

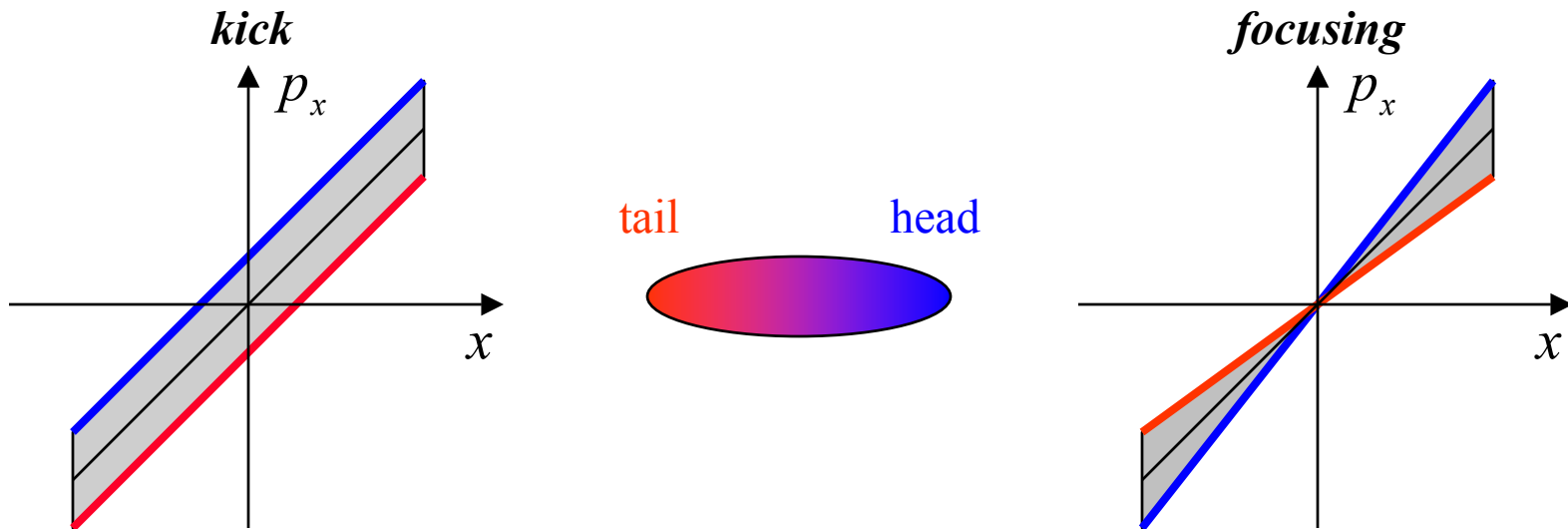
# RF emittance growth in the injector

- Cryomodule is integral part of the injector
- Must support small emittance
- Scale here is set by  $\leq 0.1$  mm-mrad
- RF emittance growth is due to time dependant transverse fields over nonzero bunch length (RF focusing, coupler kicks, tilted cavity)

# RF kick and focusing contributions

$$\varepsilon_n = \frac{1}{mc} \sqrt{\langle x^2 \rangle \langle p_x^2 \rangle - \langle xp_x \rangle^2}$$

$$p_x(x, z) = p_x(0,0) + \underbrace{\frac{\partial p_x}{\partial x} x}_{\text{kick}} + \underbrace{\frac{\partial p_x}{\partial z} z + \frac{\partial^2 p_x}{\partial x \partial z} xz}_{\text{focusing}} + \dots$$



## Some comments

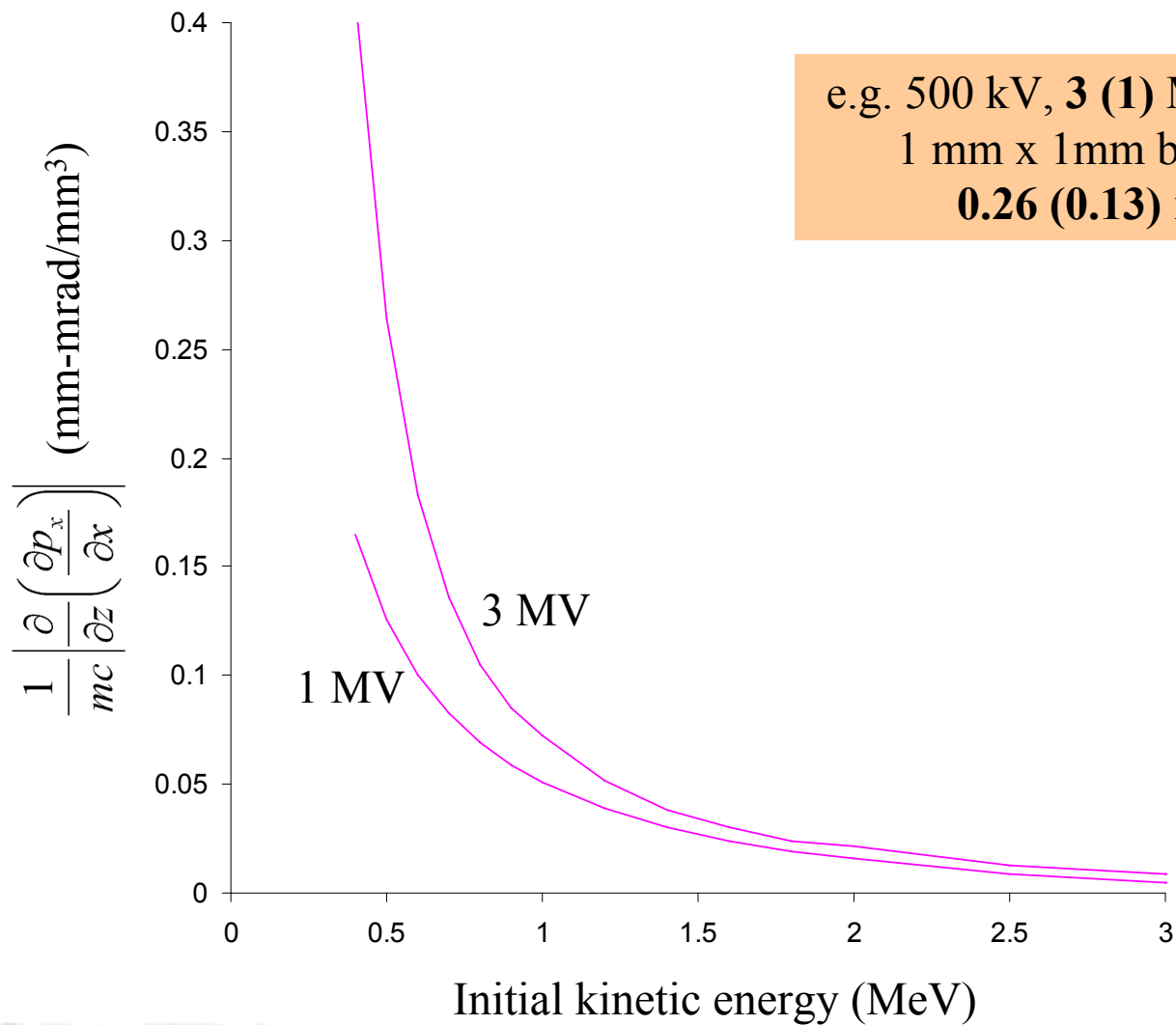
$$\varepsilon_n^2 = \varepsilon_0^2 + \varepsilon_{kick}^2 + \varepsilon_{focus}^2$$

- Kick effect on emittance is energy independent and can be cancelled downstream
- RF focusing effect scales  $\propto \frac{1}{\gamma}$  and generally is not cancelled

$$\varepsilon_{kick} = \frac{1}{mc} \left| \frac{\partial p_x}{\partial z} \right| \sigma_x \sigma_z$$

$$\varepsilon_{focus} = \frac{1}{mc} \left| \frac{\partial^2 p_x}{\partial z \partial x} \right| \sigma_x^2 \sigma_z$$

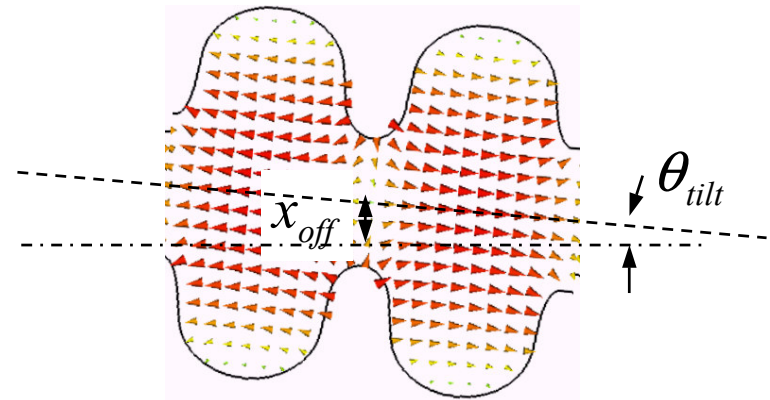
# RF focusing in 2-cell cavity (on crest!)



## RF kick (coupler kick is zero)

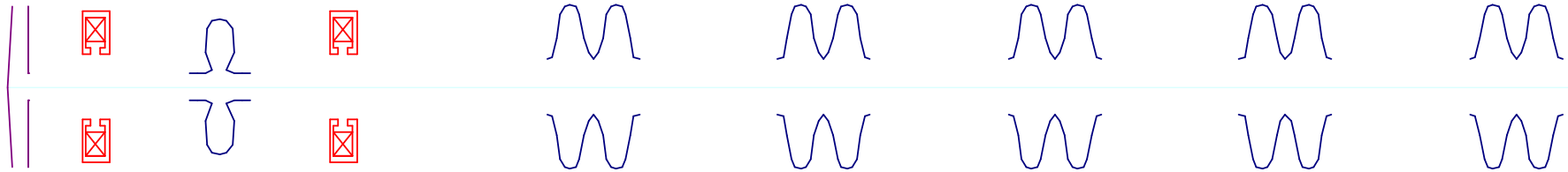
$$\varepsilon_{kick} \approx \sigma_x \sigma_z \left[ \underbrace{\theta_{tilt} \frac{\Delta E}{mc^2} k_{RF} \sin \varphi}_{\text{tilt}} + \underbrace{x_{off} \frac{1}{mc} \frac{\partial}{\partial z} \left( \frac{\partial p_x}{\partial x} \right)}_{\text{offset}} \right]$$

e.g. **3 MeV** energy gain  
for 1 mm x 1mm yields  
**0.16 sin  $\varphi$  mm-mrad**  
per mrad of **tilt**



- One would prefer on-crest running in the injector (and elsewhere!) from tolerances' point of view

# Typical injector settings in sims

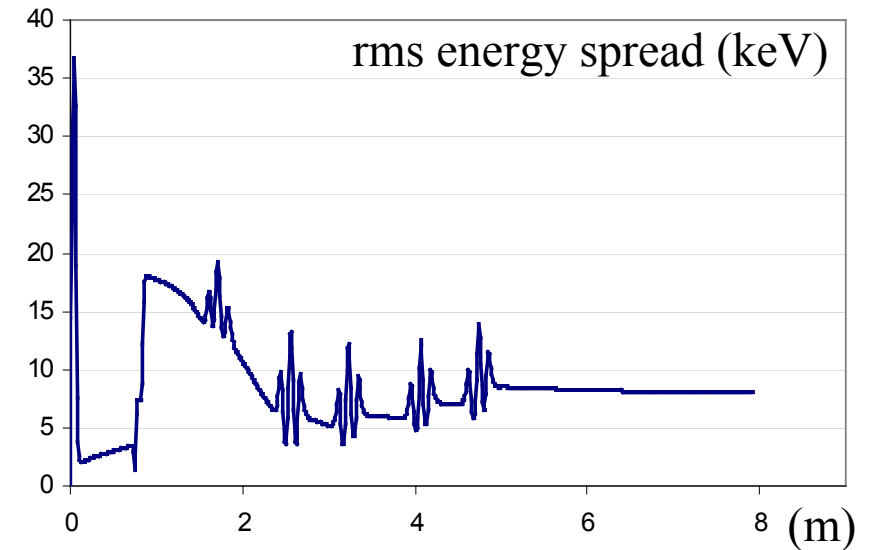
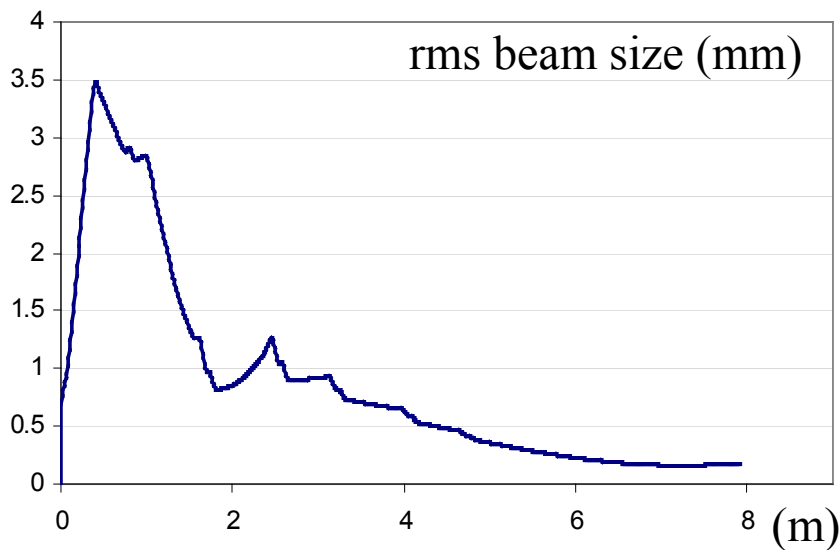
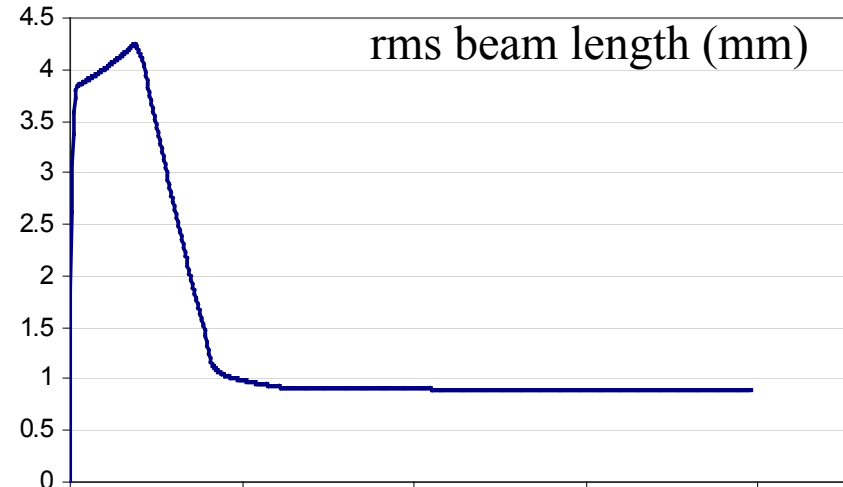
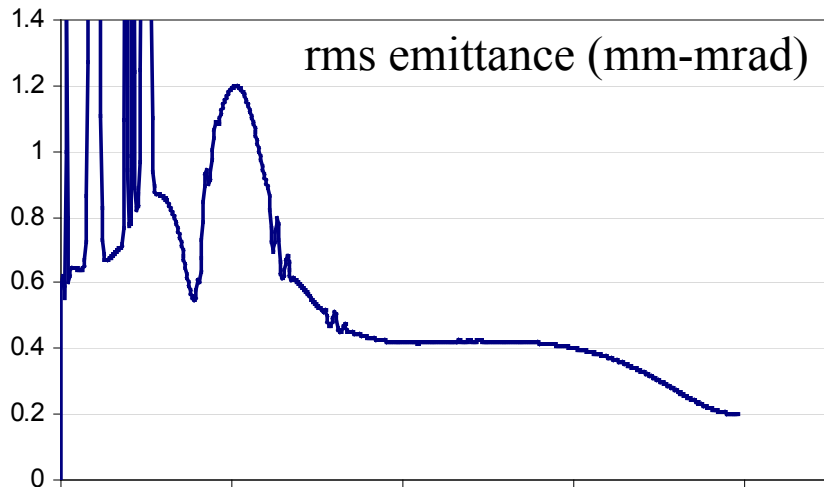


	Peak $E_z$ field (MV/m)	Phase (deg)
Gun	10	n/a
Buncher	3.0	-90
Cavity 1	12.3	-3
Cavity 2-5	25.3	-1.5

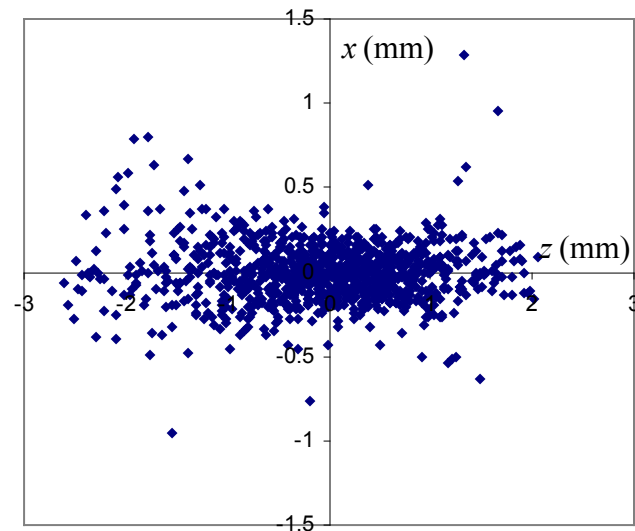
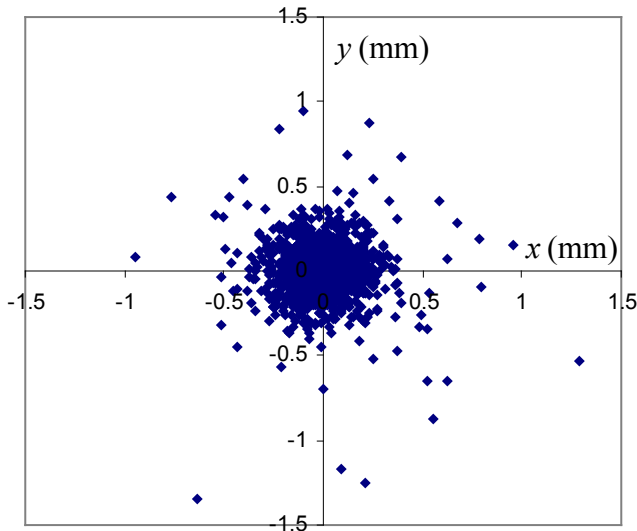
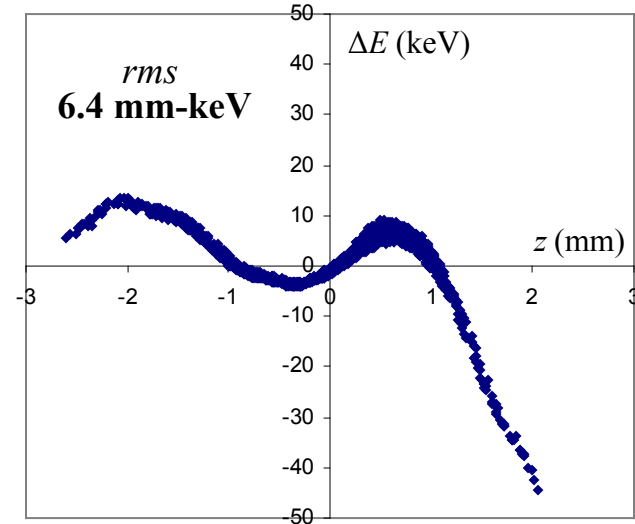
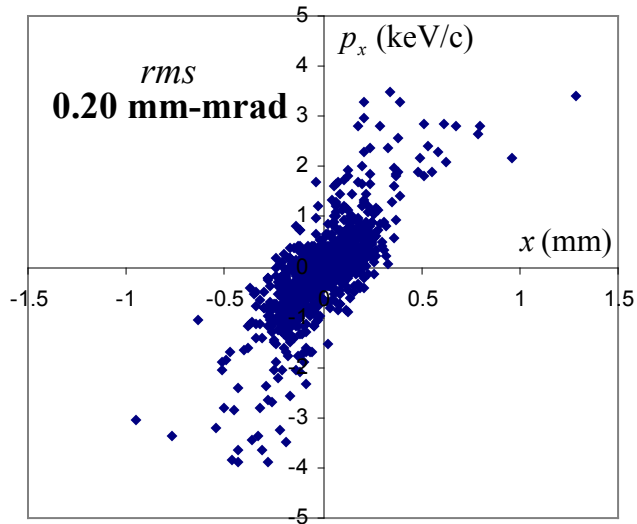
	Peak $B_z$ field (kG)
Solenoid 1	0.58
Solenoid 2	0.42

Charge / bunch (pC)	80
Distribution ( $x, t$ )	uniform
$\sigma_x$ (mm)	0.6
$\sigma_t$ (ps)	12

# Beam parameters in the injector (80 pC, 13.5 MeV)



# Bunch at the end





## Summary

- Tilt tolerance is phase dependant. Assuming 15 RF deg maximum off-crest angle, tolerance of  $\sim$  **mrاد** is required. Several mrad might be fine if the beam is not run off-crest.
- RF focusing in the 1<sup>st</sup> cavity is a noticeable contributor to the emittance. It is good enough to make displacement of the 1<sup>st</sup> cavity to be half of the rms beam size, thus, **0.5 mm** for the 1<sup>st</sup> cavity position alignment should do the job. Other cavities can be worse than that.