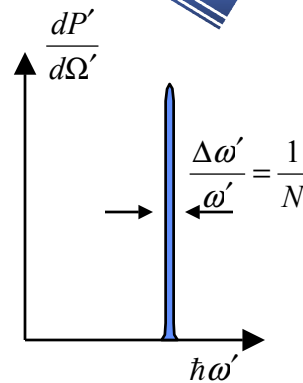
# Intuitive picture of undulator radiation



back to lab frame



in e<sup>-</sup> frame

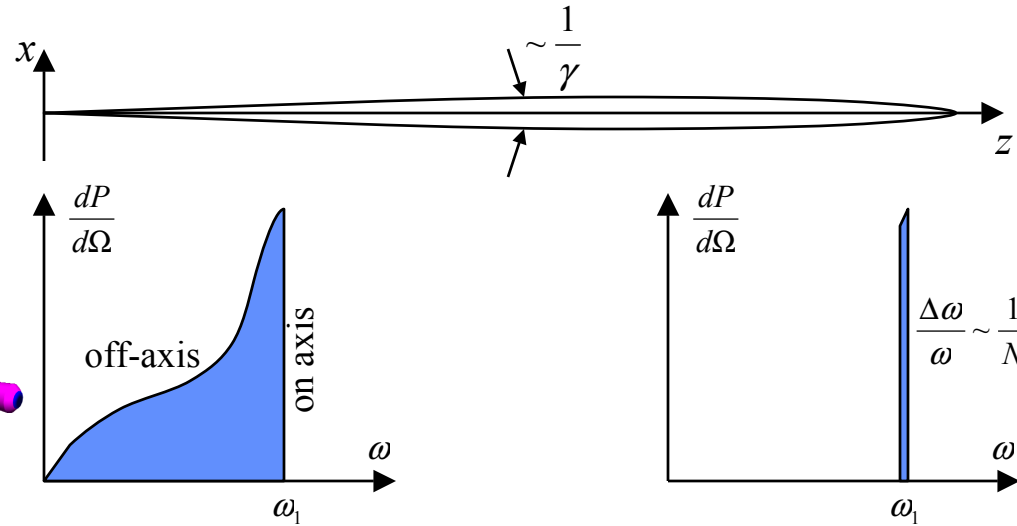
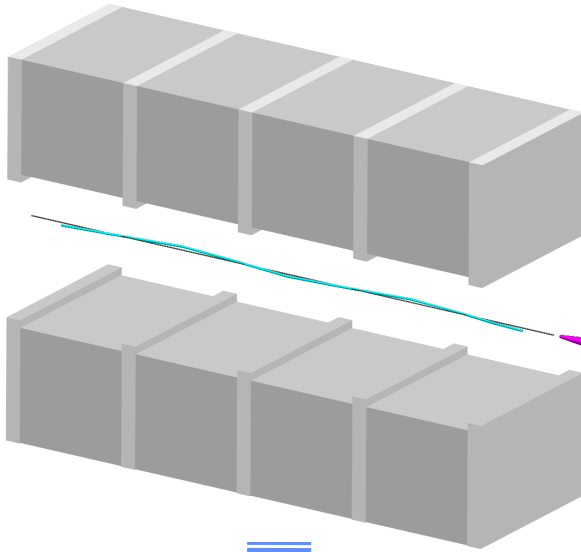


$$\lambda_n = \frac{\lambda_p}{2\gamma^2 n} \left( 1 + \frac{1}{2} K^2 + \gamma^2 \theta^2 \right)$$

$$\frac{\Delta\lambda}{\lambda_n} \sim \frac{1}{nN_p}$$

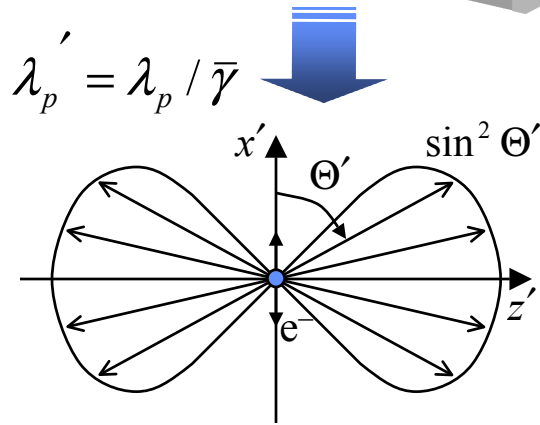
(for fixed  $\theta$  only!)

# Intuitive picture of undulator radiation

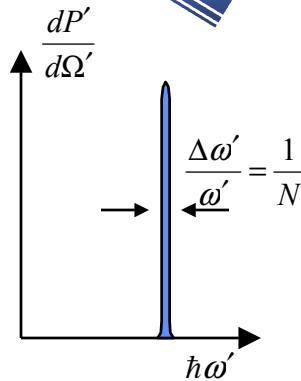


back to lab frame

after pin-hole aperture



in e<sup>-</sup> frame

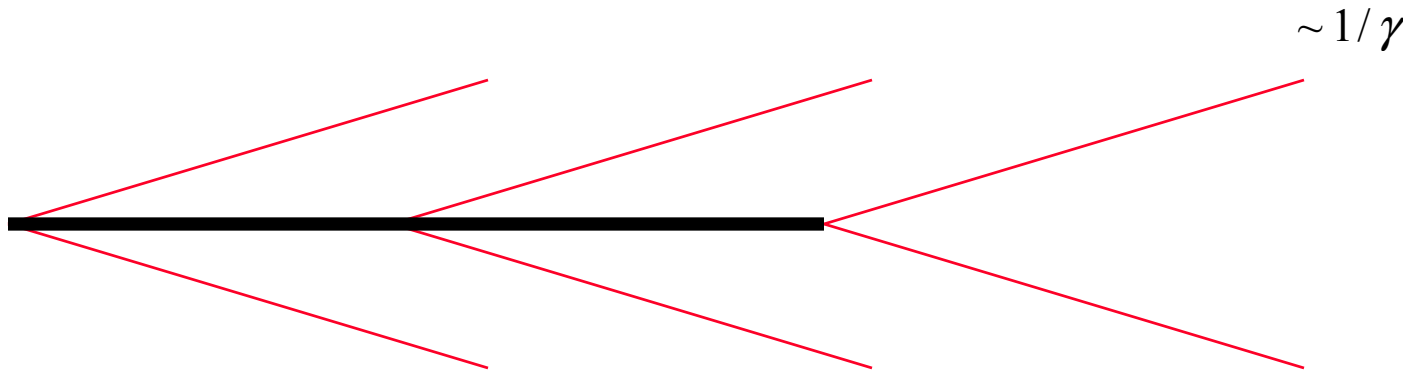


$$\lambda_n = \frac{\lambda_p}{2\gamma^2 n} \left( 1 + \frac{1}{2} K^2 + \gamma^2 \theta^2 \right)$$

$$\frac{\Delta\lambda}{\lambda_n} \sim \frac{1}{nN_p}$$

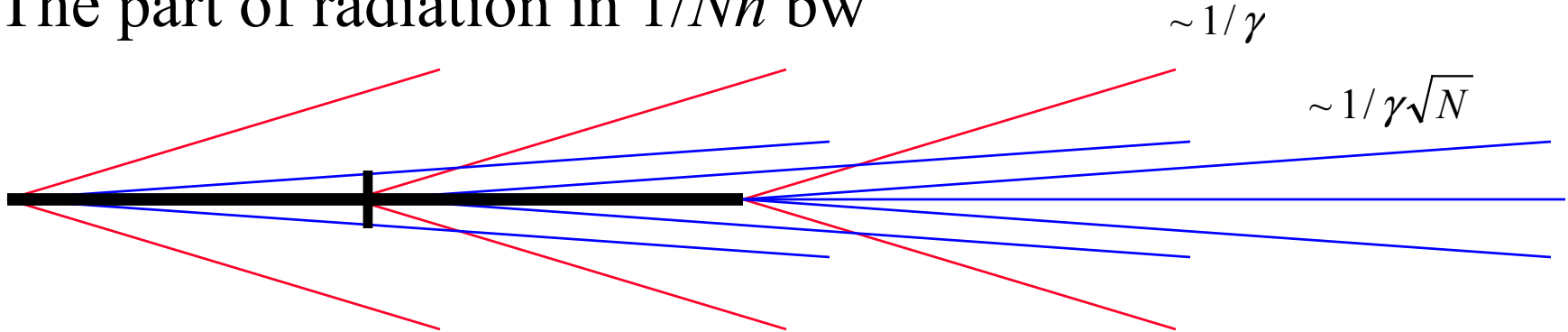
(for fixed  $\theta$  only!)

# Central cone concept



# Central cone concept

The part of radiation in  $1/Nn$  bw

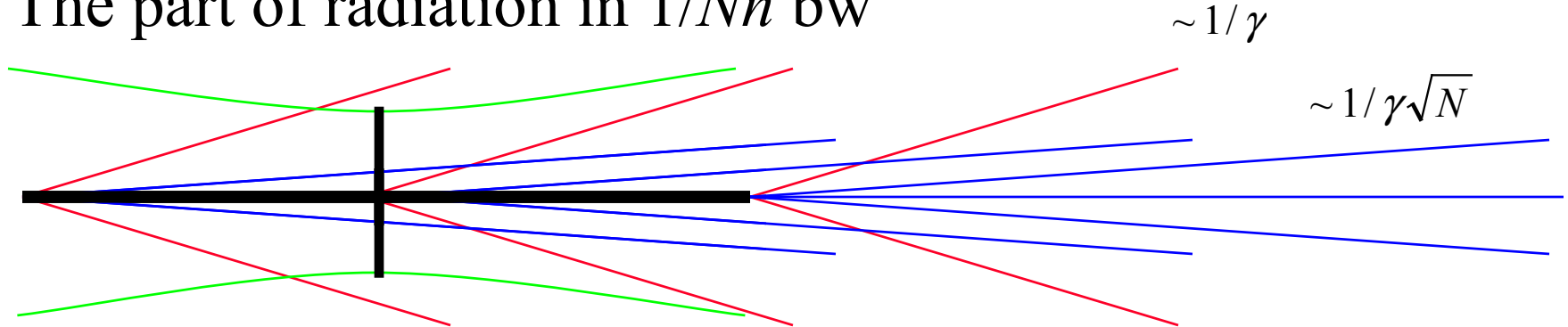


$$\sigma_{cen}^2 = \frac{\lambda}{2L}$$

$$\sigma_{cen}^2 = \frac{2\lambda L}{(4\pi)^2}$$

# Central cone concept

The part of radiation in  $1/Nn$  bw



$$\sigma_{cen}'^2 = \frac{\lambda}{2L}$$

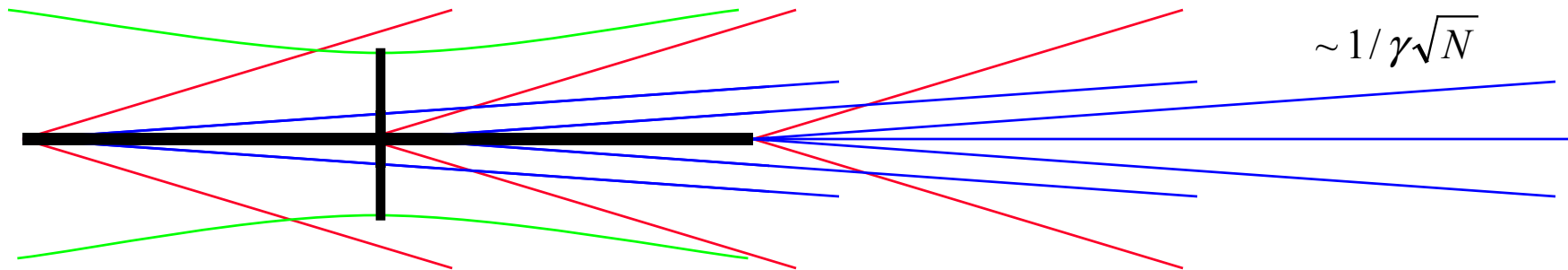
$$\sigma_T'^2 = \sigma_{cen}'^2 + \frac{\epsilon}{\beta}$$

$$\sigma_{cen}^2 = \frac{2\lambda L}{(4\pi)^2}$$

$$\sigma_T^2 = \sigma_{cen}^2 + \epsilon \beta$$

# Central cone concept

The part of radiation in  $1/Nn$  bw



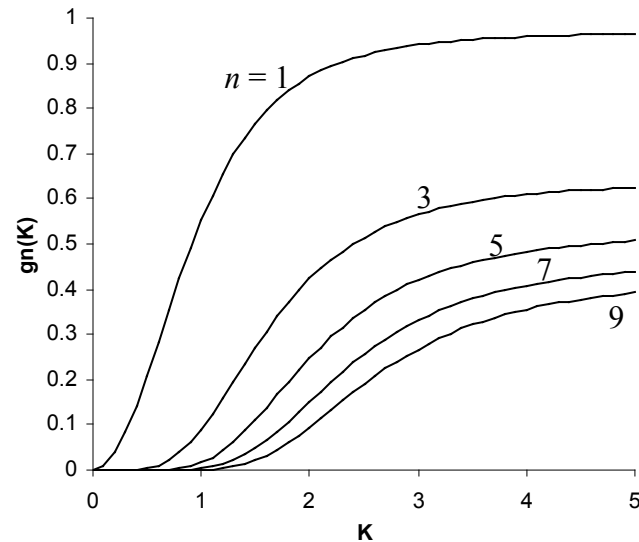
$$\sigma_{cen}'^2 = \frac{\lambda}{2L}$$

$$\sigma_T'^2 = \sigma_{cen}'^2 + \frac{\epsilon}{\beta}$$

$$\sigma_{cen}^2 = \frac{2\lambda L}{(4\pi)^2}$$

$$\sigma_T^2 = \sigma_{cen}^2 + \epsilon \beta$$

$$F_n = \pi \alpha N \frac{I}{e} g_n(K)$$



$$\text{Function } g_n(K) = \frac{nK^2 [JJ]}{(1 + \frac{1}{2} K^2)}$$



# Flux (central cone) through aperture

For aperture  $\sigma_a$  at distance  $D$ ,  $\sigma'_a = \sigma_a / D$

$$F_n \frac{1}{1 + \frac{1}{\sigma'_a{}^2} \left( \sigma_T'^2 + \frac{\sigma_T^2}{D^2} \right)} \frac{1}{\sqrt{1 + \left( \frac{N}{N_\delta} \right)^2 \frac{\sigma_{cen}'^2}{\sigma_{x-ray}'^2}}}$$

electron beam energy spread

$$N_\delta \approx \frac{1}{5\sigma_\delta} \swarrow$$

Optimum  $\beta \approx D$

here x-ray divergence after pinhole  $\sigma_{x-ray}^2 = \frac{\sigma_T'^2}{1 + \sigma_T'^2 / (\sigma_a'^2 + \frac{\sigma_T^2}{D^2})} \approx \sigma_T'^2$

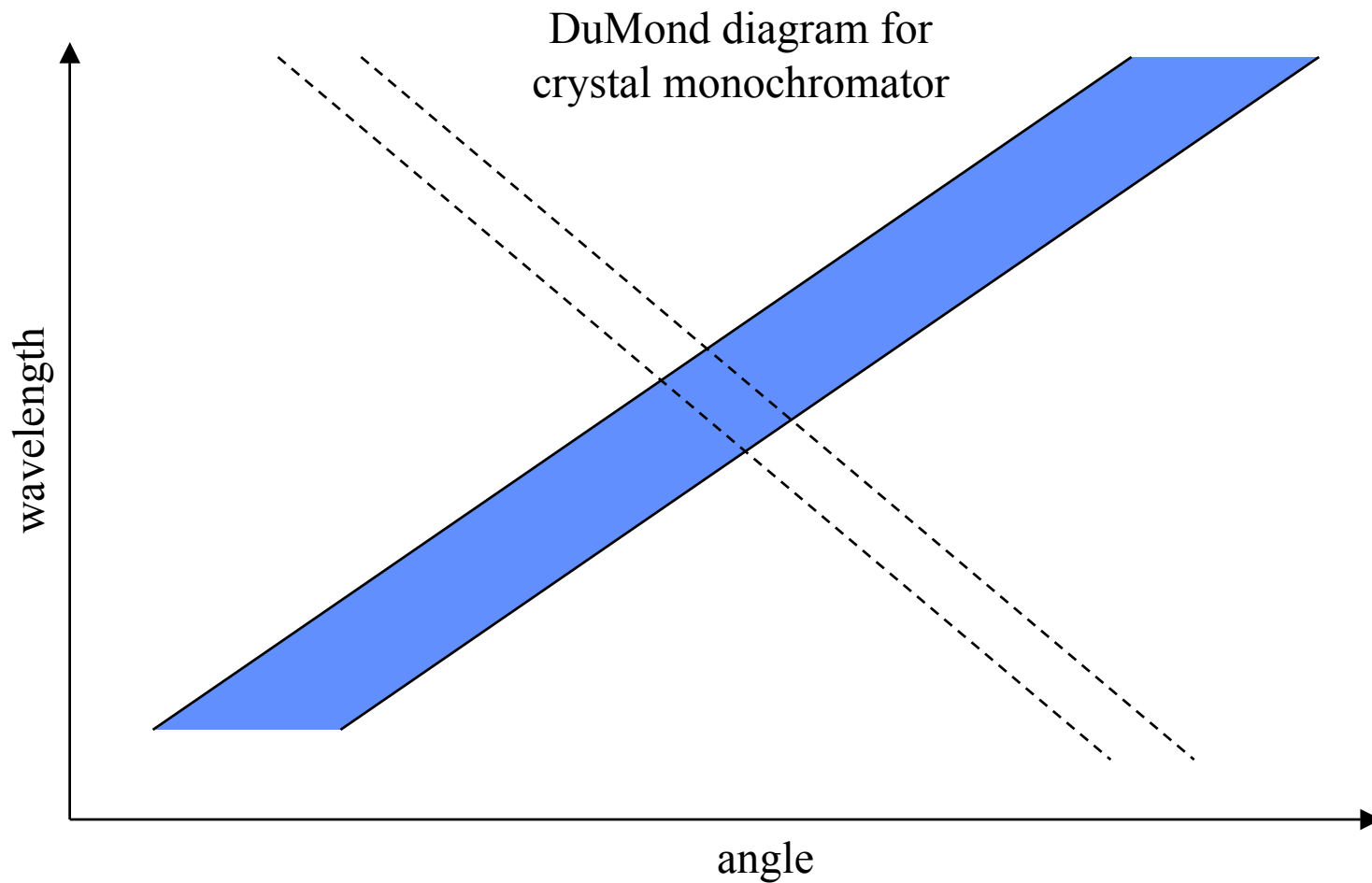
# Brightness through aperture

For aperture  $\sigma_a$  at distance  $D$ ,  $\sigma'_a = \sigma_a / D$

$$\frac{F_n}{2\pi\sigma_T'^2} \frac{1}{1 + \frac{\sigma_T^2}{\sigma_a^2}} \frac{1}{\sqrt{1 + \left(\frac{N}{N_\delta}\right)^2 \frac{\sigma_{cen}^2}{\sigma_{x-ray}^2}}}$$

Optimum  $\beta$  depends on the pinhole, usually large

# Real figure of merit for many beamlines



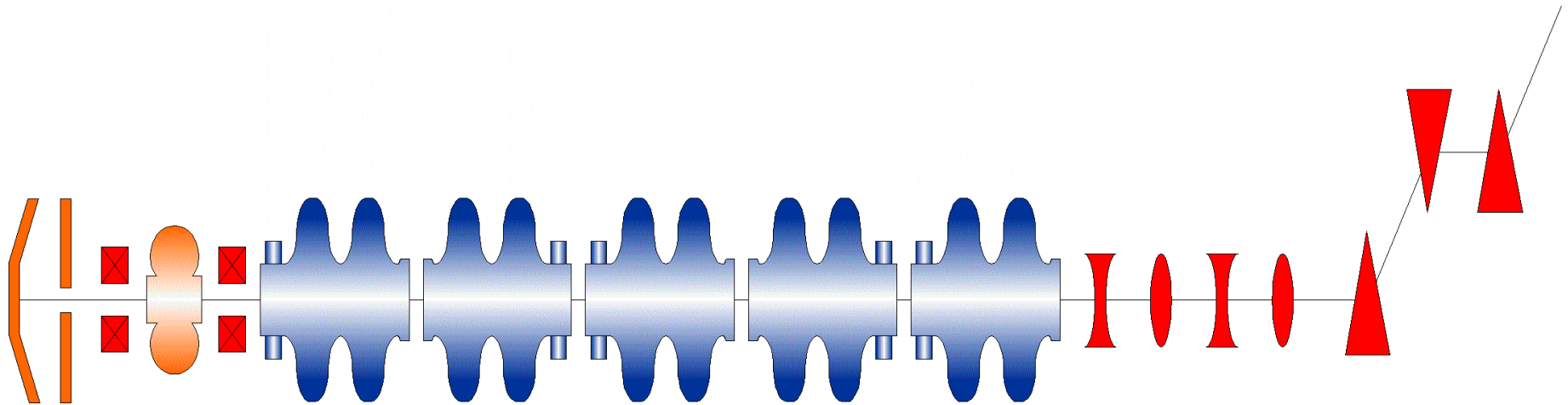
to maximize monochromator throughput one needs 1D brightness (flat beam ok)

# Optimized brilliance

$$\frac{F_n}{(\lambda/2)^2} \frac{1}{\left(1 + \frac{\epsilon}{\lambda/4\pi}\right)^2} \frac{1}{\sqrt{1 + \left(\frac{N}{N_\delta}\right)^2 \frac{\sigma_{cen}'^2}{\sigma_{x-ray}'^2}}}$$

For optimum  $\beta \approx \frac{L}{2\pi}$

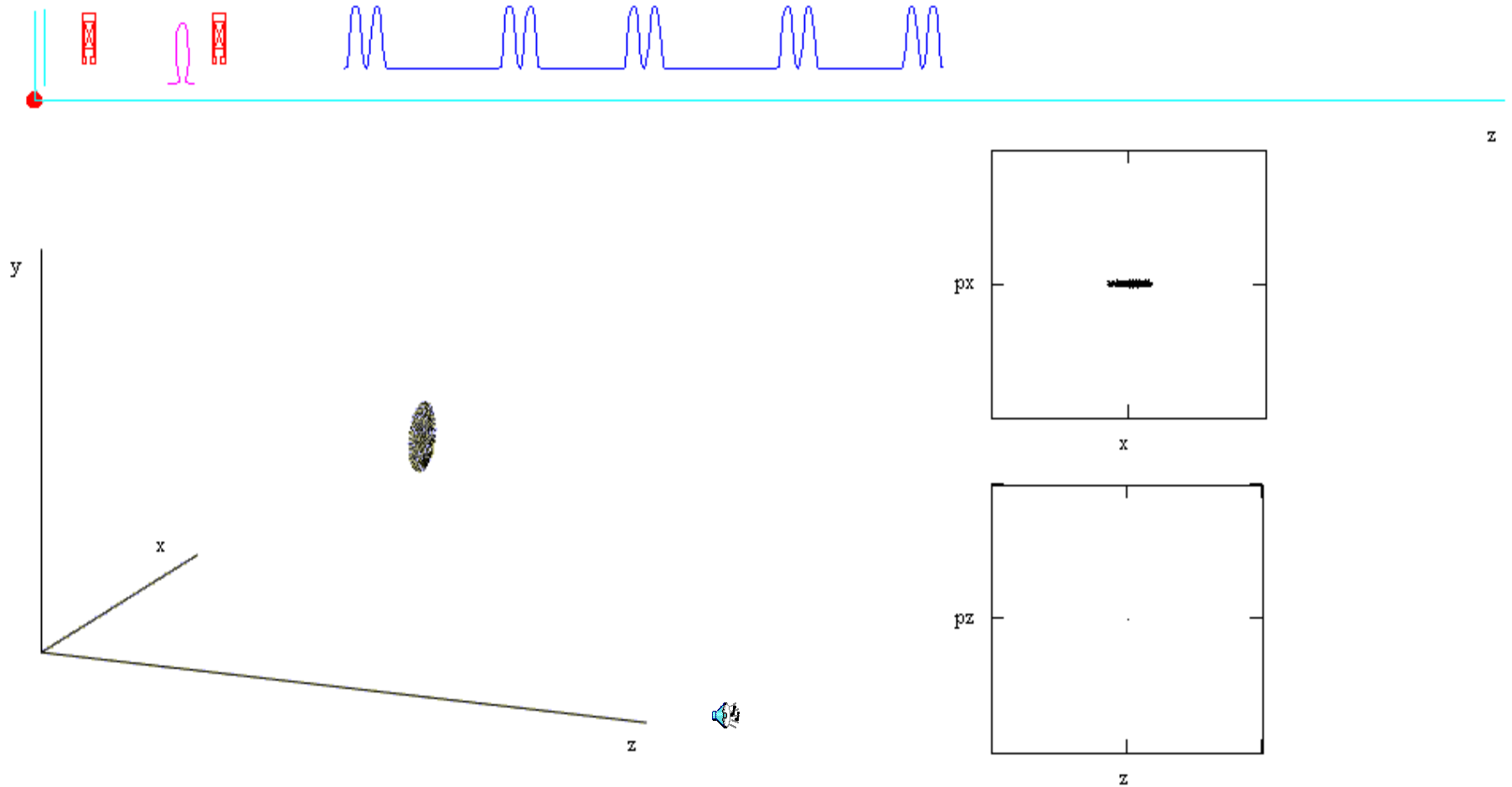
# Phase 1a ERL injector schematic



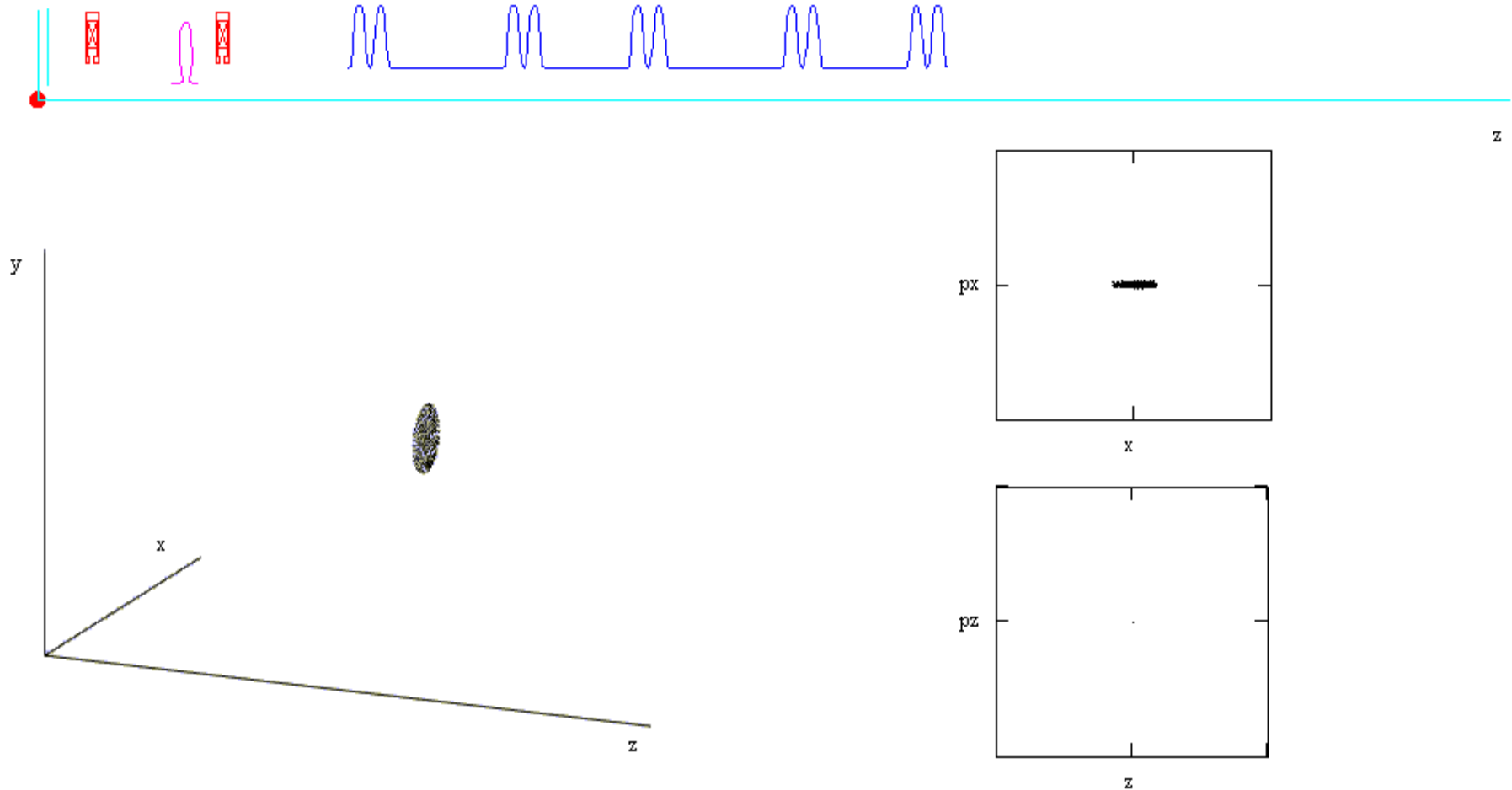
Defocusing for uniform cylinder:  $K_{s.c.} = -\frac{1}{2\epsilon_{x,n} \beta_x (\beta\gamma)^2} \frac{I}{I_A}$ ,  $f_{s.c.} = \lim_{\Delta z \rightarrow 0} \frac{1}{K_{s.c.} \Delta z}$

One might expect this scaling:  $\epsilon \propto \frac{q_{bunch}}{\sigma_z}$

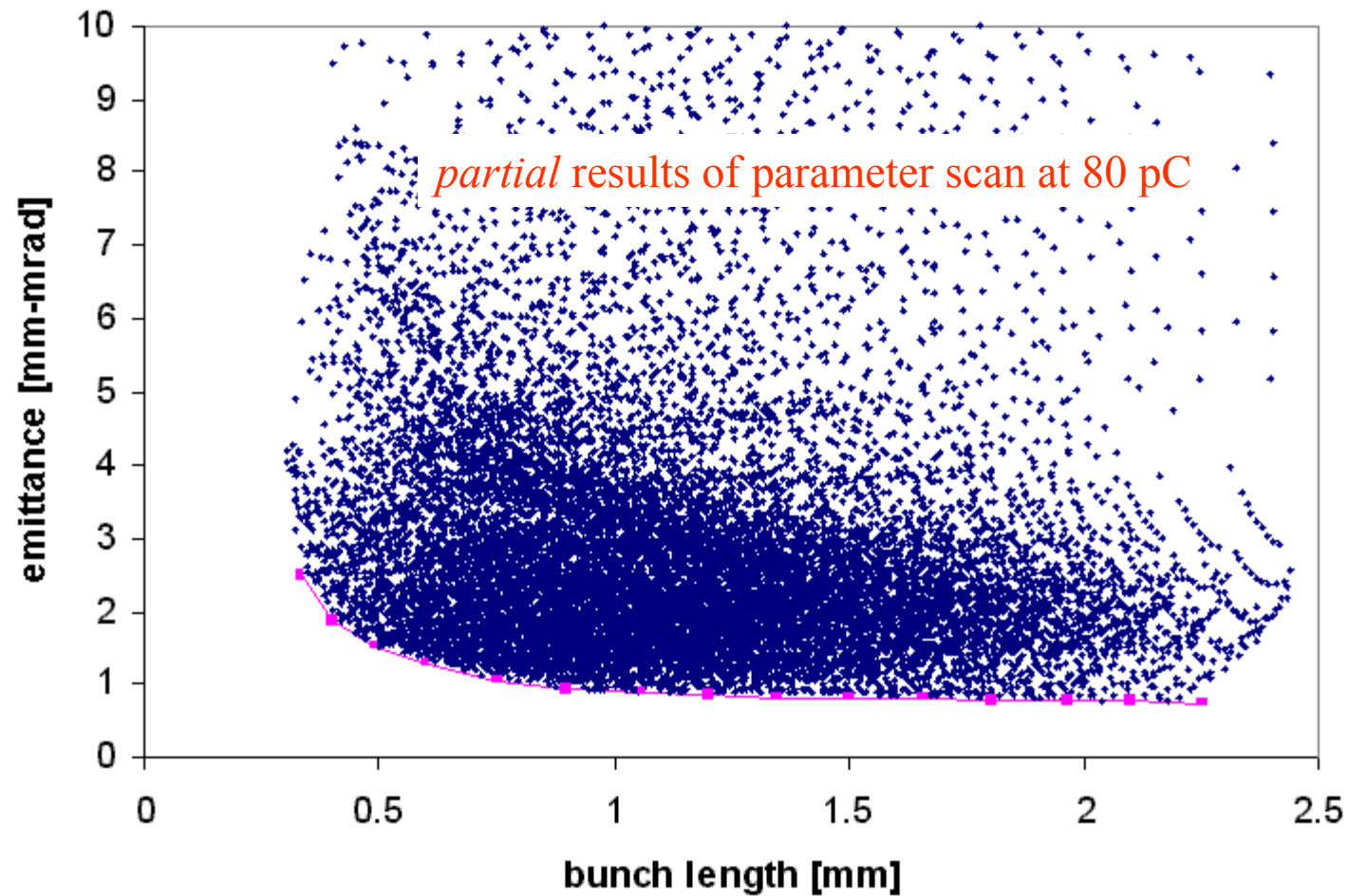
# Bunch dynamics in the injector (77 pC)



# Bunch dynamics at the DC gun (77 pC)

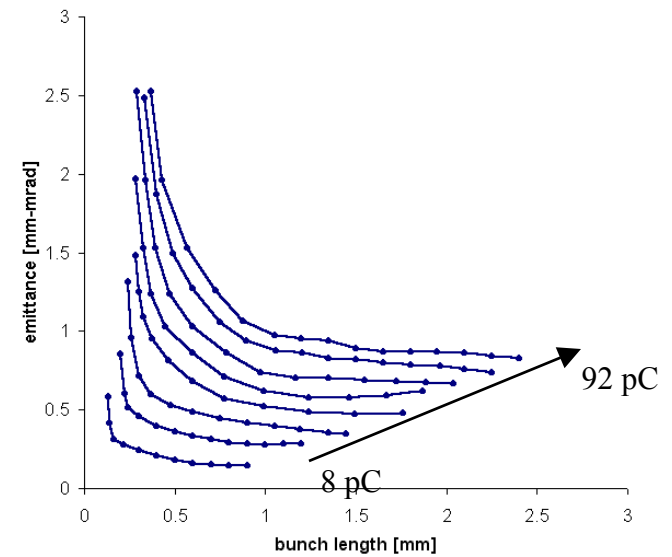
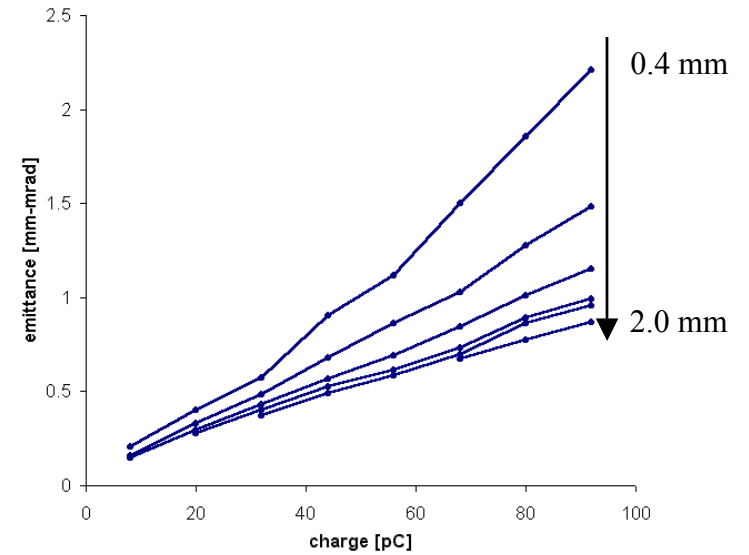
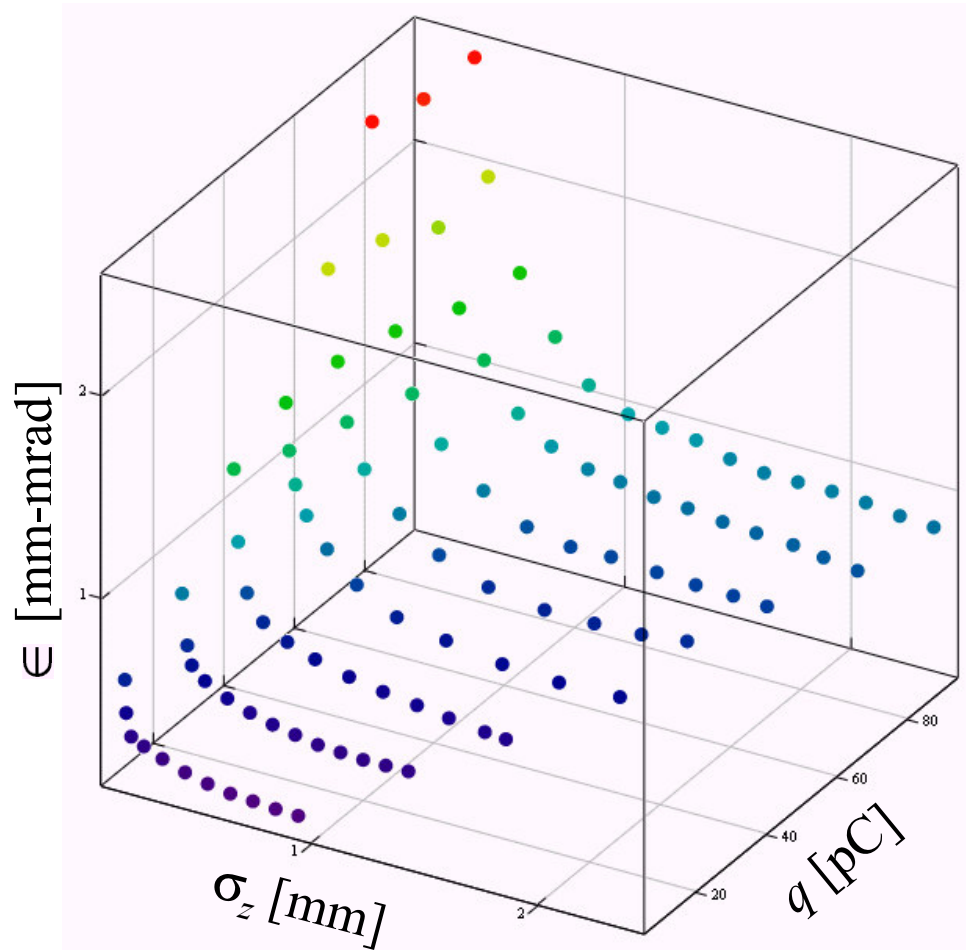


# 'feynman' at work on ERL injector

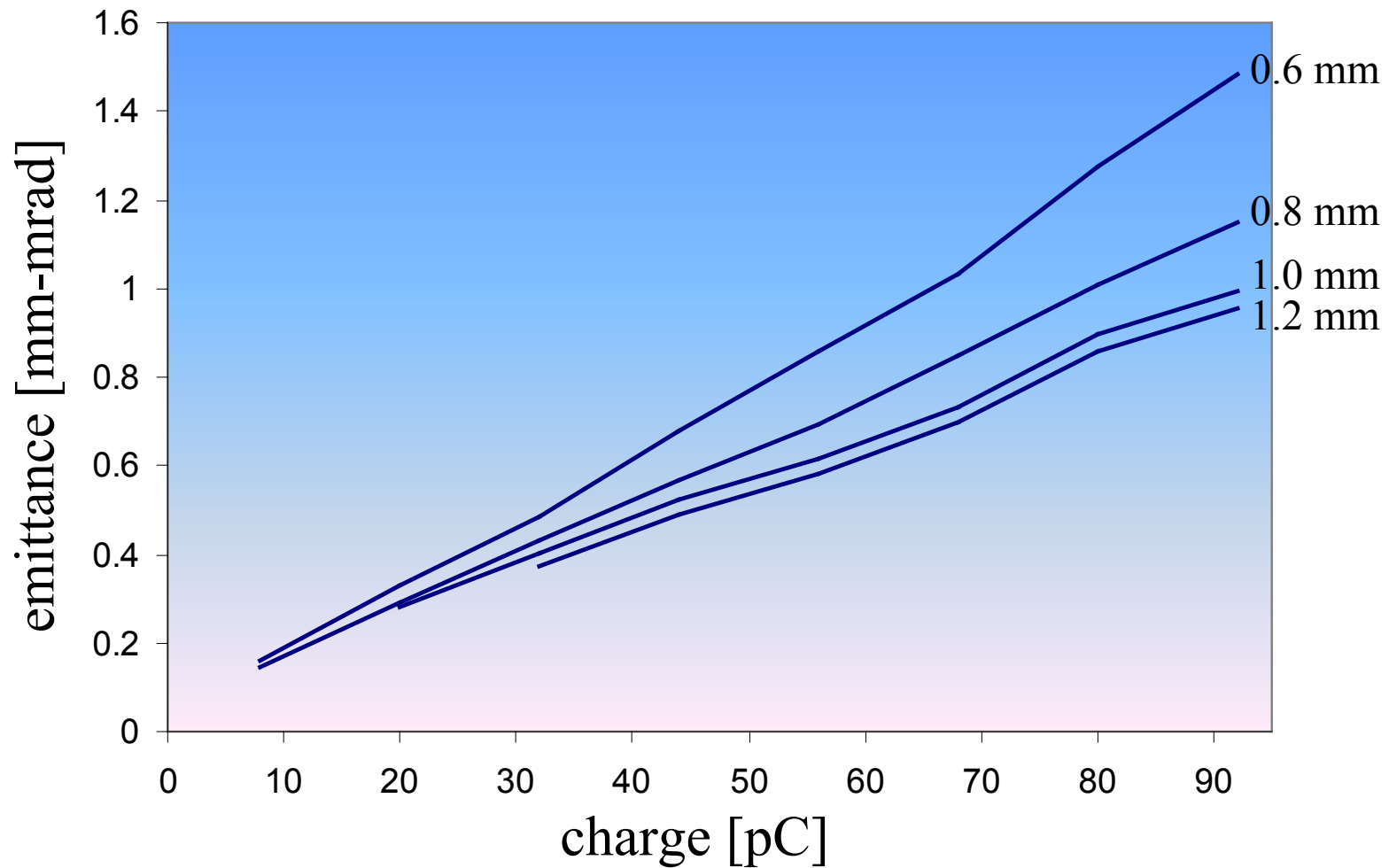




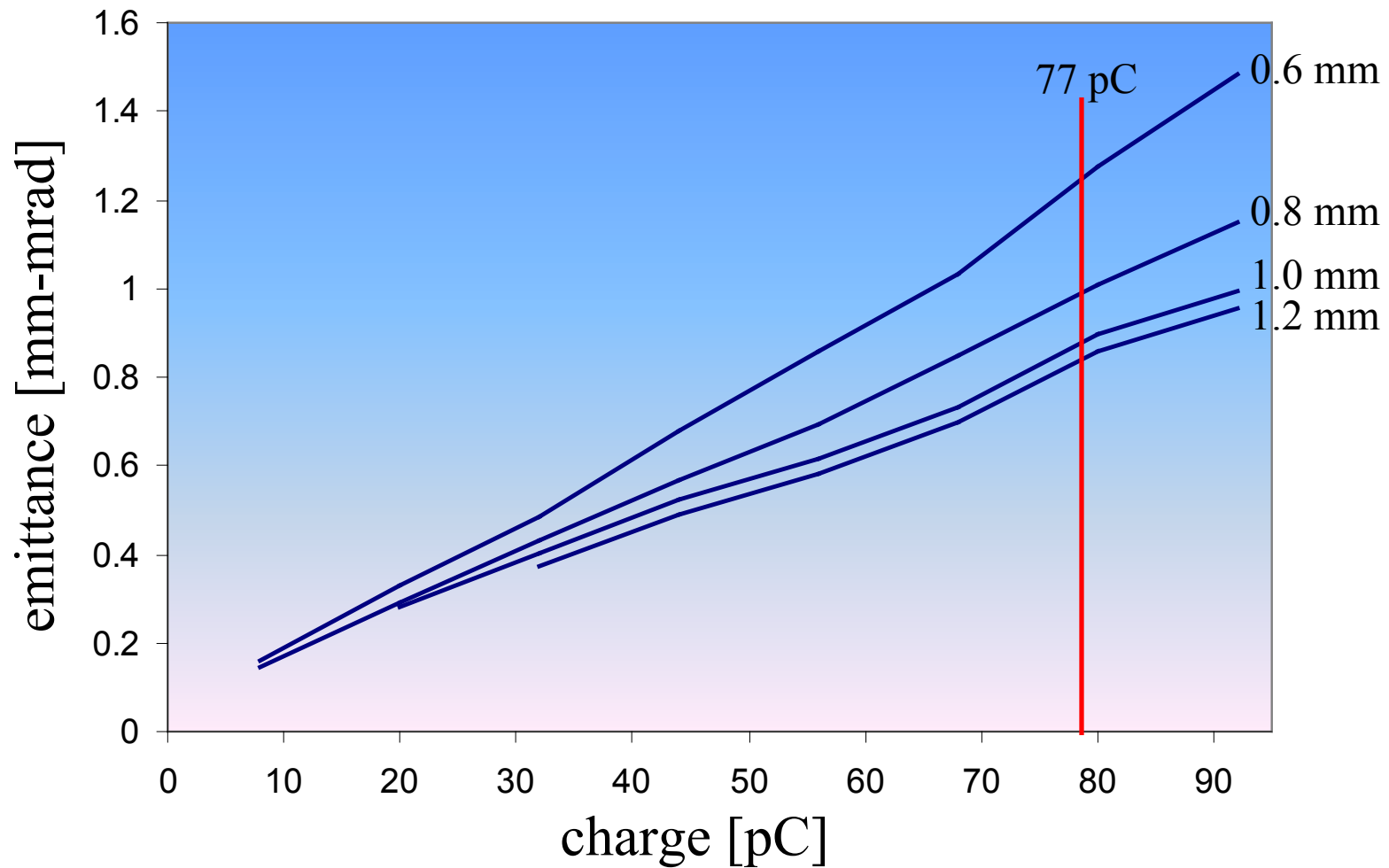
# Emit. scaling vs. charge, vs. bunch length



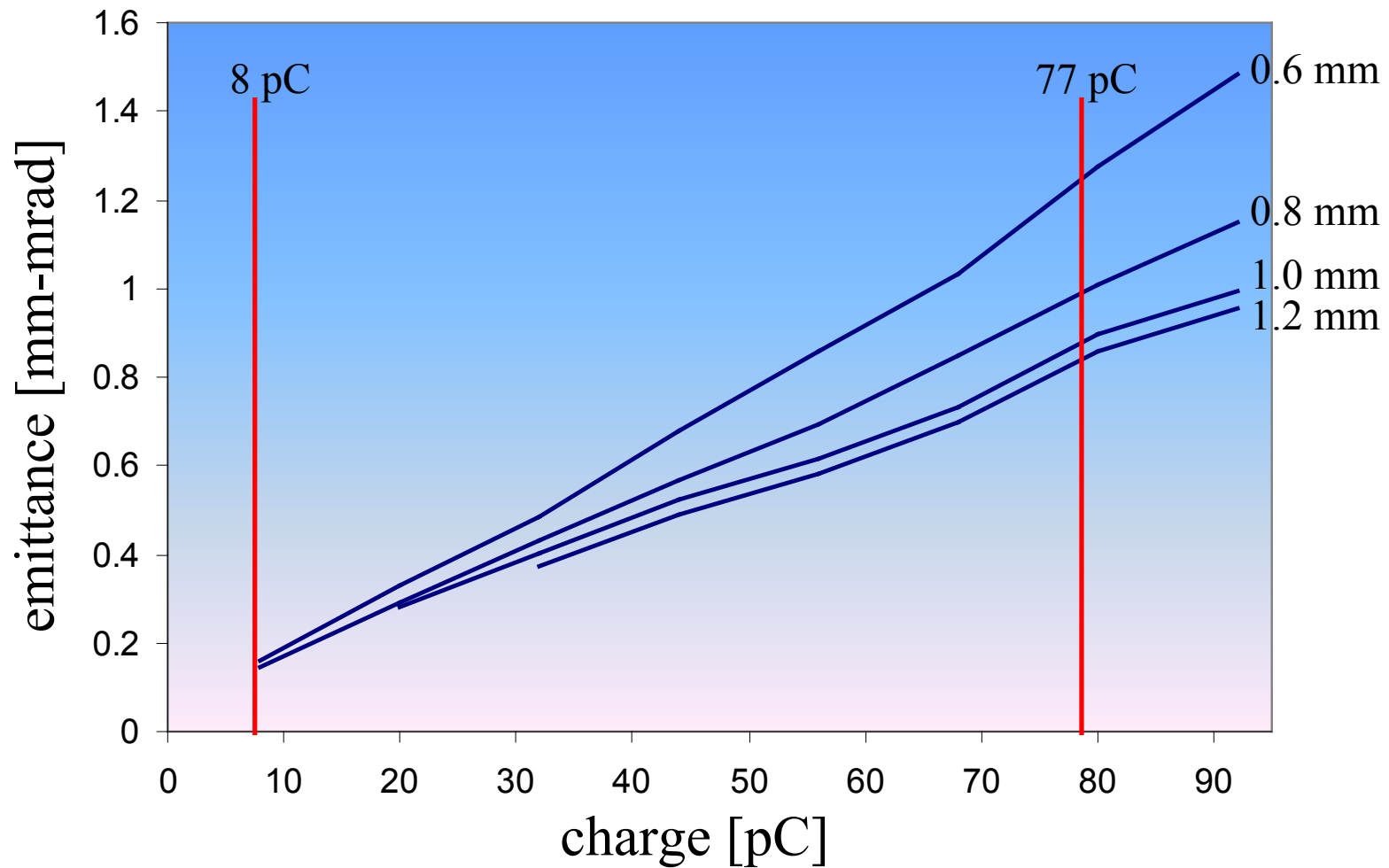
# Scaling with charge



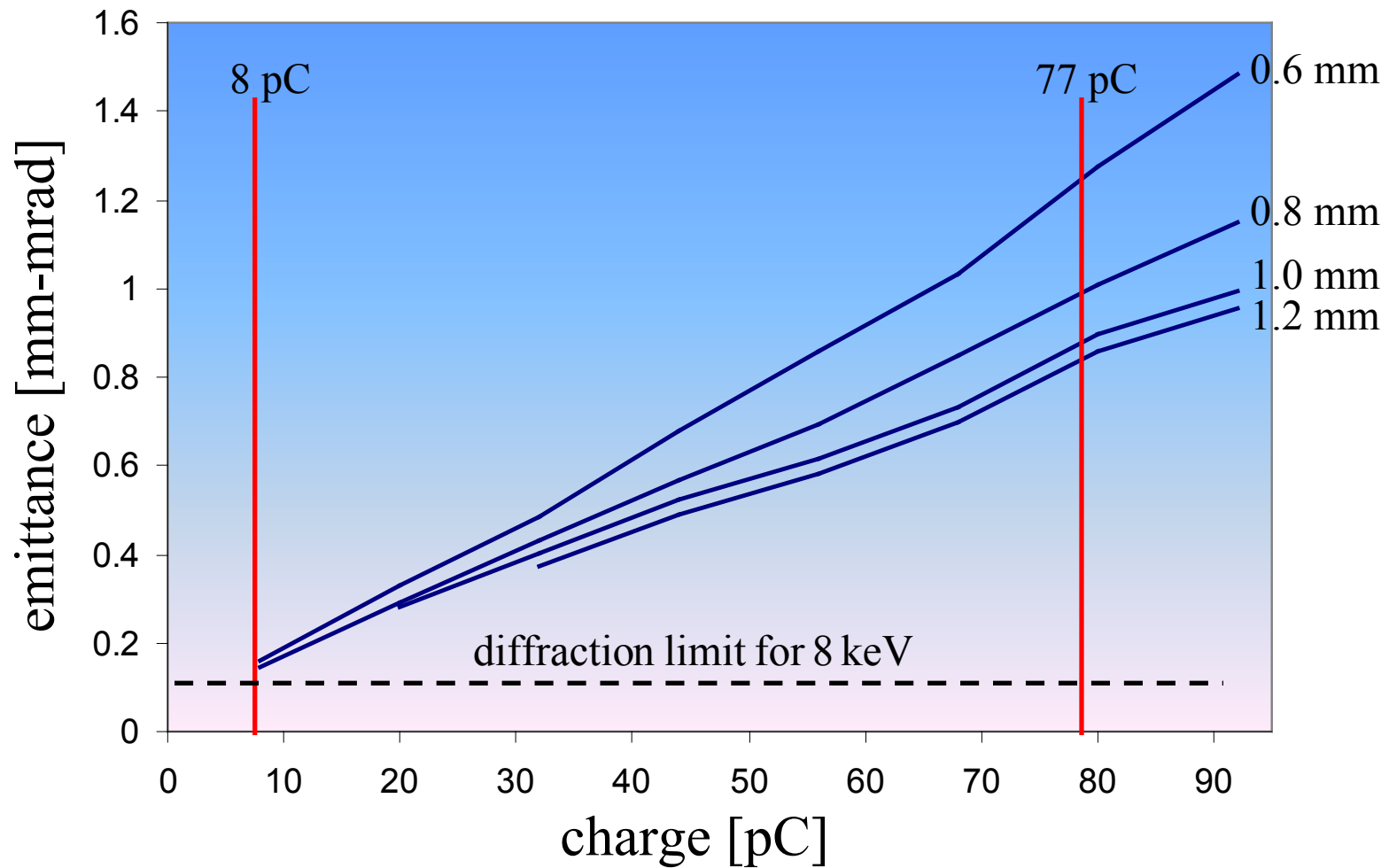
# Scaling with charge



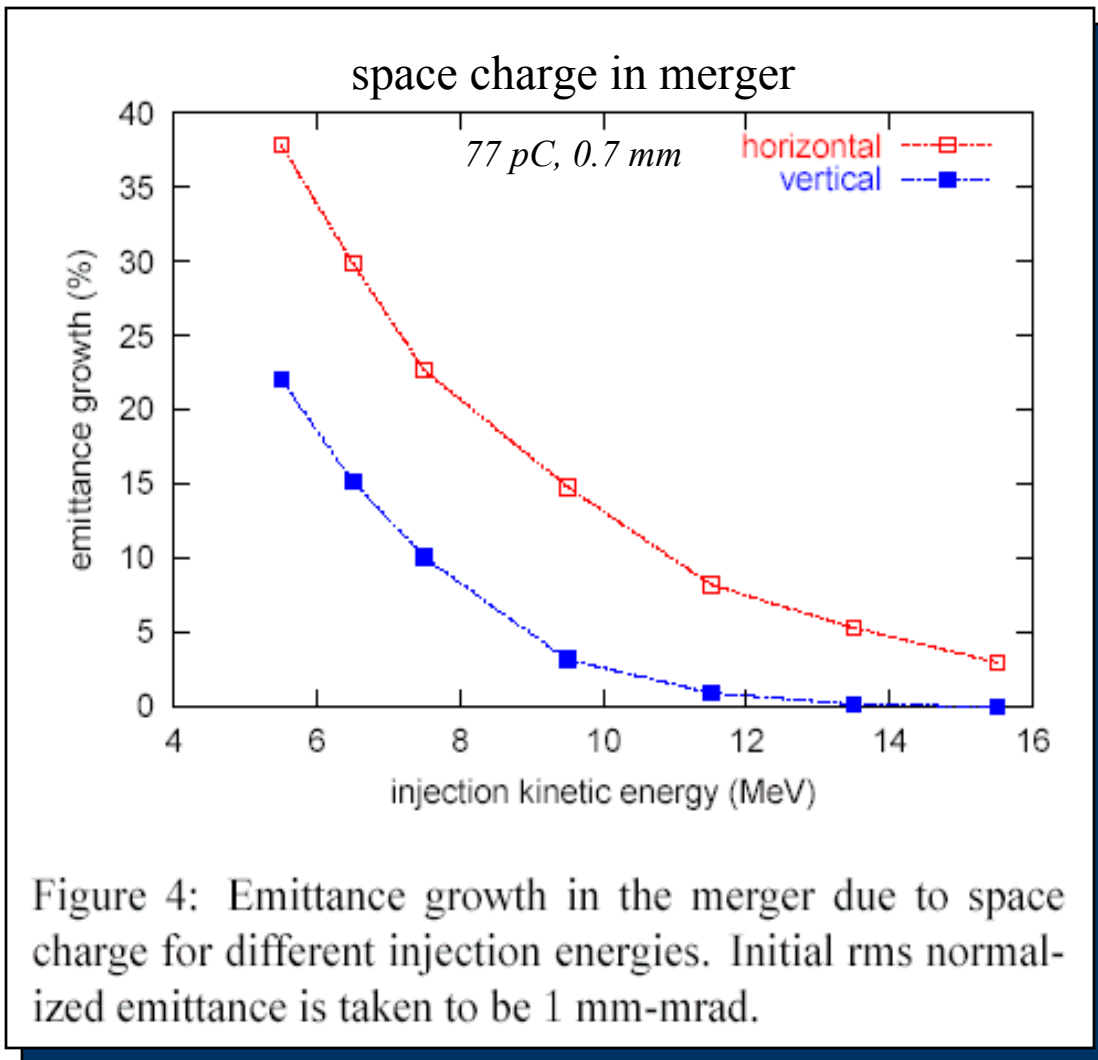
# Scaling with charge



# Scaling with charge



# Not the whole story...



# Not the whole story...

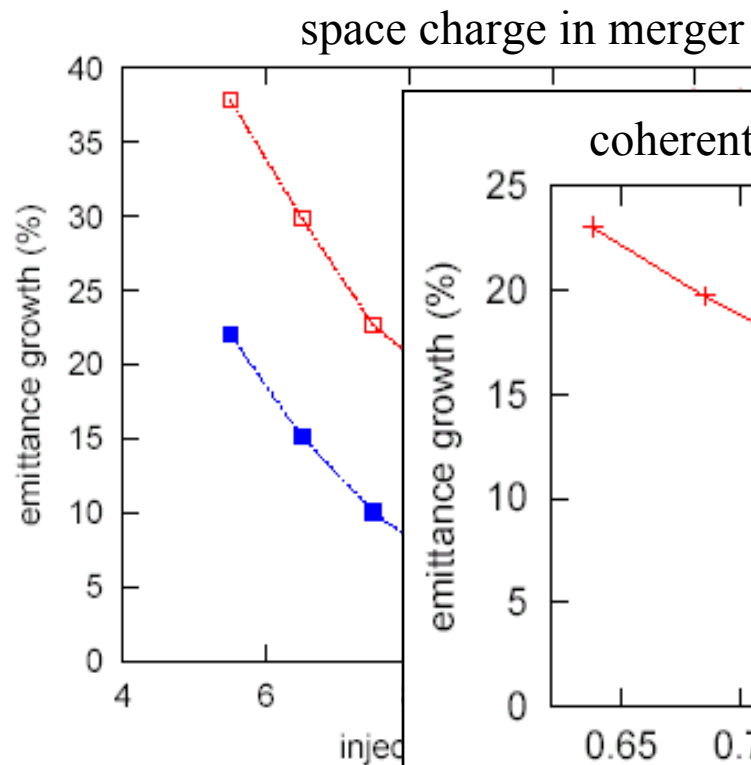


Figure 4: Emittance growth due to space charge for different injected emittances. Initial rms normalized emittance is taken to be 1 mm-mrad.

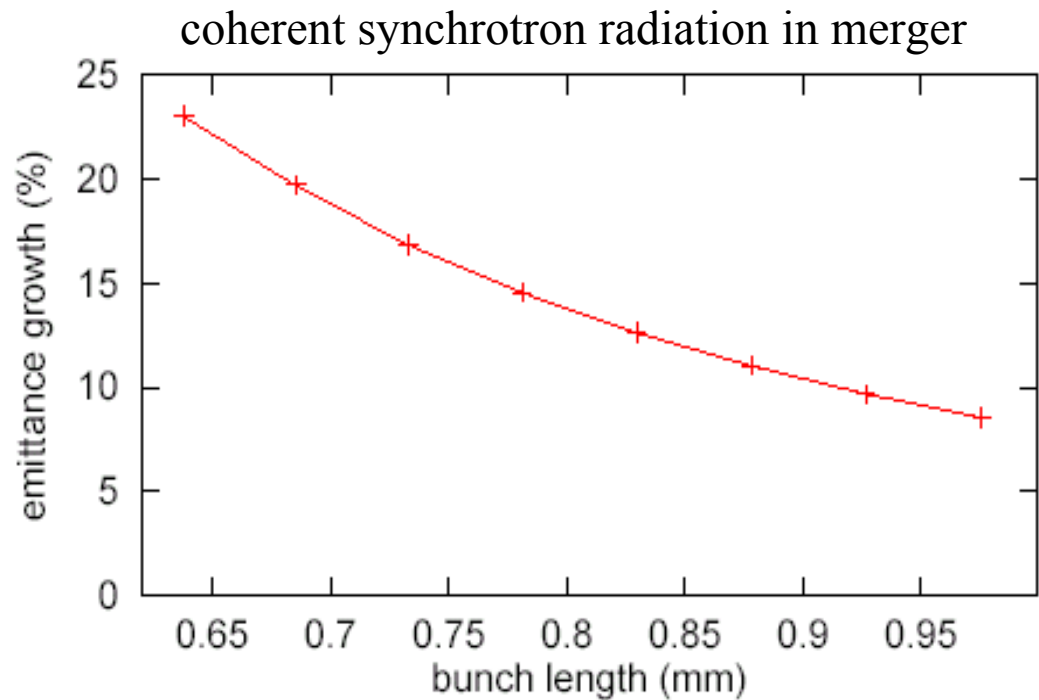


Figure 5: Emittance growth in the merger due to CSR for 77-pC bunch as a function of rms bunch length (top) and dipole bend angle for 0.6-mm bunch (bottom). Initial rms normalized emittance is taken to be 1 mm-mrad.

# Not the whole story...

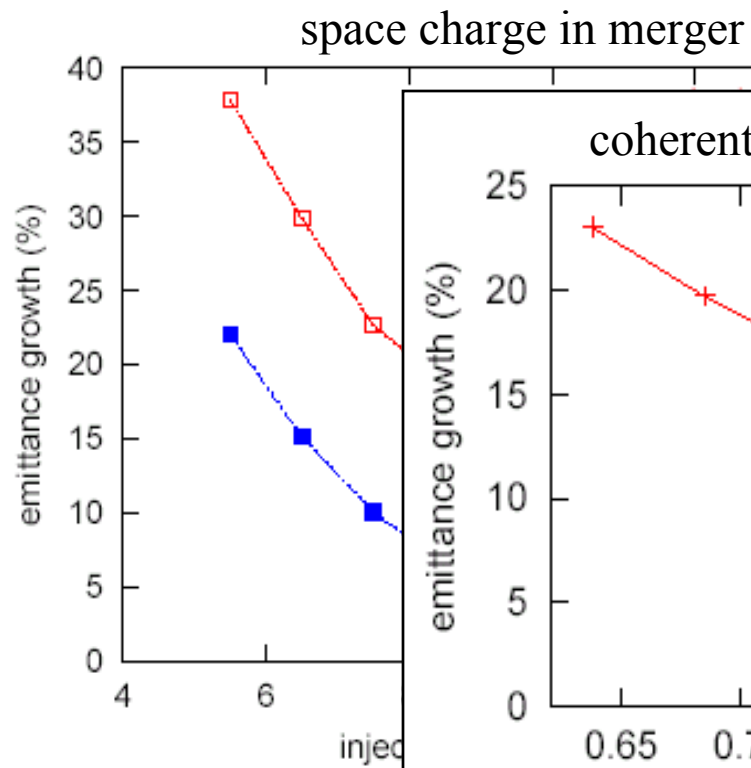


Figure 4: Emittance growth due to space charge for different injected emittances. The normalized emittance is taken to be 0.1.

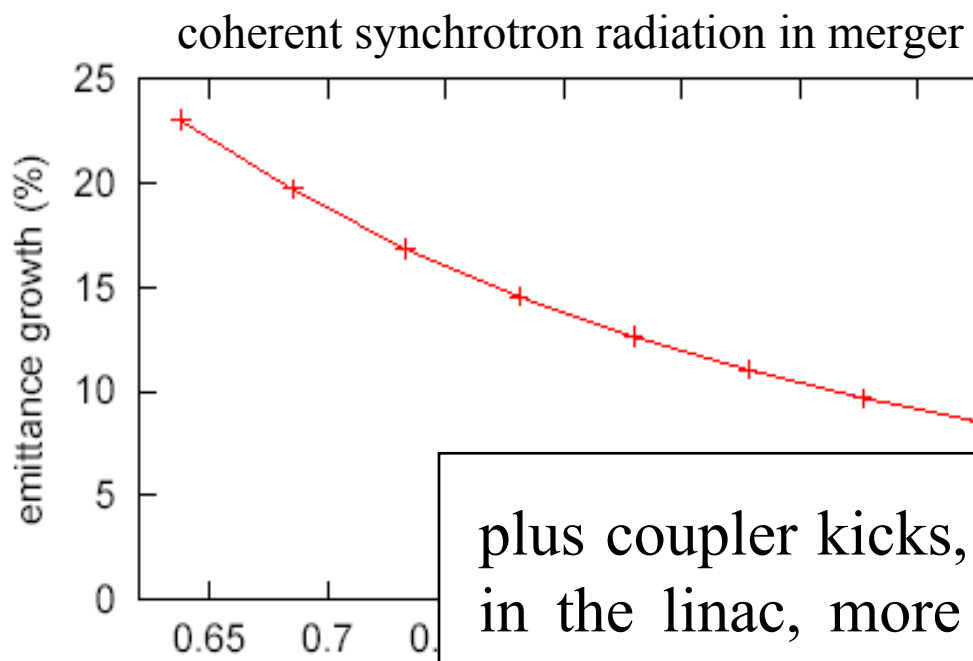


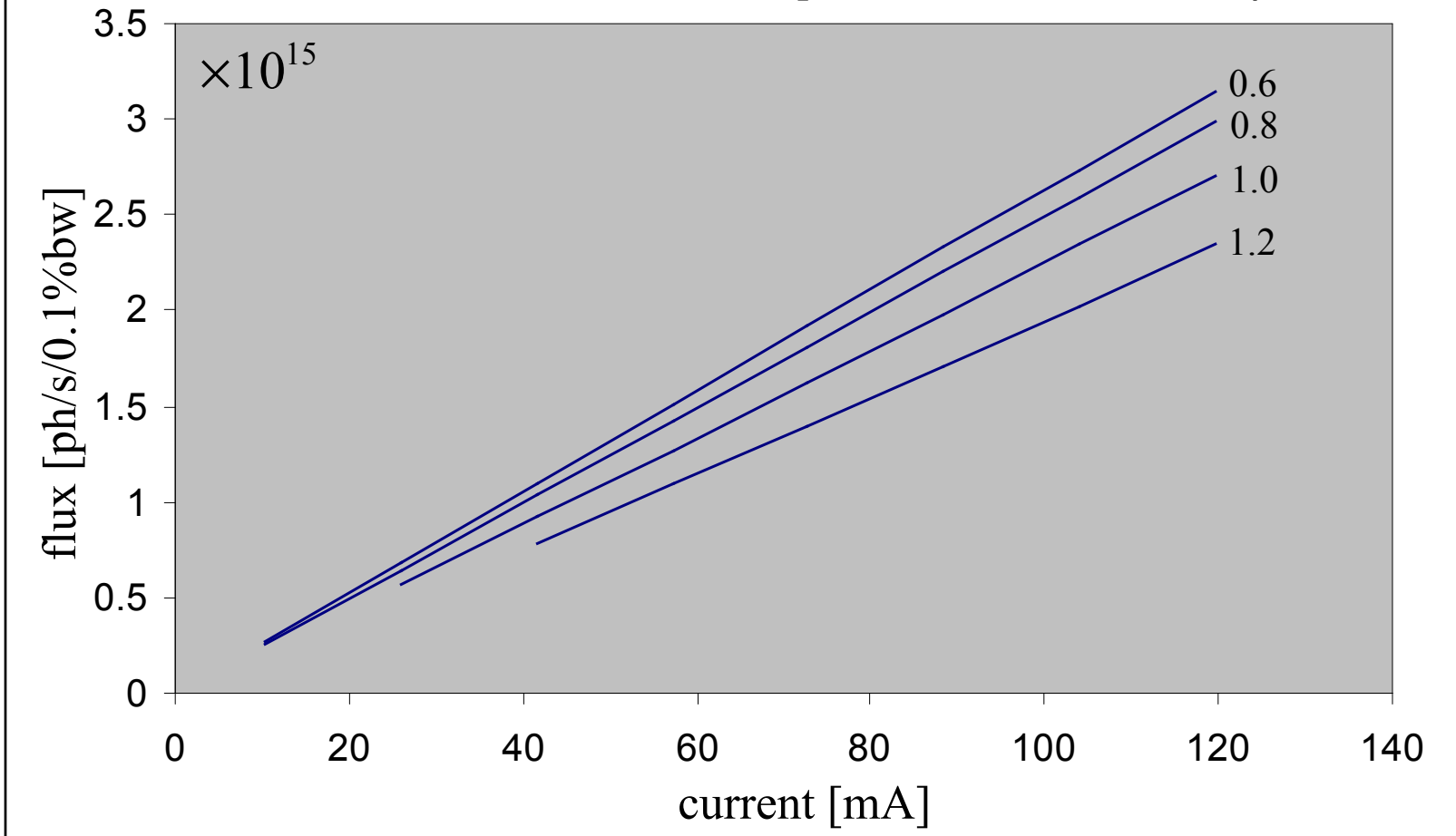
Figure 5: Emittance growth due to coherent synchrotron radiation for a 77-pC bunch as a function of dipole bend angle for a 0.1 normalized emittance is shown.

plus coupler kicks, transport in the linac, more radiation in the arcs (both coherent and incoherent), chromatic and geometric aberrations in electron optics ...

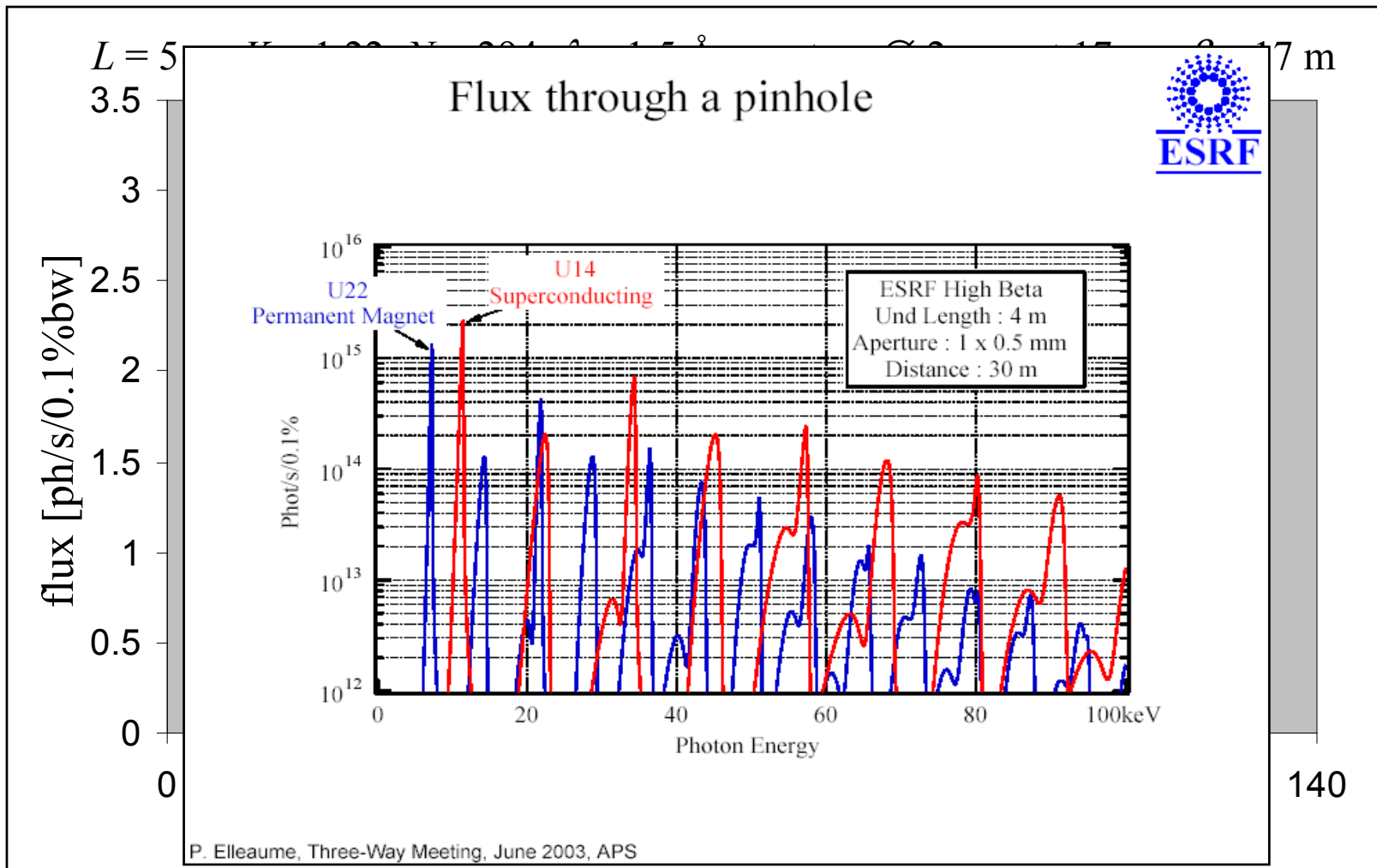


# Flux scaling

$L = 5$  m,  $K = 1.22$ ,  $N = 294$ ,  $\lambda = 1.5$  Å, aperture  $\varnothing$  2 mm at 17 m,  $\beta = 17$  m

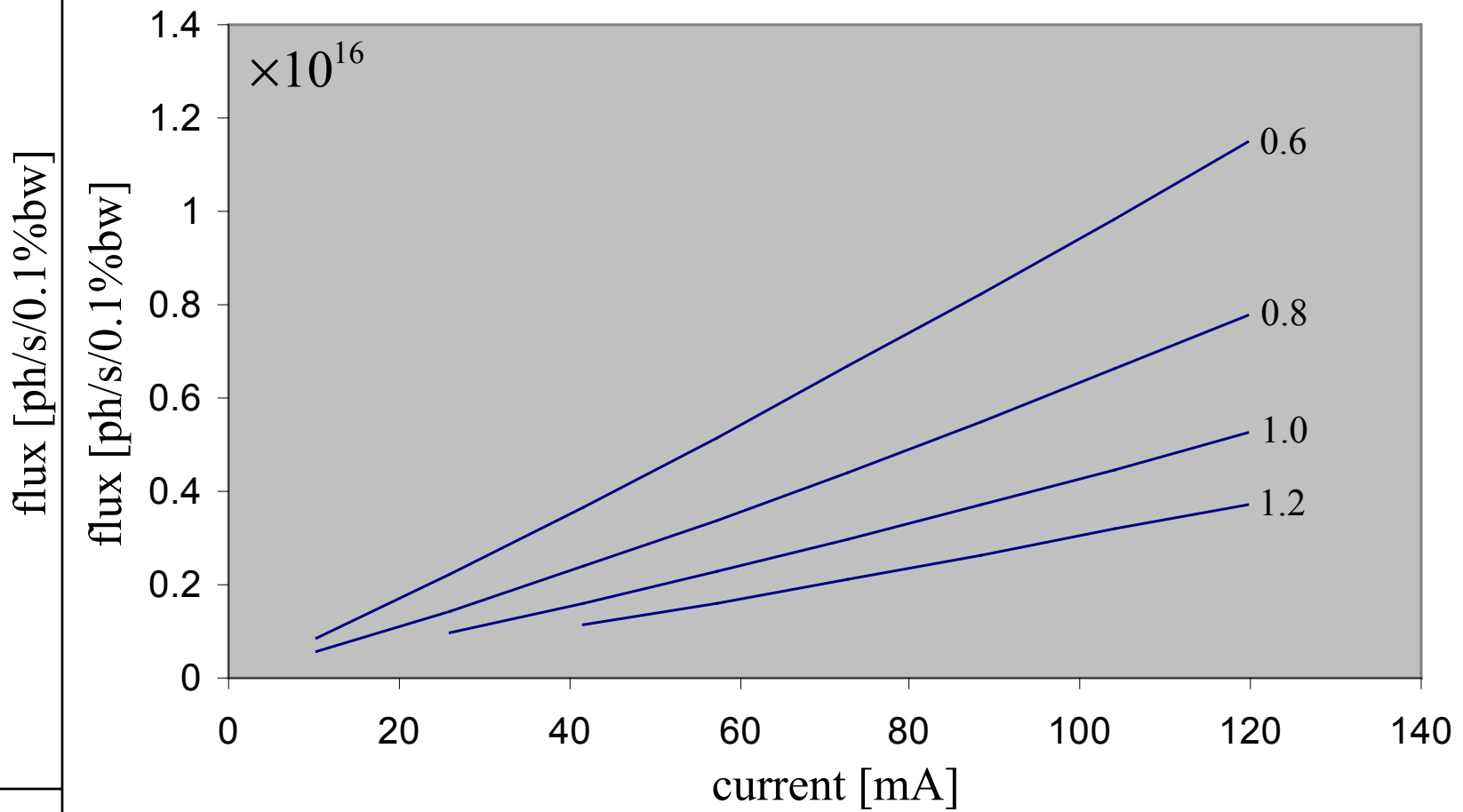


# Flux scaling

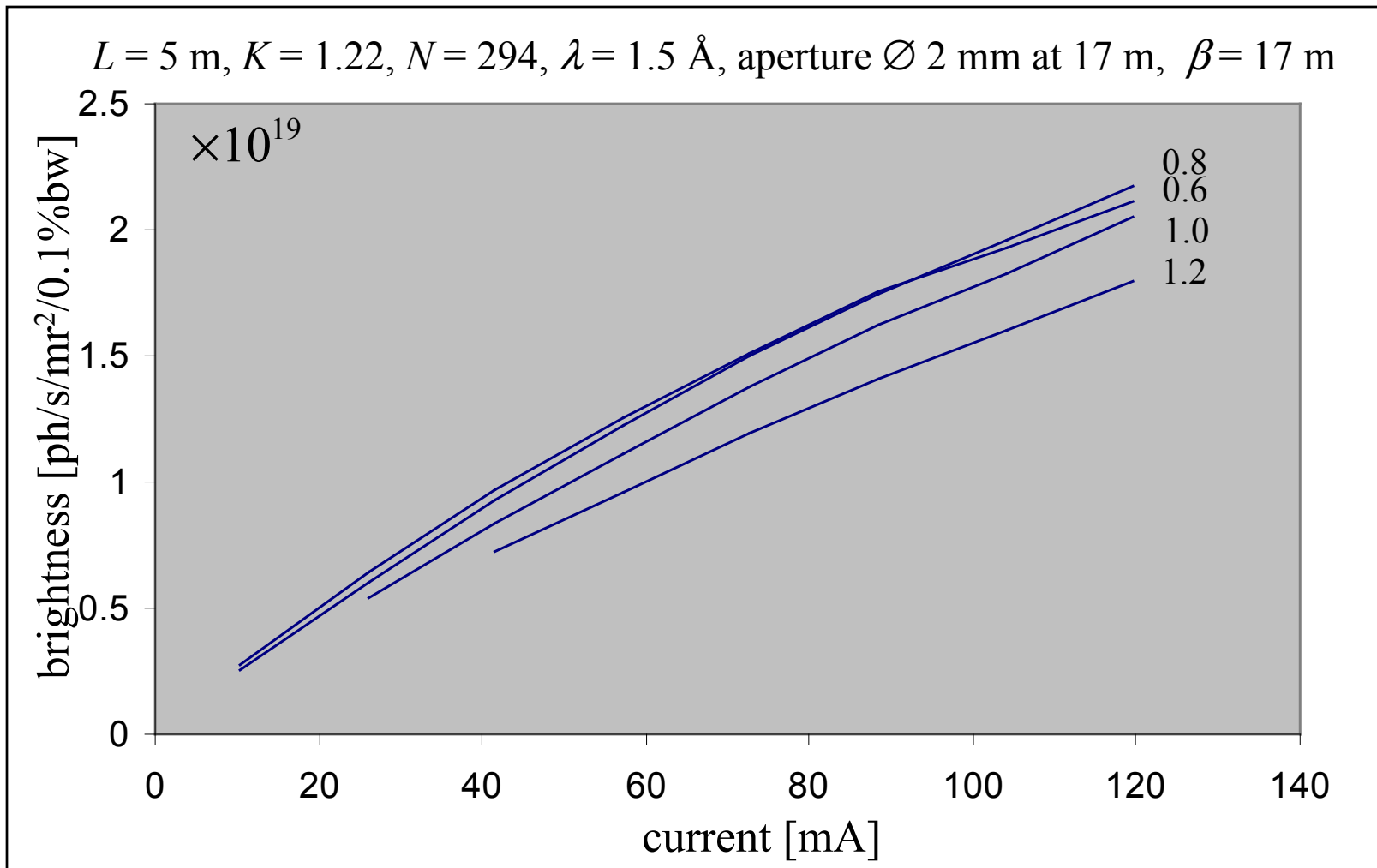


# Flux scaling

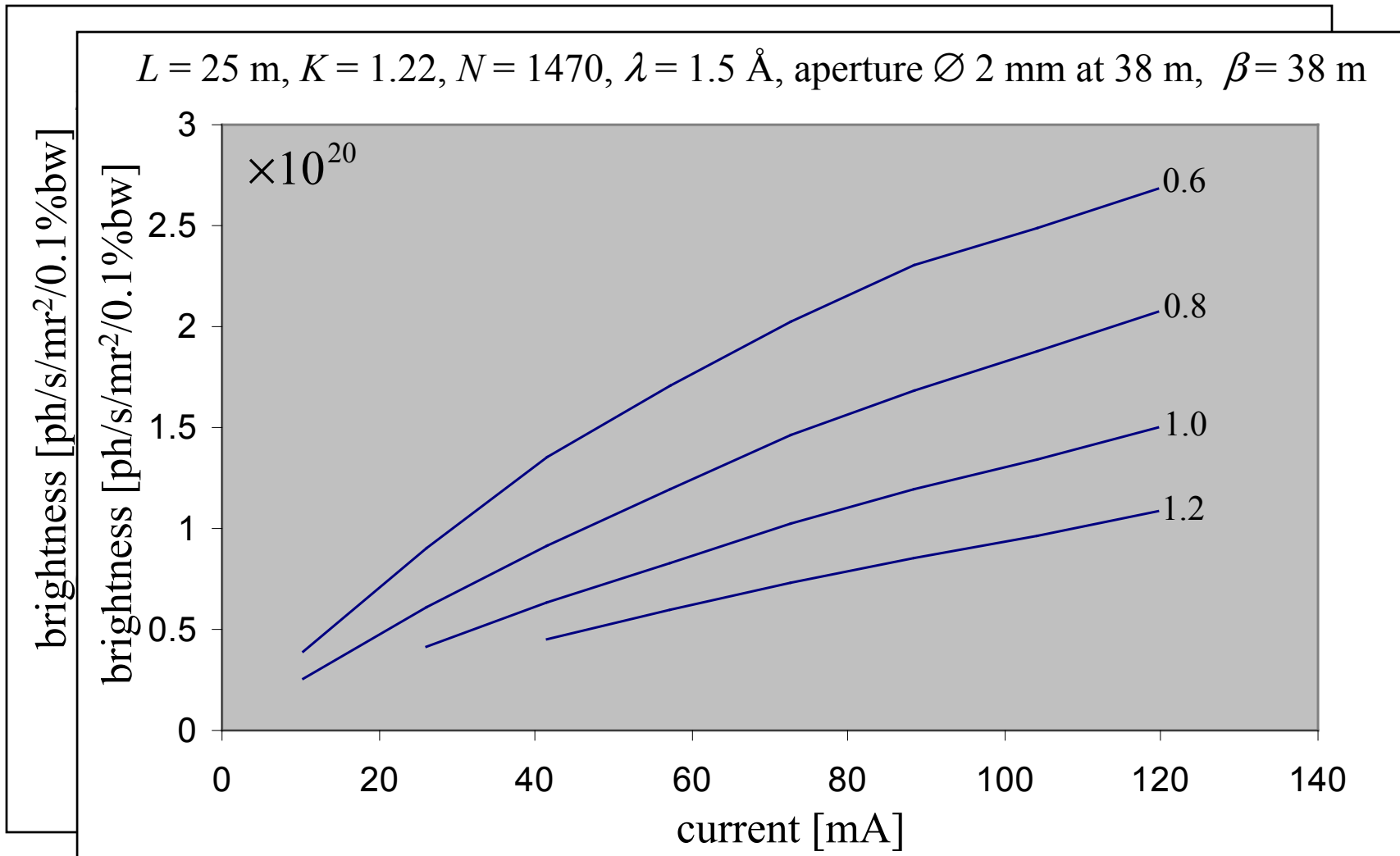
$L = 25$  m,  $K = 1.22$ ,  $N = 1470$ ,  $\lambda = 1.5$  Å, aperture  $\varnothing$  2 mm at 38 m,  $\beta = 38$  m



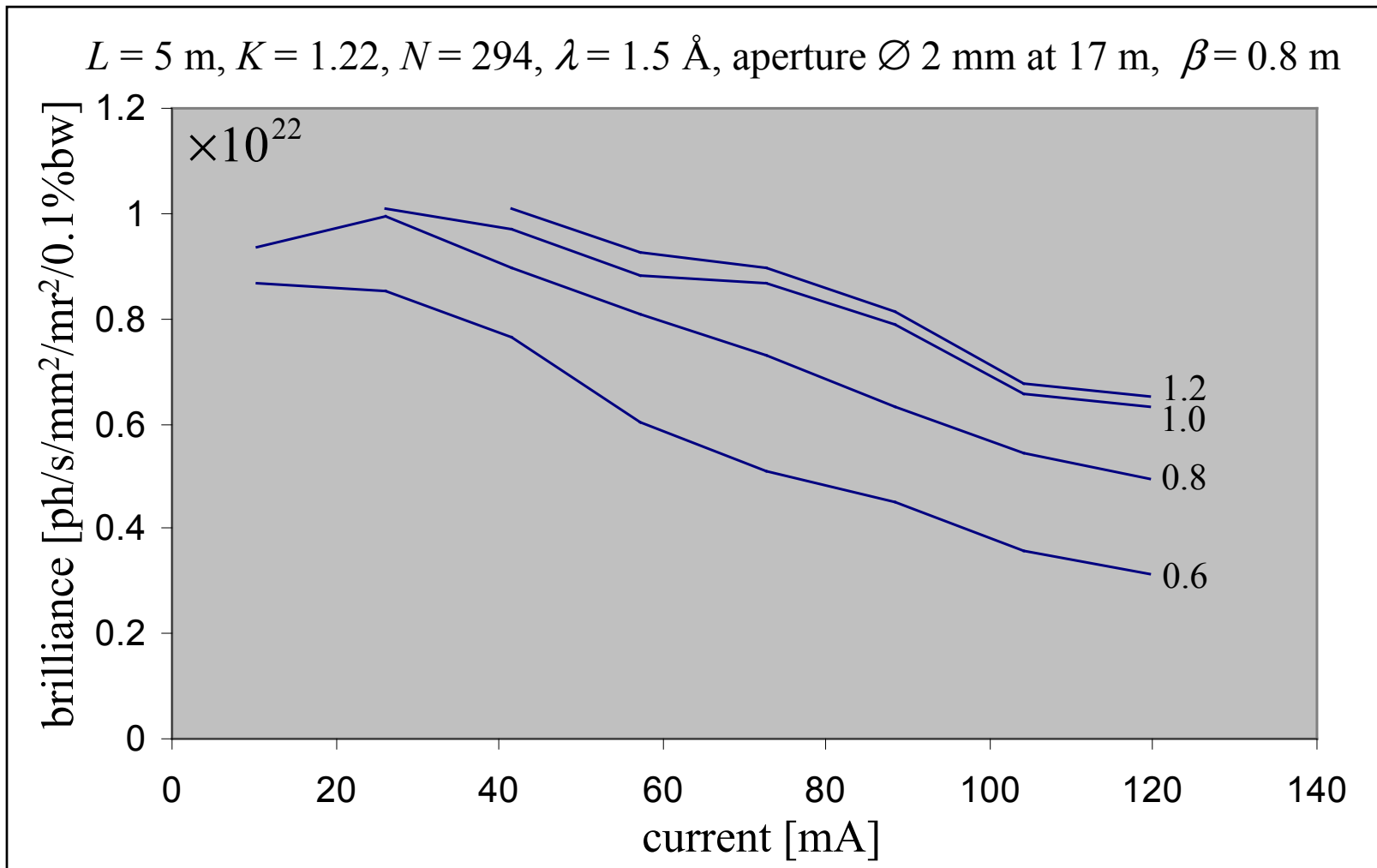
# Brightness scaling



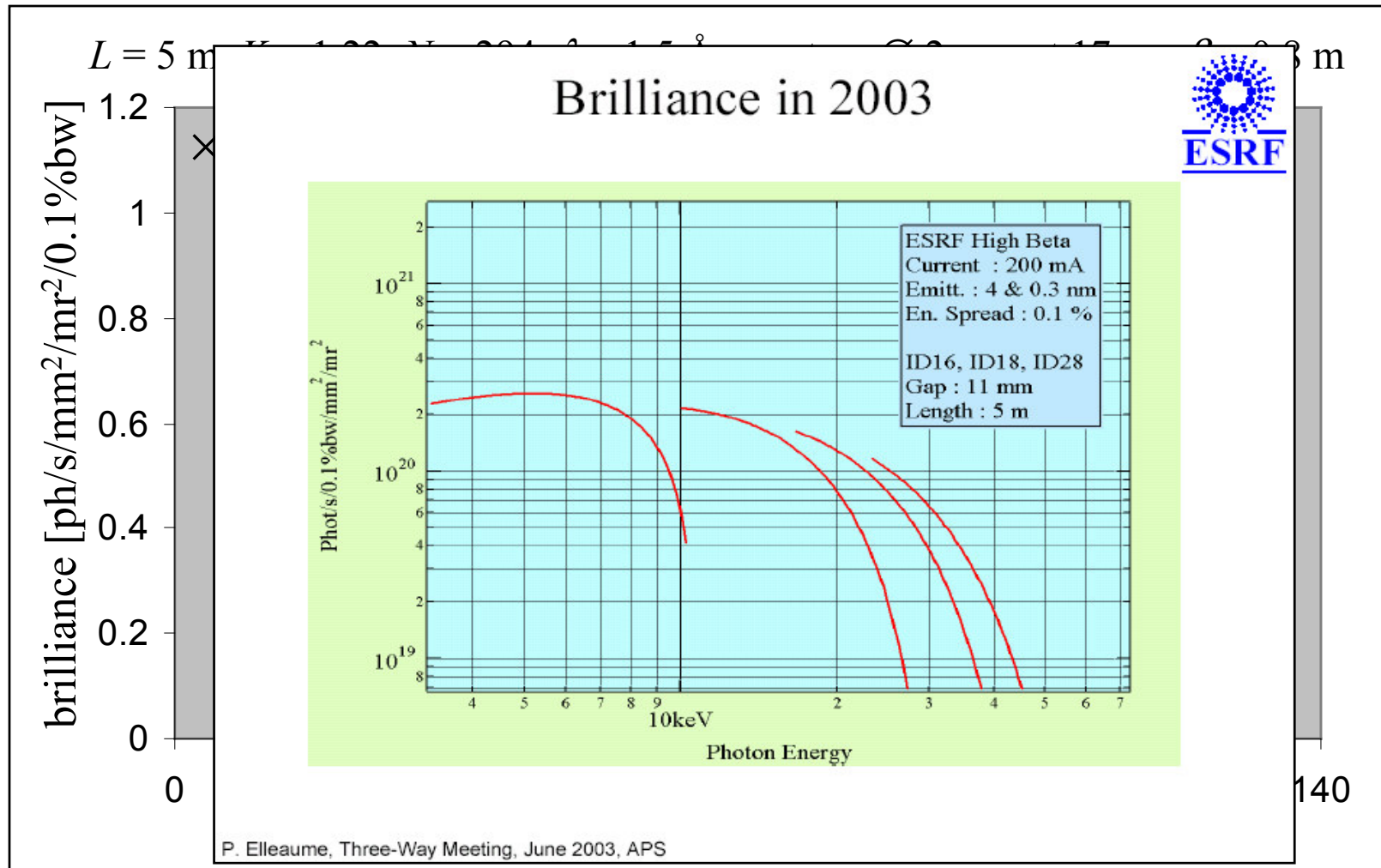
# Brightness scaling



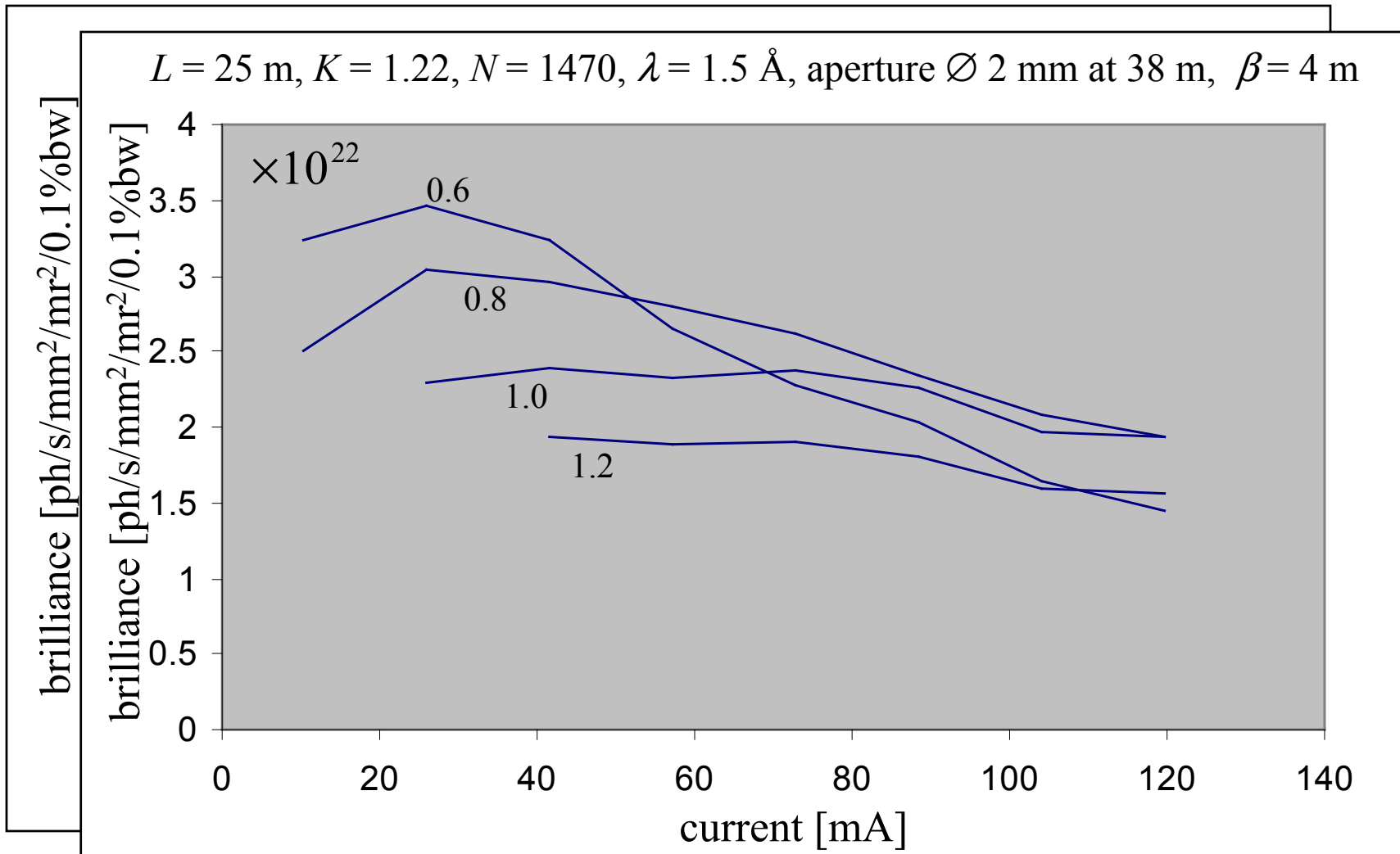
# Brilliance scaling



# Brilliance scaling



# Brilliance scaling





# Need small energy spread

# Need small energy spread

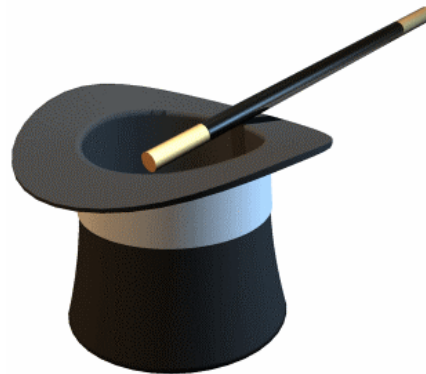
- compress the bunch length (either in the injector or early on in the main linac)

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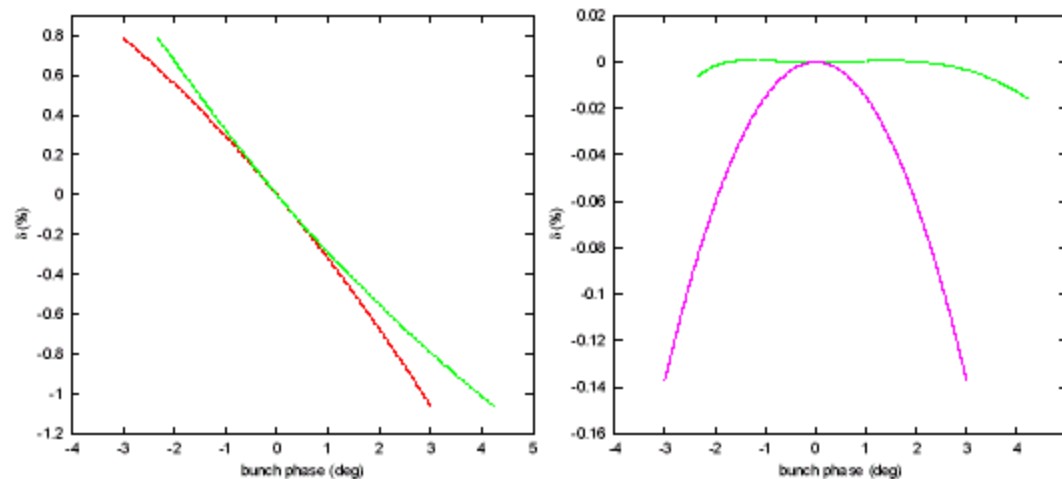
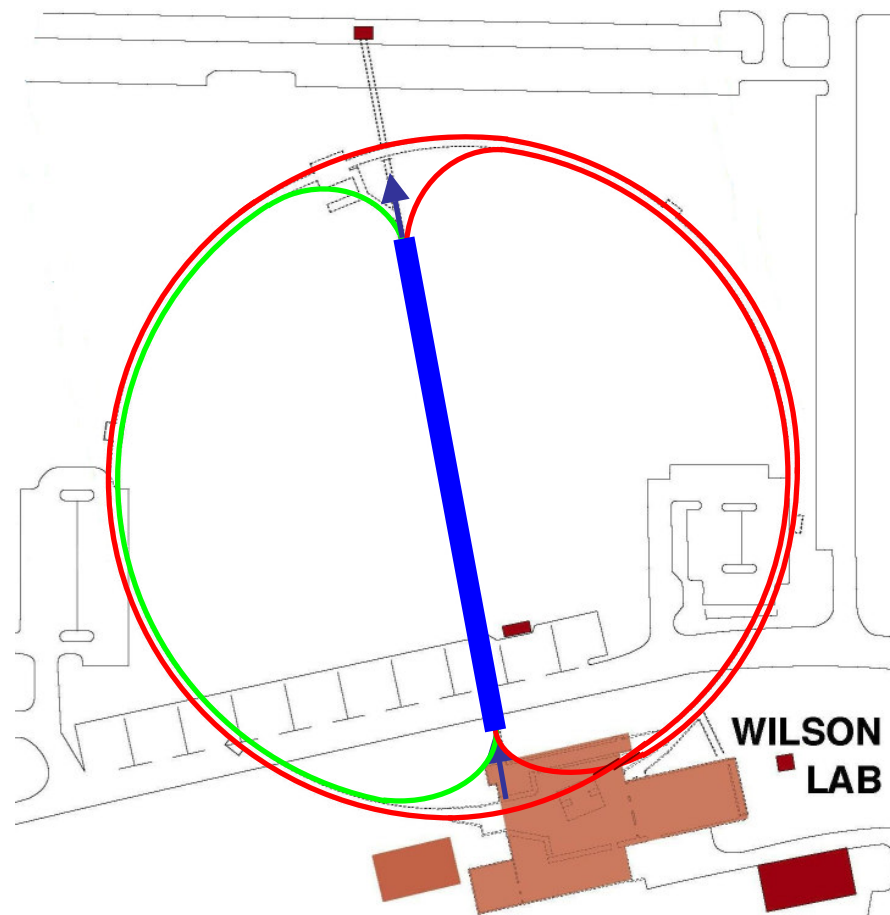
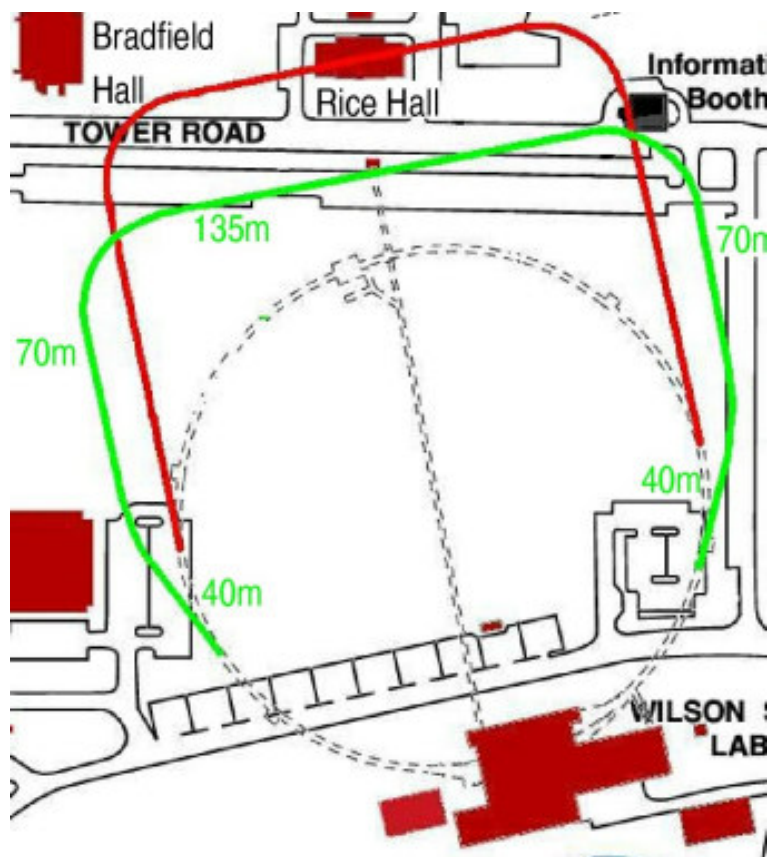
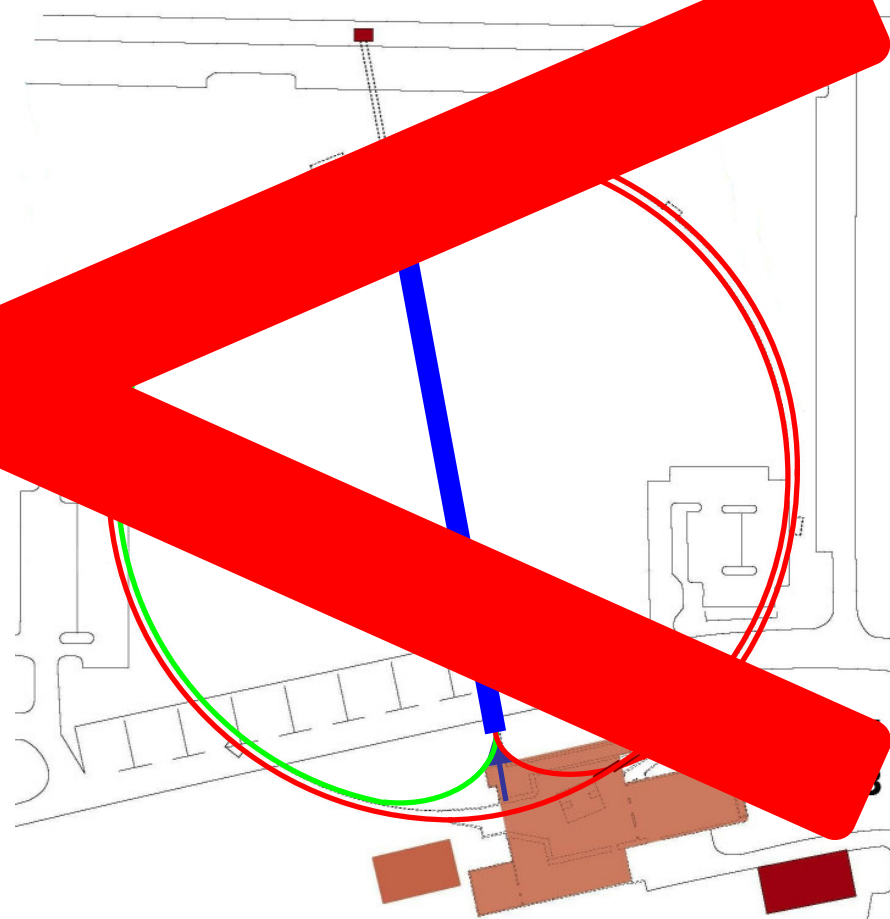


Figure 3. Energy spread compression using split linac configuration. On the left: longitudinal phase-space after the first section (solid line) and after properly chosen  $T_{566}$  (dashed line). On the right: the phase-space after linear and quadratic correlations have been removed after the second linac section. Phase-space distribution for on-crest operation is shown for comparison (dotted line).

# Laying out ERL x-ray source



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# Laying out ERL x-ray source

We're starting from the wrong end!

Should layout x-ray laboratories, beamlines, undulators first.

Accelerator folks will produce the rest of it.



# Observation

# Observation



# Observation



# Observation



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# Observation



*All ground level*

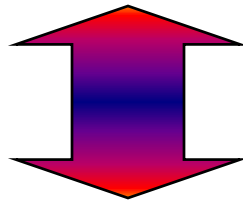


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## To do list

### X-ray folks

- (re)calculate photon budget & design beamlines' frontend (30 – 70 m) with specific applications / science case in mind, layout lab-space, undulators ( $\geq 12$ , i.e. should not be less than CHESS beamlines)



### Accelerator folks

- continue to resolve outstanding issues, proceed with detailed proposal for accelerator after the input from CHESS